

# Fans, Ducts and Air Handling Systems: Design, Performance and Commissioning Issues

## Ducts



Instructor:

David Sellers

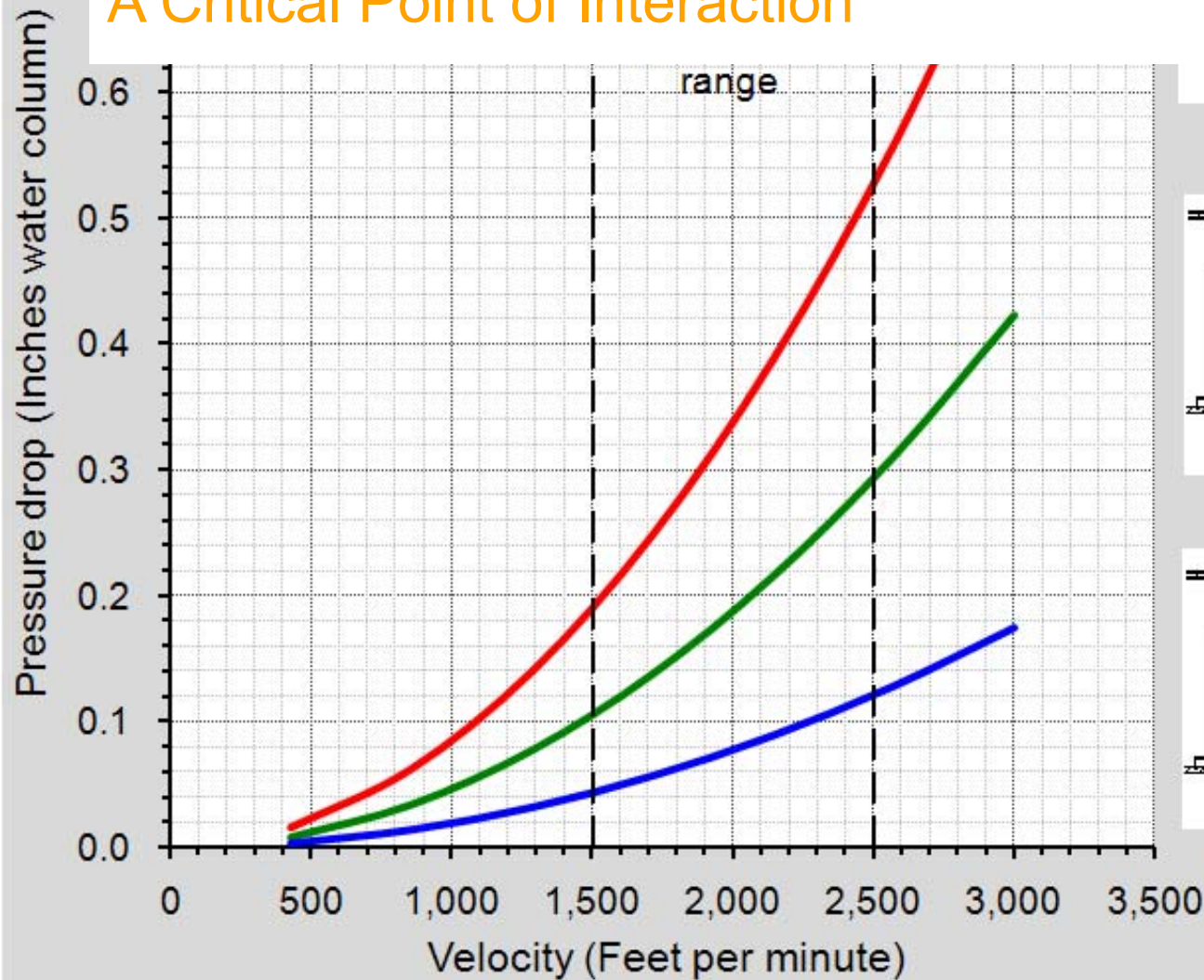
Senior Engineer

Facility Dynamics Engineering

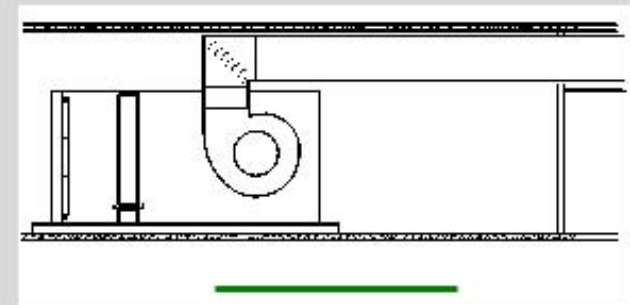
November 7, 2017



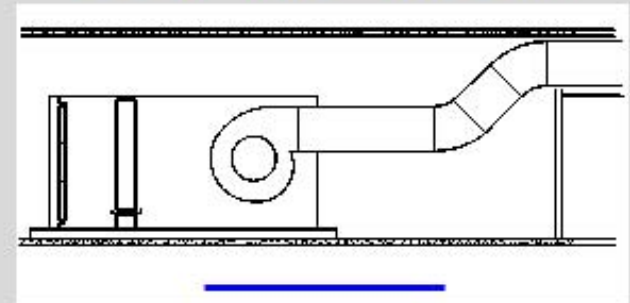
# Fan to System Interface; A Critical Point of Interaction



Top discharge, reversed turn



Top discharge, forward turn

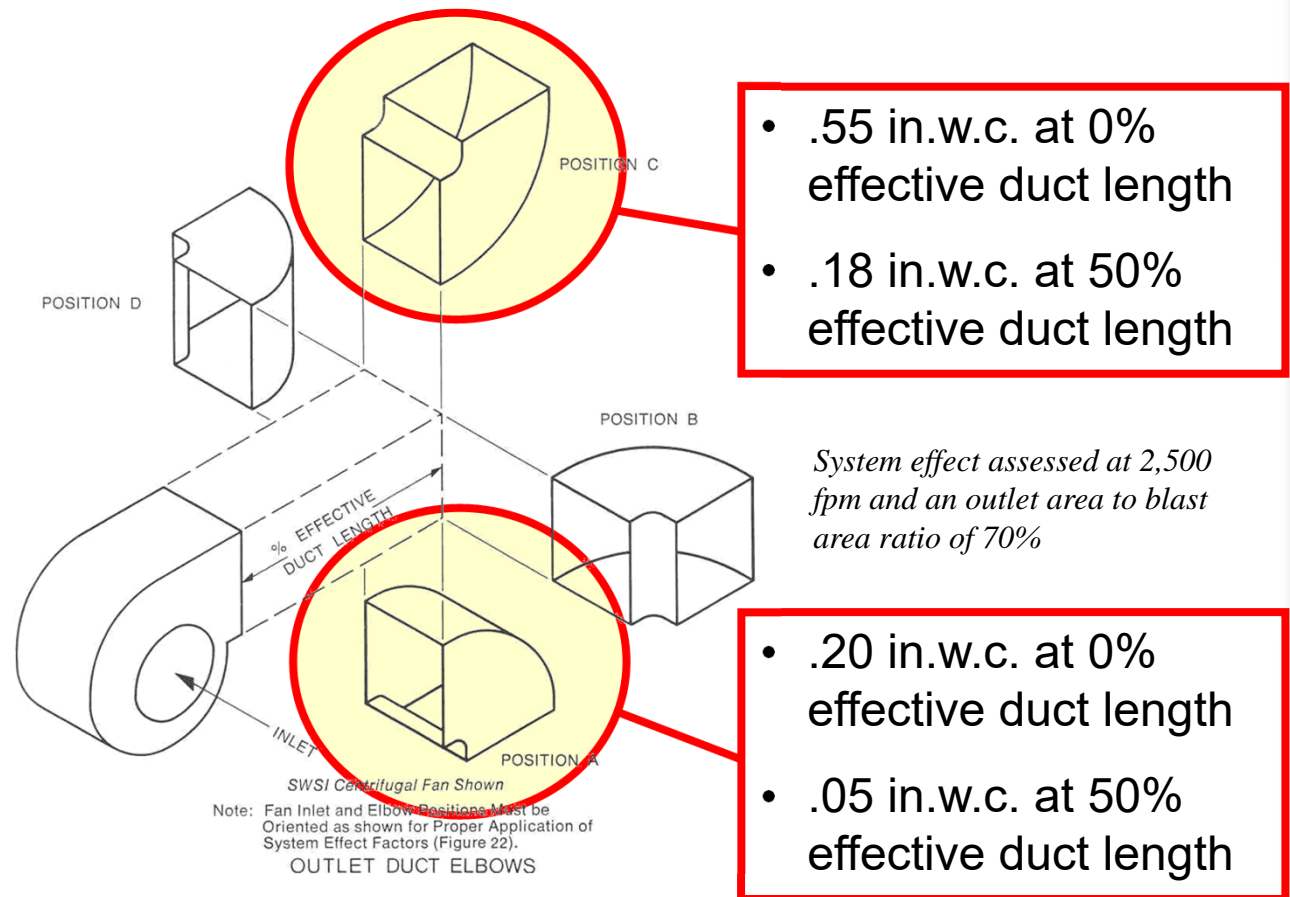


Front discharge with offset after  
100% effective duct length



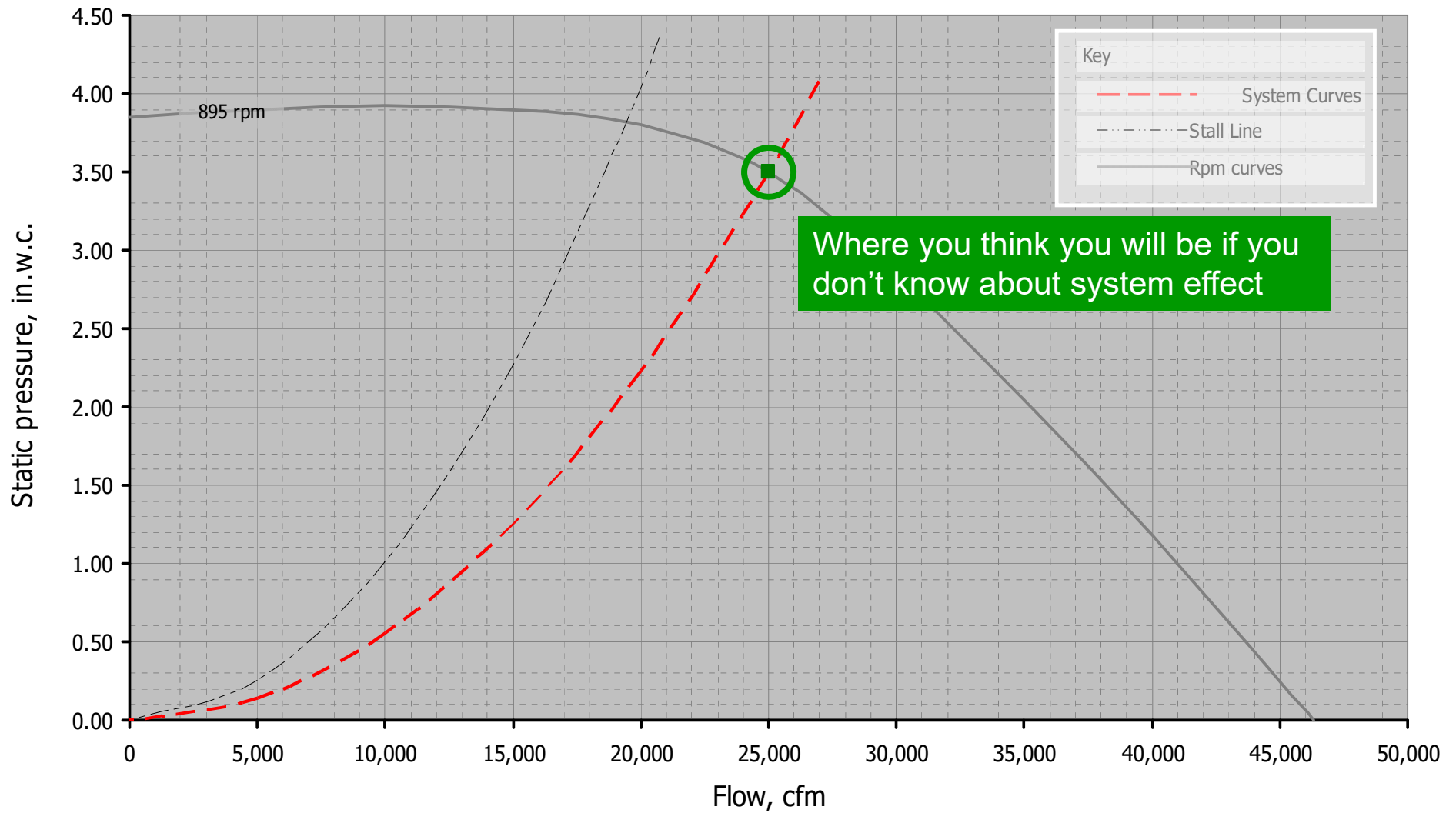
# System Effect Varies with Configuration

Fitting placement and/or lack of a discharge duct has the same effect as adding static pressure



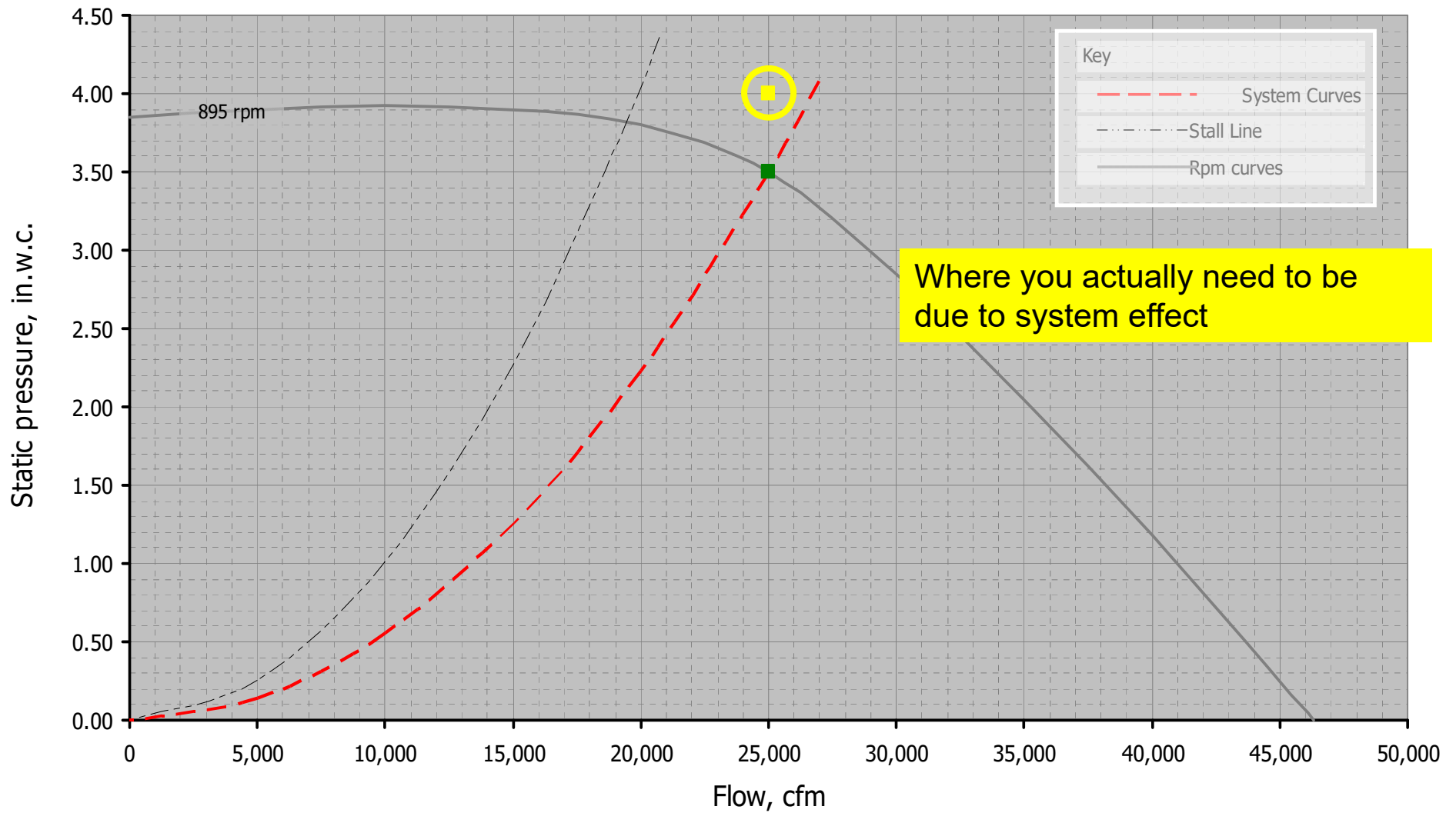


## Supply Fan - Greenheck 36-AFDW-41



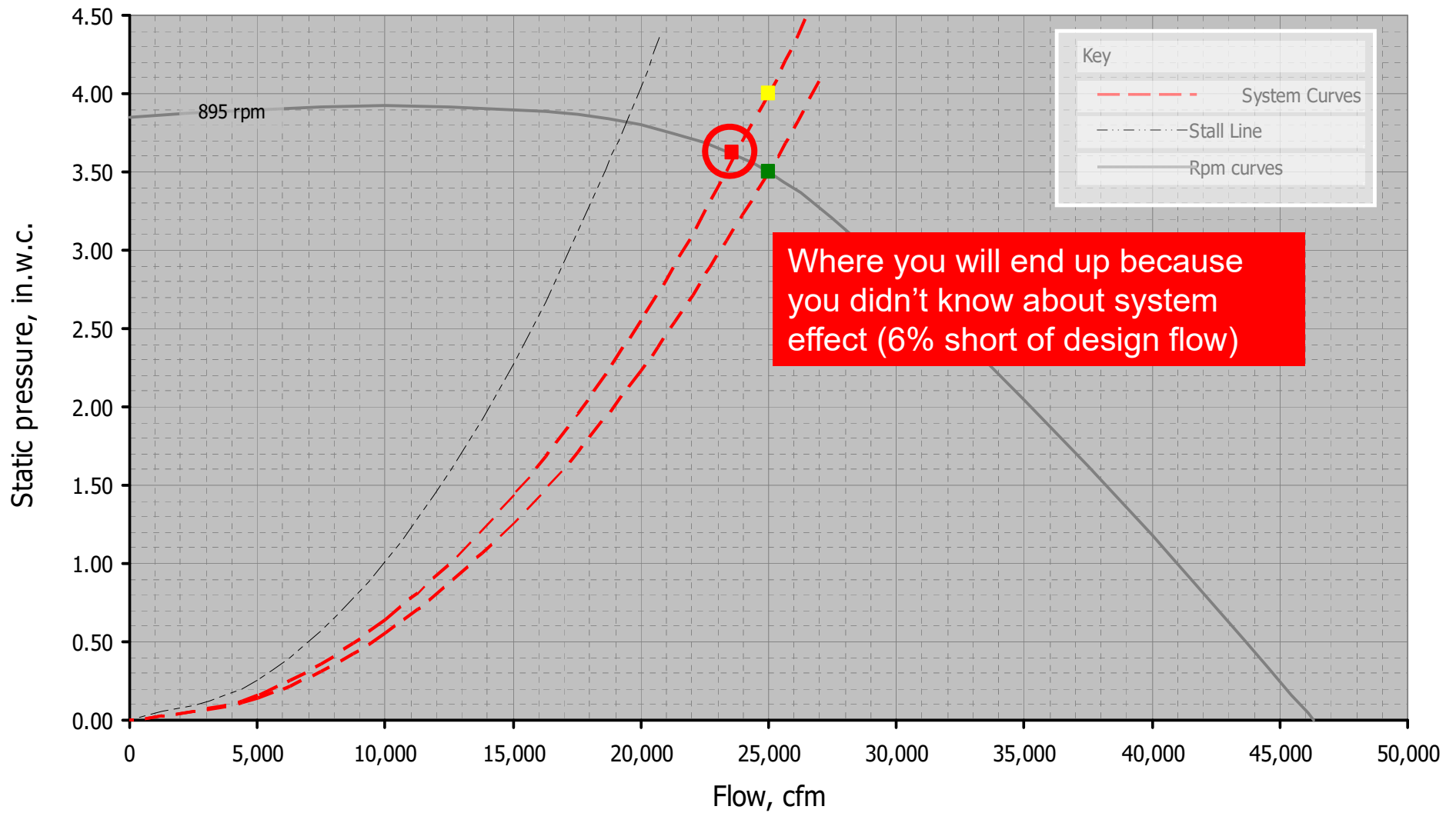


## Supply Fan - Greenheck 36-AFDW-41





## Supply Fan - Greenheck 36-AFDW-41





# Fan Energy is Directly Related to Flow and Fan Static Pressure

Flow rate – 25,000 cfm

Unnecessary static pressure burden – 0.50 in.w.c.

Fan static efficiency – 72%

Brake horsepower used - 2.8 bhp



# Motors Come in Standard Incremental Sizes

Fan brake horsepower requirement is typically less than the incremental motor horsepower supplied

Motor service factor provides some margin for error

- For our example:
  - Brake horsepower at design is approximately 18 bhp
  - Brake horsepower required if system effect is accommodated is approximately 21 bhp
  - Horsepower available from a 20 hp motor with a service factor of 1.15 is 23 hp

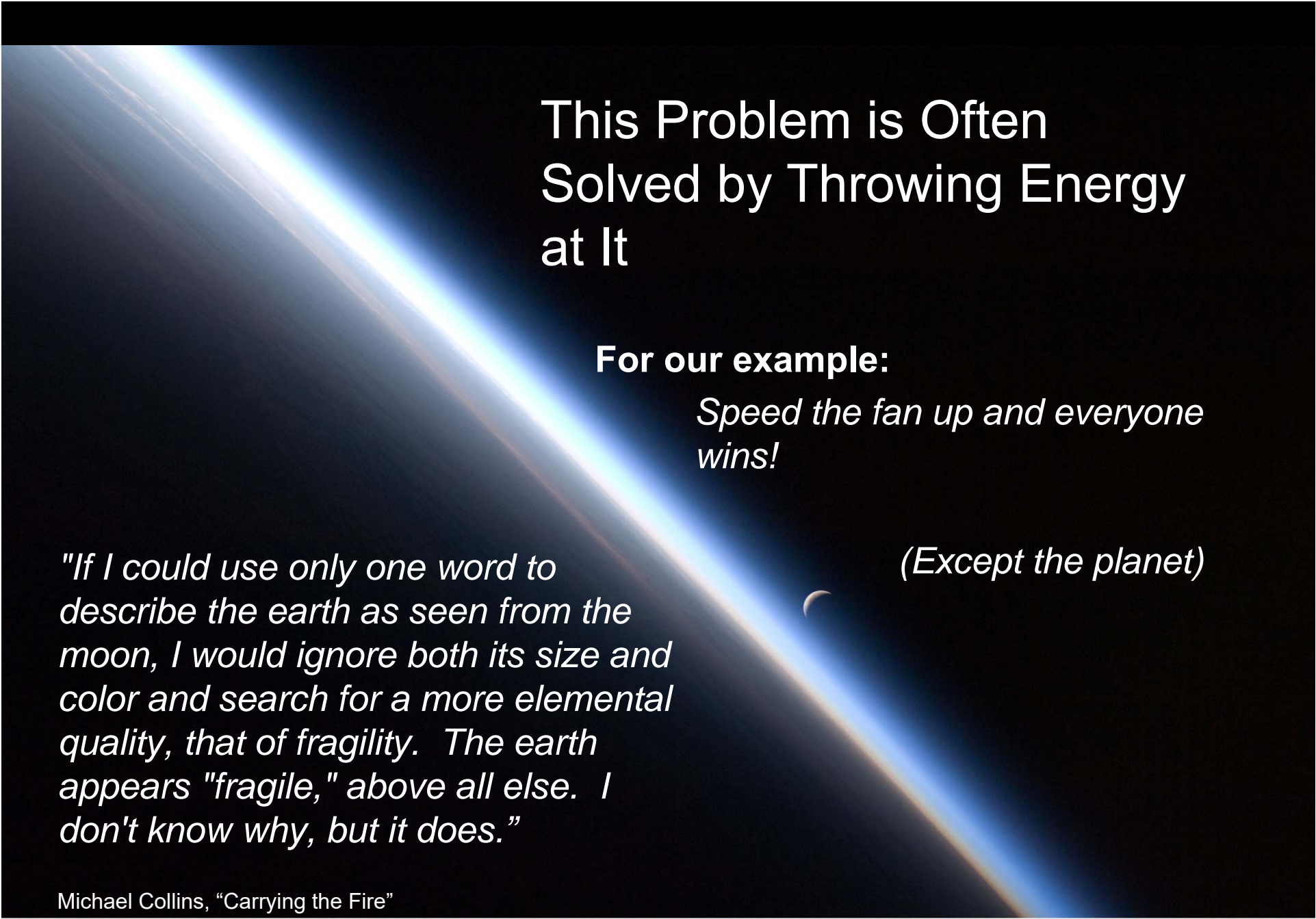


# This Problem is Often Solved by Throwing Energy at It

**For our example:**

*Speed the fan up and everyone  
wins!*





# This Problem is Often Solved by Throwing Energy at It

**For our example:**

*Speed the fan up and everyone  
wins!*

*"If I could use only one word to  
describe the earth as seen from the  
moon, I would ignore both its size and  
color and search for a more elemental  
quality, that of fragility. The earth  
appears "fragile," above all else. I  
don't know why, but it does."*

*(Except the planet)*

Michael Collins, "Carrying the Fire"

ISS024E013421

*Image Courtesy NASA ISS Image Archives*



A photograph of four children sitting on a wicker porch swing. From left to right: a boy in a green cap and white shirt, a girl in a pink shirt, a girl in a light blue patterned shirt, and a girl in a maroon shirt. They are all smiling. The swing is hanging from a chain. In the background, there is a house with green siding, a window, and a white pillar. A red fire hydrant is visible on the left. A large green plant with white flowers is in the foreground. The text "This Problem is Often Solved by Throwing Energy at It" is overlaid on the right side of the image.

# This Problem is Often Solved by Throwing Energy at It

*We don't inherit the world  
from our ancestors;  
We borrow it from our children*

Unknown

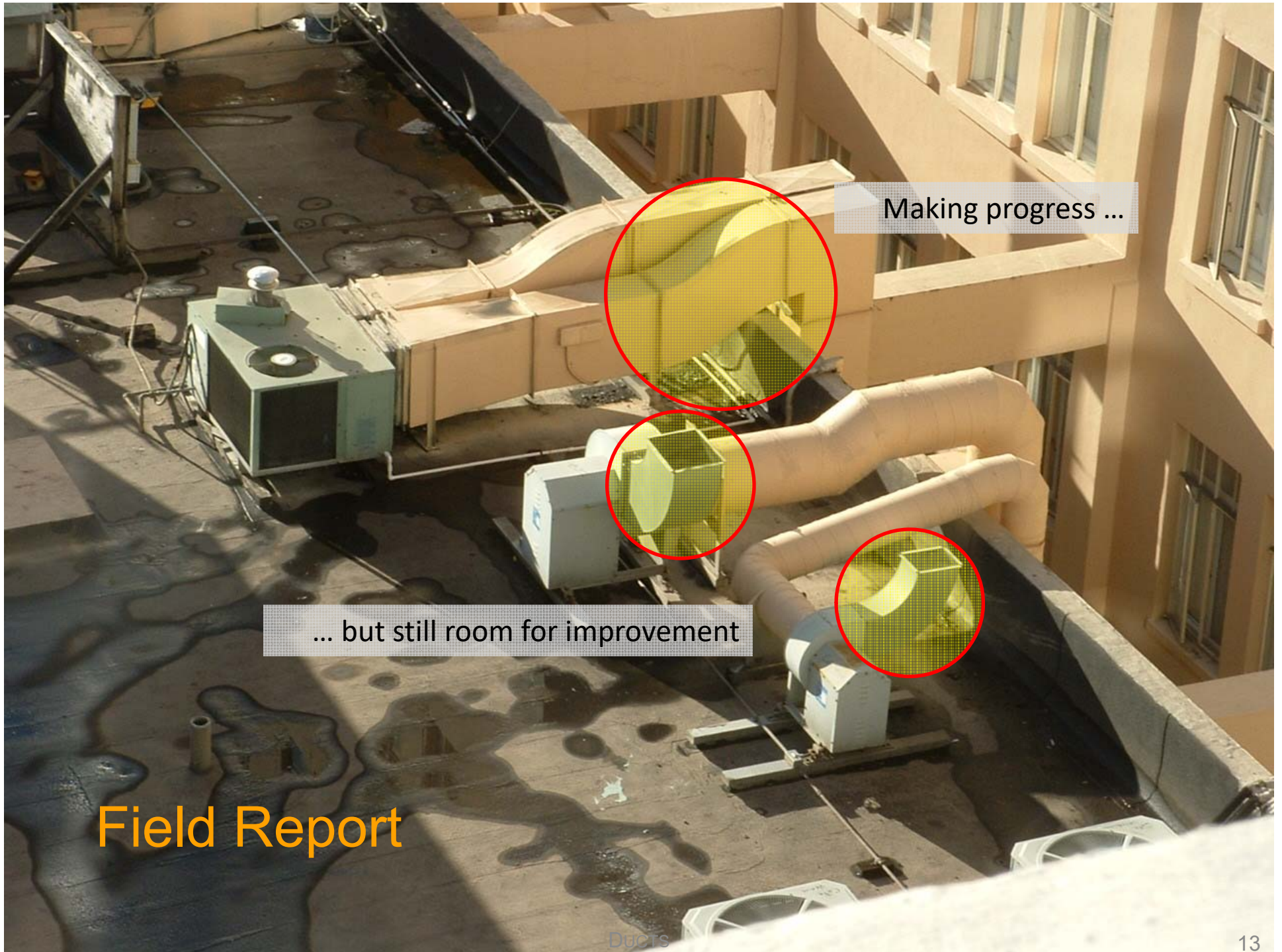


## Remember ...

*Simply using “Best Practices” could save significant fan energy*

*“Best Practices” are things we already know how to do*





Making progress ...

... but still room for improvement

## Field Report



# Effective Duct Length

For velocities of 2,500 fpm or less:

$$L_{\text{Effective100\%}} = 2.5 \times D_E$$

Where:

$L_{\text{Effective100\%}}$  = 100% effective duct length as defined by AMCA in consistent units

$D_E$  = Equivalent duct diameter in consistent units.

Note that the ASHRAE definition of an equivalent duct diameter for a round duct uses a different formula from the AMCA definition. The results are very similar however.

For velocities over 2,500 fpm:

$$L_{\text{Effective100\%}} = 2.5 \times D_E + \left( D_E \times \left( \frac{V - 2,500}{1,000} \right) \right)$$

Where:

$V$  = Duct velocity in feet per minute

AMCA 210 requires that the outlet duct has an area no greater than 105% and no less than 95% of the fan outlet area. It also specifies that the slope of a transition element on the discharge be no greater than 15° for converging elements and no greater than 7° for diverging elements.



# Rectangular Duct Equivalent Diameter

## ASHRAE Basis

$$D_e = \frac{1.3 \times (a \times b)^{.625}}{(a + b)^{.25}}$$

Where:

$D_e$  = The equivalent circular duct diameter in consistent units

$a$  = The dimension of one side of the rectangular duct in consistent units

$b$  = The dimension of the other side of the rectangular duct in consistent units

Source = ASHRAE Handbook of Fundamentals based on work by Huebscher (1948), who developed the relationship. ASHRAE uses it to determine size equivalency based on equal flow, resistance, and length for the table in the Handbook of Fundamentals.



# Rectangular Duct Equivalent Diameter

## AMCA Basis

$$D_e = \left( \frac{4 \times a \times b}{\pi} \right)^{0.5}$$

Where:

$D_e$  = The equivalent circular duct diameter in consistent units

$a$  = The dimension of one side of the rectangular duct in consistent units

$b$  = The dimension of the other side of the rectangular duct in consistent units

Source = AMCA 201-01, referencing AMCA 99-0066



# Flat Oval Duct Equivalent Diameter

## ASHRAE Basis

$$D_e = \frac{1.55 \times A_{FlatOval}^{.625}}{P_{FlatOval}^{.25}}$$

Where:

$D_e$  = The equivalent circular duct diameter in consistent units

$A_{FlatOval}$  = The cross sectional area of the flat oval duct in consistent units (see below)

$P_{FlatOval}$  = The perimeter of the flat oval duct in consistent units

$$A_{FlatOval} = \left( \frac{\pi a^2}{4} \right) + (a \times (A - a))$$

Where:

$A$  = The major axis of the flat oval duct (the wide dimension) in consistent units

$a$  = The minor axis of the flat oval duct (the narrow dimension) in consistent units

$$P_{FlatOval} = (\pi \times a) + (2 \times (A - a))$$

Source = ASHRAE Handbook of Fundamentals based on work by Heyt and Diaz (1975) who developed the relationship. ASHRAE uses it to determine size equivalency based on equal flow, resistance, and length for the table in the Handbook of Fundamentals.



# Hydraulic Diameter

$$D_h = 4 \times \left( \frac{A}{P} \right)$$

Where:

$D_h$  = The hydraulic diameter of the duct or pipe in consistent units

$A$  = The duct or pipe area in consistent units

$P$  = The perimeter of the duct or pipe cross-section in consistent units

Source = ASHRAE Handbook of Fundamentals Chapter 21



# Darcy Equation for Friction Loss in Duct

$$\Delta p_{Friction} = \left( \frac{12 \times f \times L}{D_h} \right) \times \rho \times \left( \frac{V}{1,097} \right)^2$$

Where:

$\Delta p_{Friction}$  = Friction loss for a given length of duct in inches of water column

$f$  = Dimensionless friction factor from the Colebrook equation or a Moody Diagram

$L$  = Duct length in feet

$D_h$  = Hydraulic diameter in inches

$\rho$  = Density in pounds per cubic foot

$V$  = Velocity in feet per minute



# Reynolds Number

If you look up the friction factor in a Moody Chart, you will need to know Reynolds number and relative roughness.

$$Re = \left( \frac{D_h \times V}{720 \times \nu} \right)$$

Where:

$Re$  = Reynolds number (dimensionless)

$D_h$  = Hydraulic diameter in inches

$V$  = Velocity in feet per minute

$\nu$  = kinematic viscosity in feet squared per second

For air between 40 and 100°F, this equation can be simplified to:

$$Re = 8.50 \times D_h \times V$$

Source - ASHRAE Handbook of Fundamentals Chapter 21



# Relative Roughness

Relative roughness is determined from absolute roughness and hydraulic diameter as follows:

$$\text{Relative Roughness} = \frac{\varepsilon}{D_h}$$

Where

$\varepsilon$  = Absolute roughness factor in feet (determined by experiment)

Absolute roughness is determined via experiment.

If you use the Colebrook equation, you have to iterate to a solution based on Reynolds number, absolute roughness, and hydraulic diameter.



# Nikuardse's Experiment

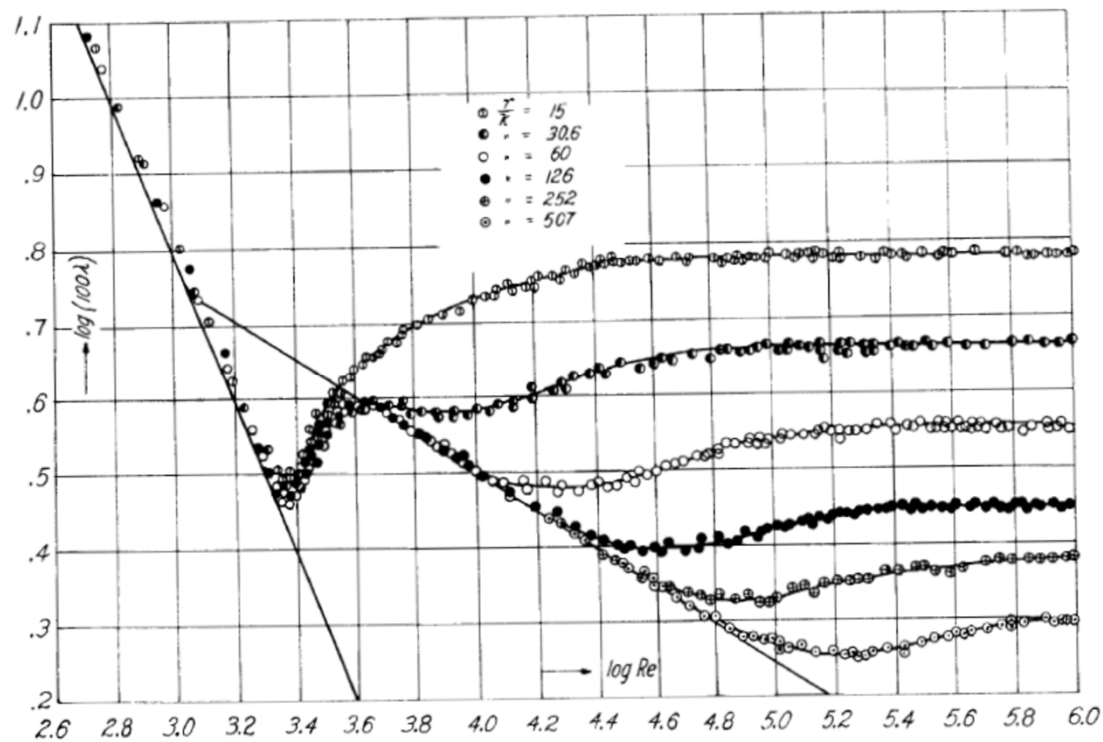


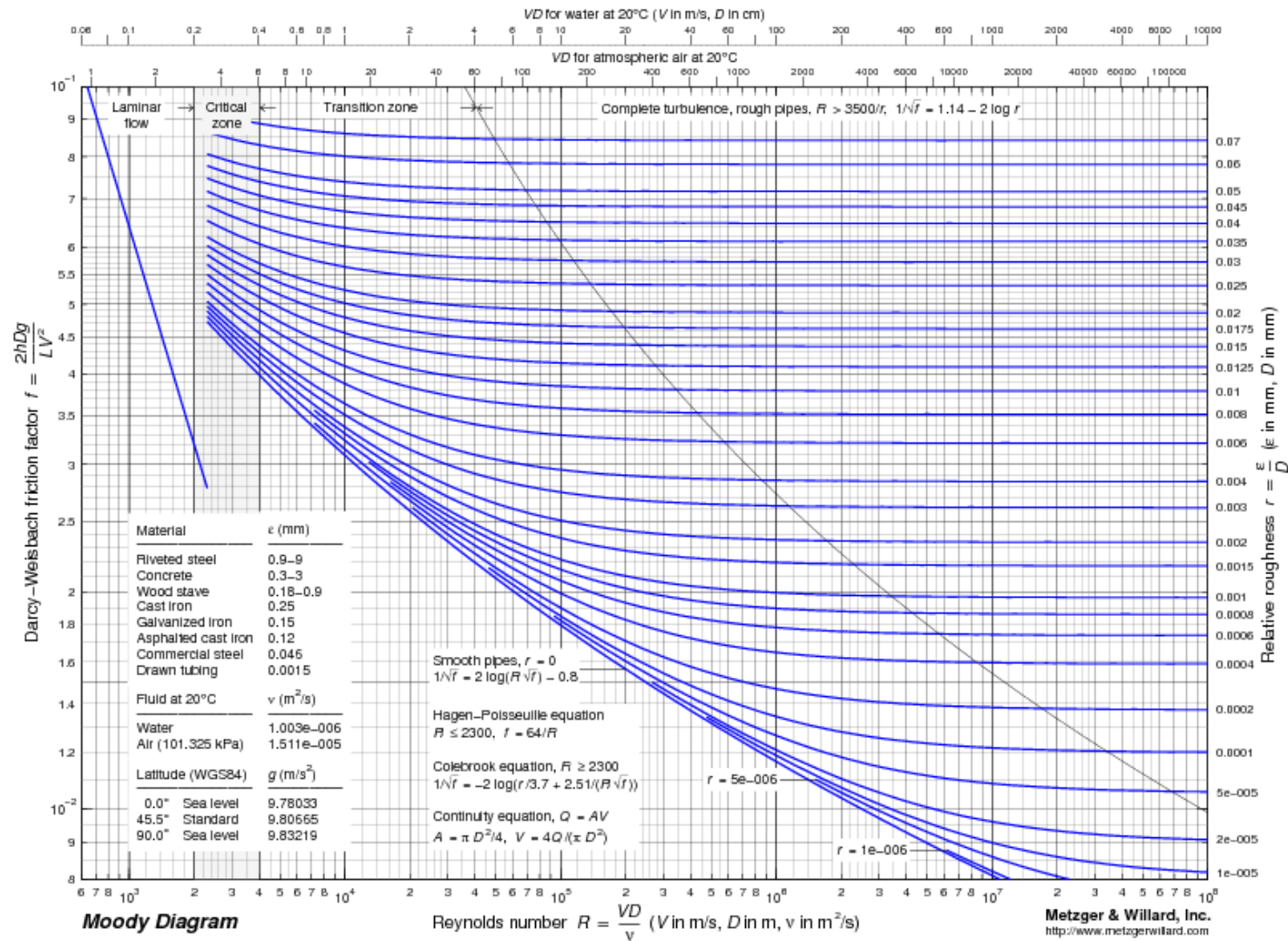
Figure 9.- Relation between  $\log(100\lambda)$  and  $\log Re$ .

NACA TM 1292

51



# Moody Diagram





# Duct Friction Chart

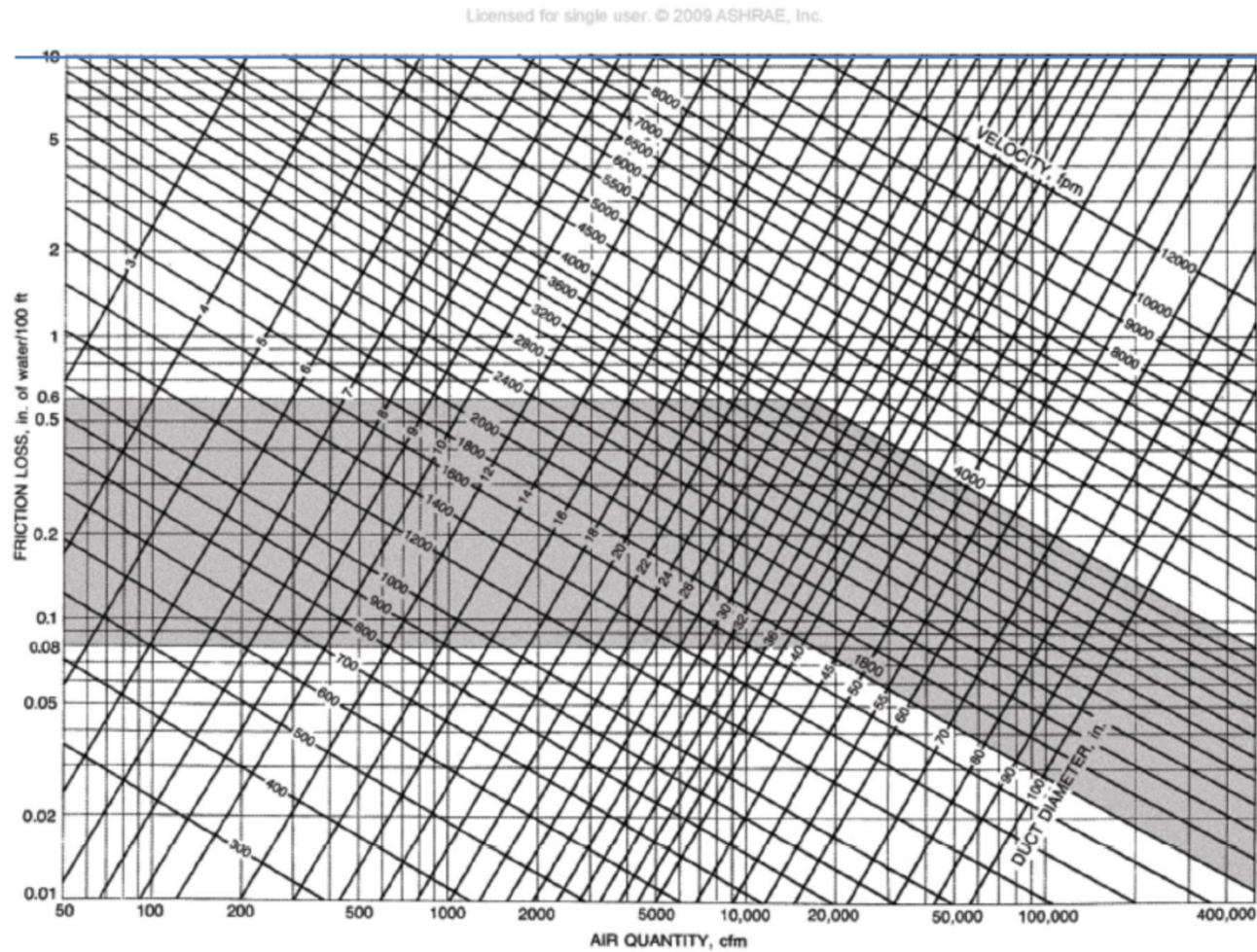


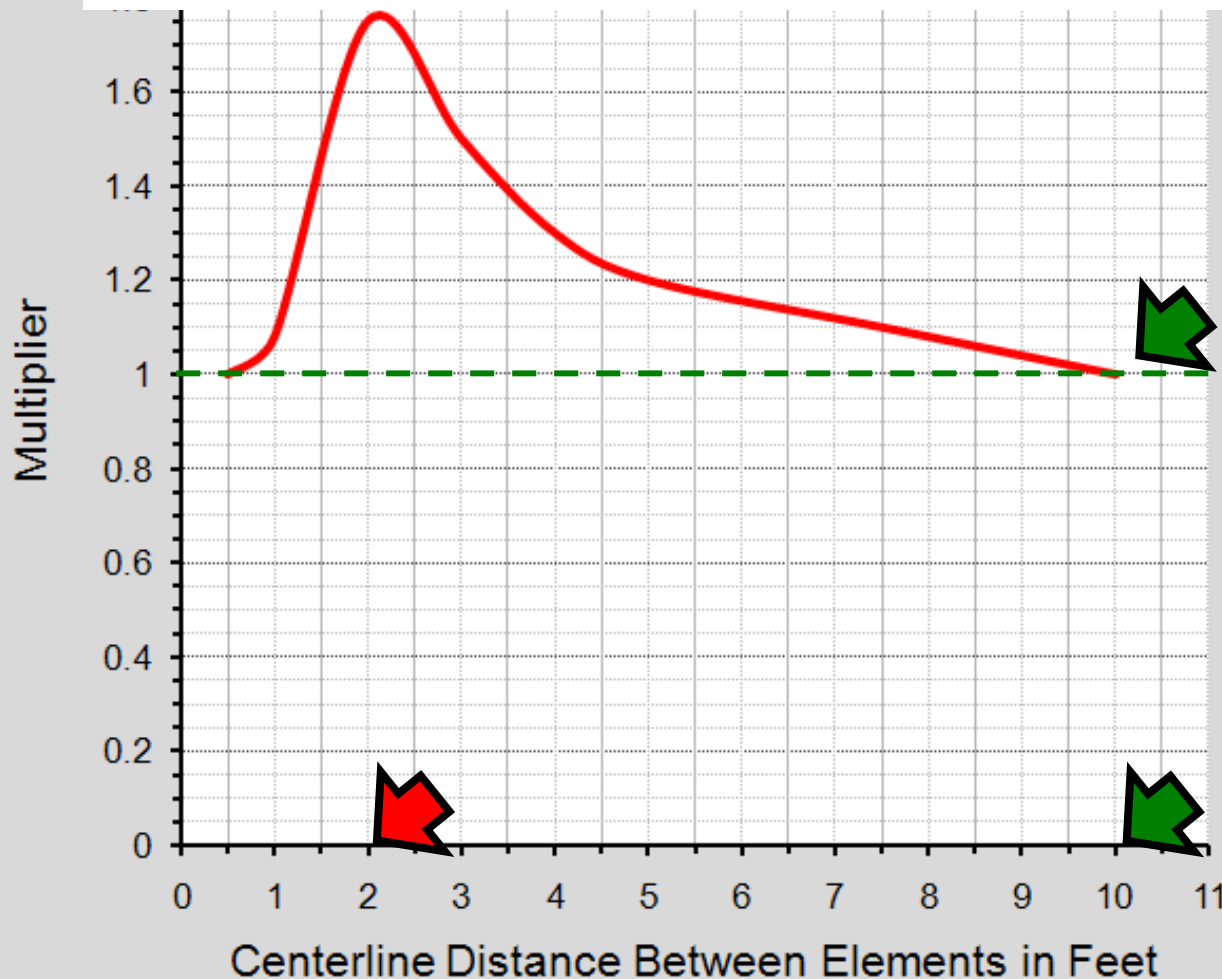
Fig. 9 Friction Chart for Round Duct ( $\rho = 0.075 \text{ lb}_m/\text{ft}^3$  and  $\epsilon = 0.0003 \text{ ft}$ )

21.8

2009 ASHRAE Handbook—Fundamentals



# System Effect and Duct Fittings (Fittings Interact!)



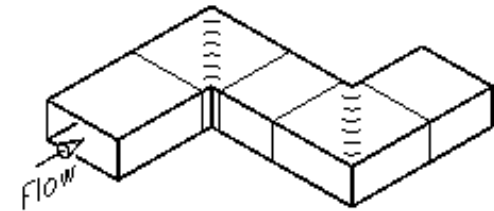
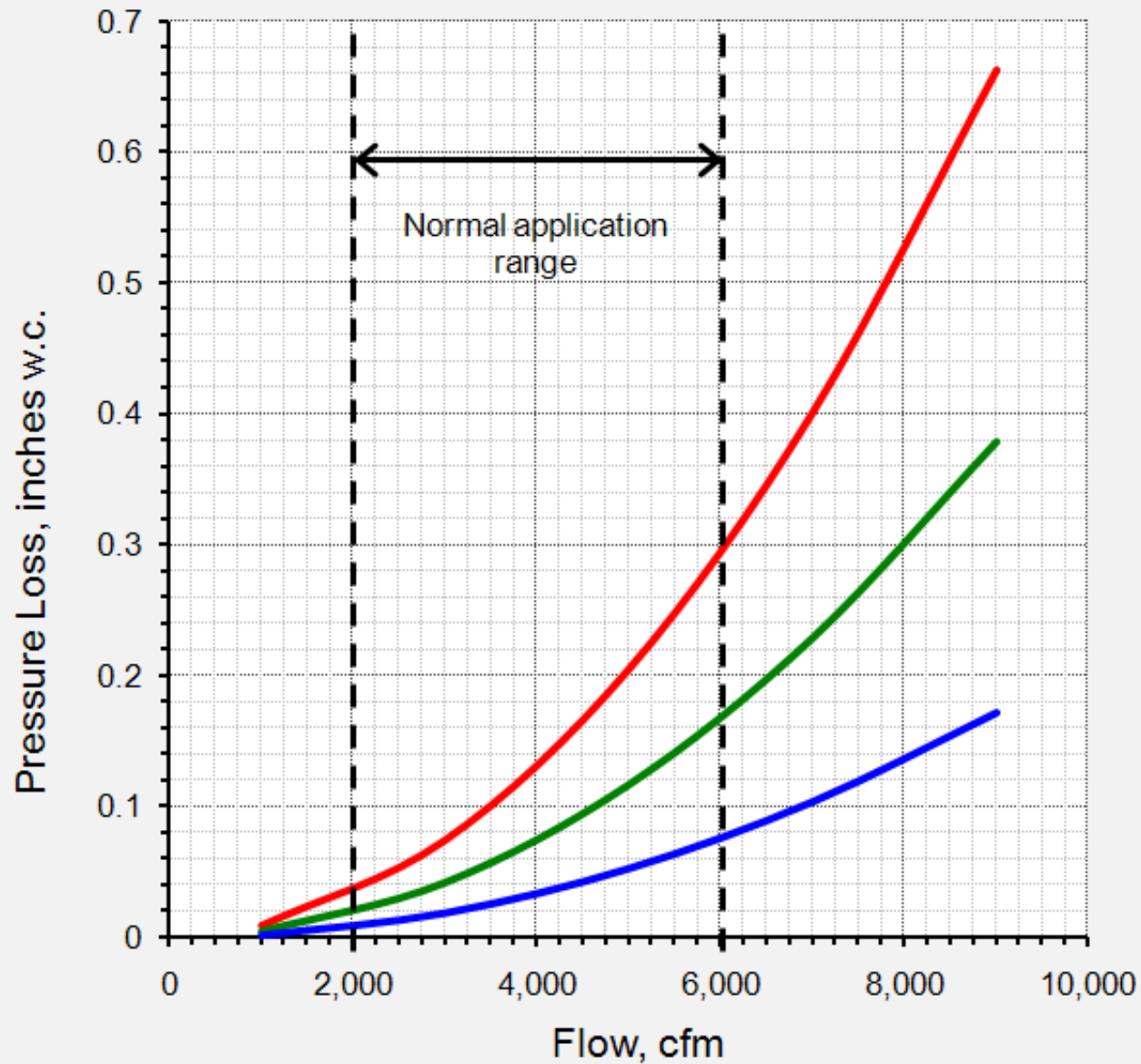
— K = system effect multiplier for turning elements in series (elbows, offsets, etc.)

Total pressure drop for the closely space fittings is calculated by adding the losses calculated for the fittings as individual elements and then multiplying them by the system effect multiplier shown in the curve.

*Data taken from AMCA test results*



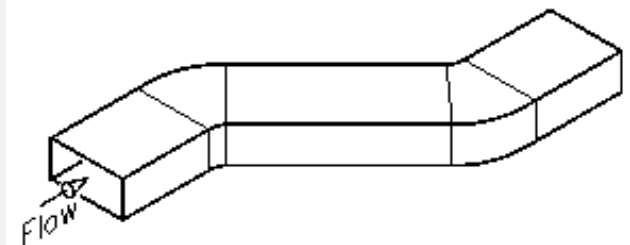
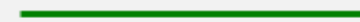
## Duct Offset Options



Offset made with 2 - 90° elbows in close proximity



Sum of the pressure drop through two individual 90°



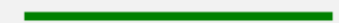
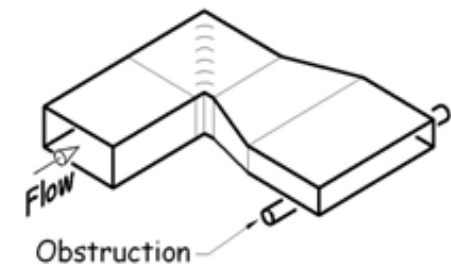
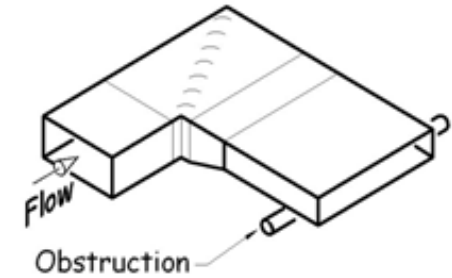
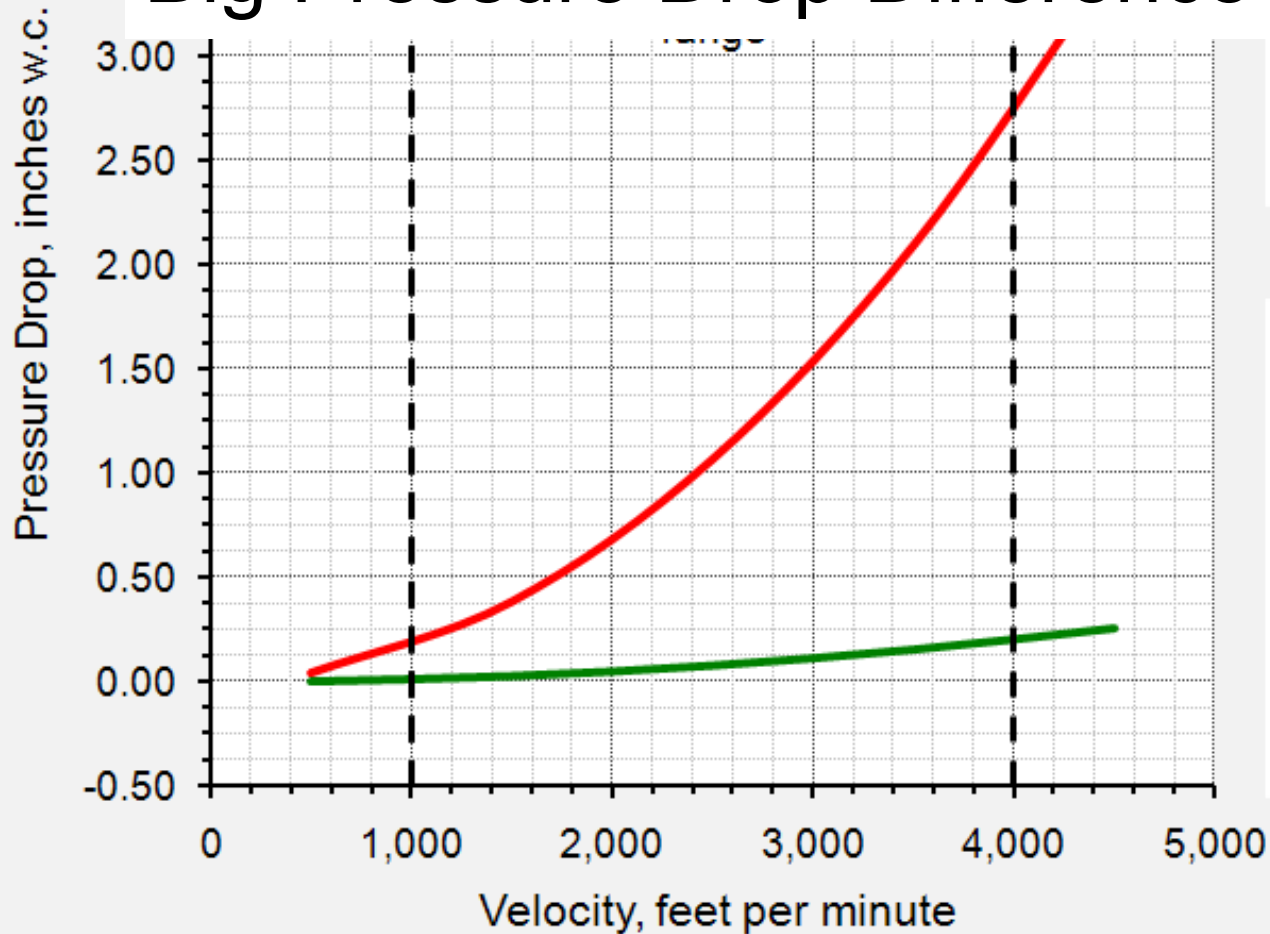
Offset made with 2 - 30° elbows separated by some duct



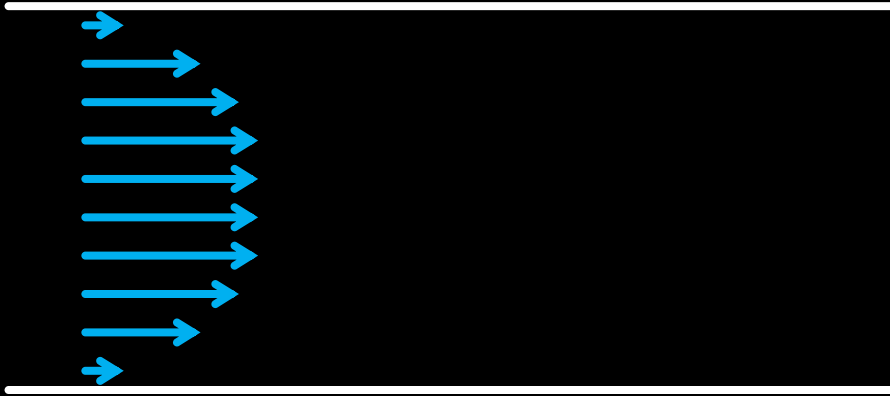


## Expanding Elbow vs. Non-expanding Elbow

4. Subtle Geometry Difference =
3. Big Pressure Drop Difference

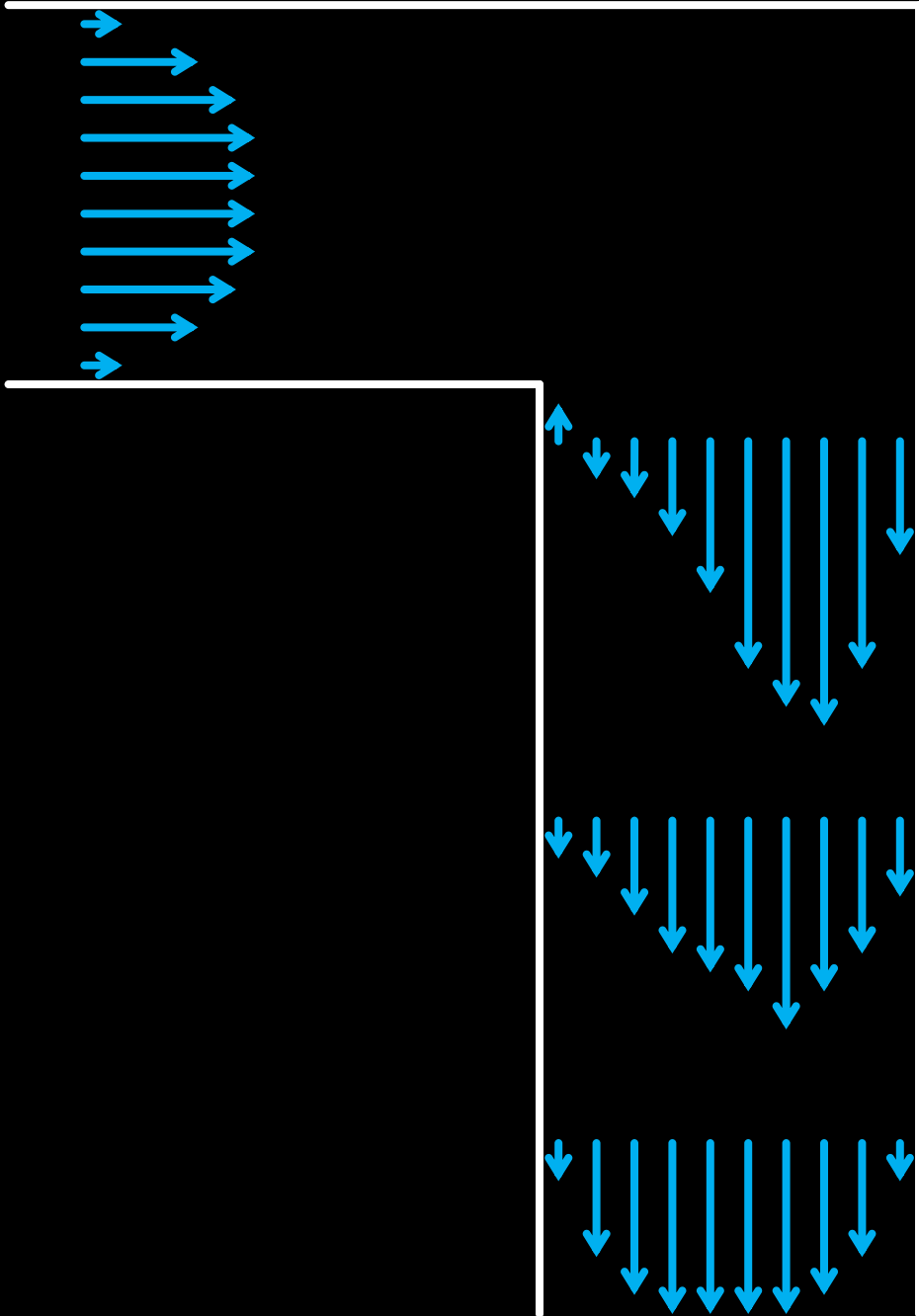






Loss coefficients rely on a uniform velocity profile for accurate measurements





Turns and other obstructions distort the flow profile

Interactions between the air and the duct wall will eventually restore the uniform flow profile

Generally takes 5-10 equivalent duct diameters of distance





# Typical Terminal Unit Inlet Duct

11/14/2002



# Using Loss Coefficients

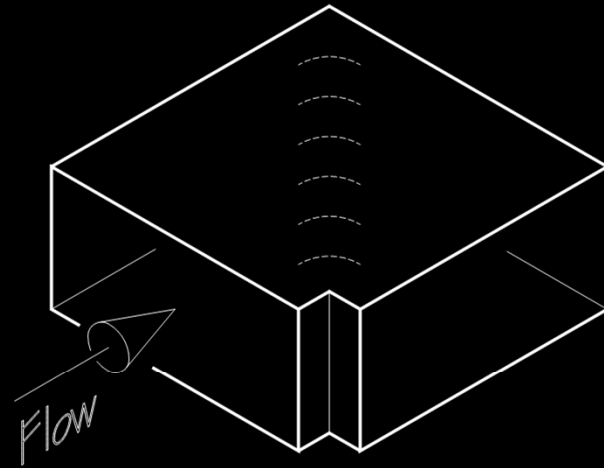
$$\Delta p_{\text{fitting}} = C_o p_{\text{velocity}}$$

Where :

$\Delta p_{\text{fitting}}$  = Fitting pressure loss

$C_o$  = Local loss coefficient from ASHRAE tables or equivalent

$p_{\text{velocity}}$  = Velocity pressure





# Velocity Pressure is VERY significant

$$V = 4,005 \sqrt{p_{velocity}}$$

Therefore :

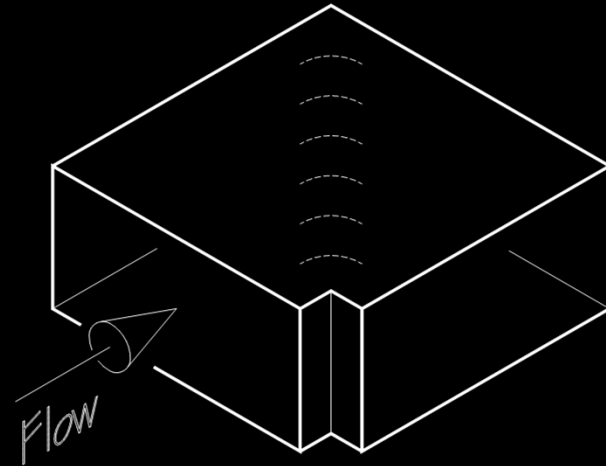
$$p_{velocity} = \left( \frac{V}{4,005} \right)^2$$

Where :

$p_{velocity}$  = Velocity pressure in inches water column

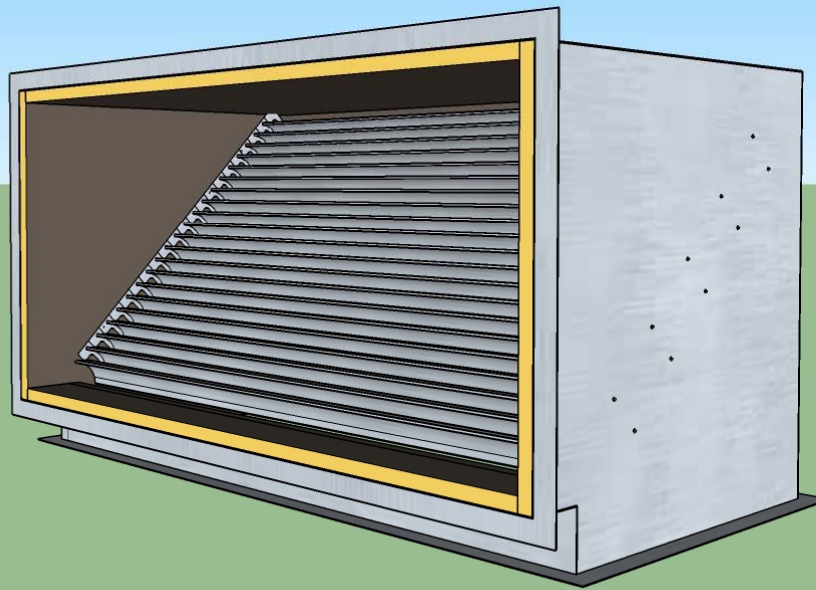
$V$  = Velocity in feet per minute

4,005 = A units conversion constant





# A Closer Look at a Mitered Elbow





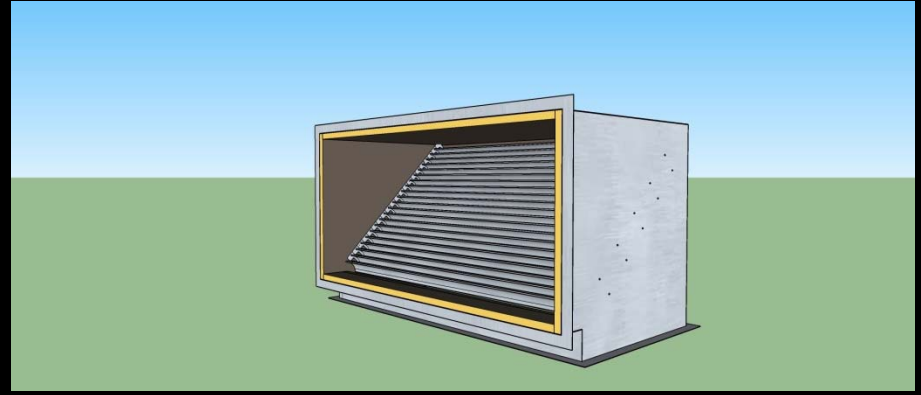
# An Exercise

Velocity Pressure Calculation

$$p_{velocity} = \left( \frac{V}{4,005} \right)^2$$

$$p_{velocity} = \left( \frac{1,500}{4,005} \right)^2$$

$$p_{velocity} = 0.14 \text{ inches w.c.}$$



What is the loss for the fitting?



# An Exercise

## Velocity Pressure Calculation

$$p_{velocity} = \left( \frac{V}{4,005} \right)^2$$

$$p_{velocity} = \left( \frac{1,500}{4,005} \right)^2$$

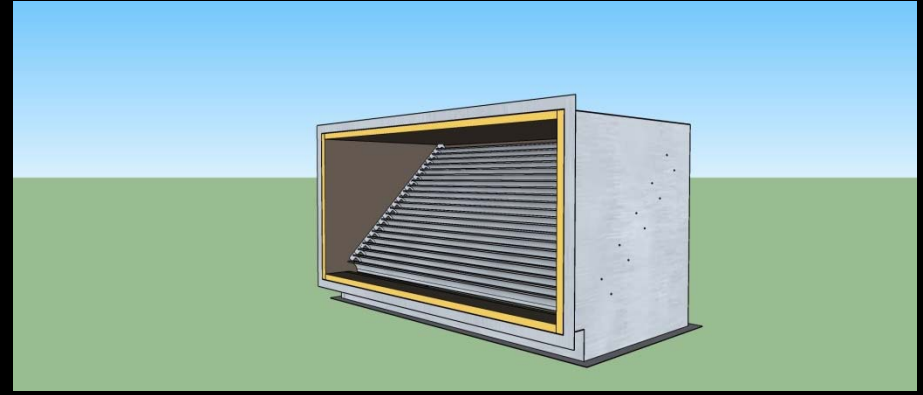
$$p_{velocity} = 0.14 \text{ inches w.c.}$$

## Fitting Loss Calculation

$$\Delta p_{fitting} = C_o \times p_{velocity}$$

$$\Delta p_{fitting} = 0.41 \times 0.14$$

$$\Delta p_{fitting} = 0.06 \text{ inches w.c.}$$



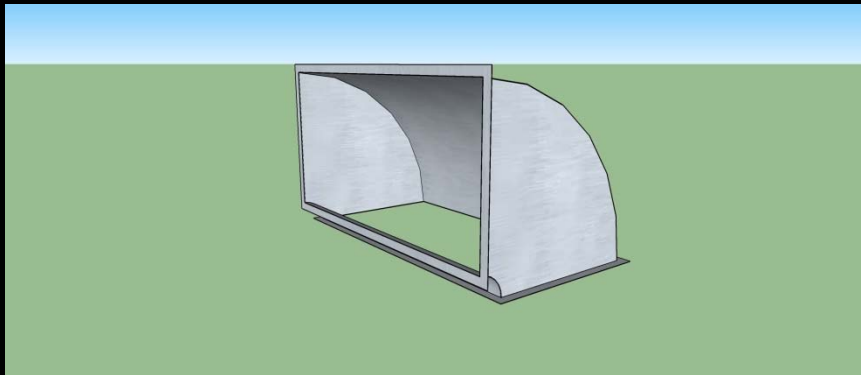
What is the loss for the fitting?



# Different Geometry = Different Loss

Losses Through A Radius 90 Degree Elbow with Different Flows, Numbers of Vanes, Turning Radiuses, and Aspect Ratios

Height (inches)	Width (inches)	Centerline Radius (inches)	Number of Vanes	Flow (cfm)	Velocity (fpm)	Velocity Pressure (inches w.c.)	Loss Coefficient	Loss	
								inches w.c.	% of base case
12	12	12	0	1,500	1,500	0.14	0.21	0.03	Base Case



## Base Case

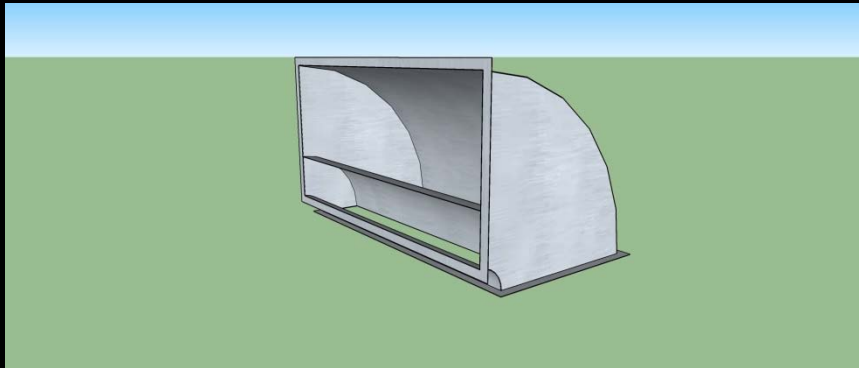
- Square duct
- Low velocity
- 12" centerline radius
- No vanes



# Different Geometry = Different Loss

Losses Through A Radius 90 Degree Elbow with Different Flows, Numbers of Vanes, Turning Radiuses, and Aspect Ratios

Height (inches)	Width (inches)	Centerline Radius (inches)	Number of Vanes	Flow (cfm)	Velocity (fpm)	Velocity Pressure (inches w.c.)	Loss Coefficient	Loss	
								inches w.c.	% of base case
12	12	12	0	1,500	1,500	0.14	0.21	0.03	Base Case
12	12	12	1	1,500	1,500	0.14	0.05	0.01	33%



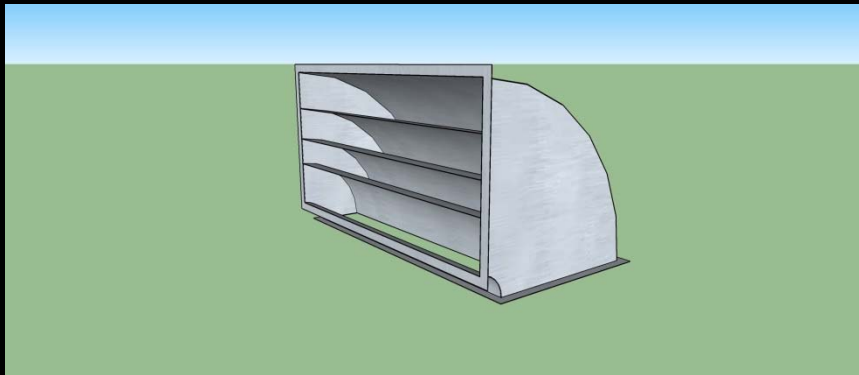
Base Case with One Vane



# Different Geometry = Different Loss

Losses Through A Radius 90 Degree Elbow with Different Flows, Numbers of Vanes, Turning Radiuses, and Aspect Ratios

Height (inches)	Width (inches)	Centerline Radius (inches)	Number of Vanes	Flow (cfm)	Velocity (fpm)	Velocity Pressure (inches w.c.)	Loss Coefficient	Loss	
								inches w.c.	% of base case
12	12	12	0	1,500	1,500	0.14	0.21	0.03	Base Case
12	12	12	1	1,500	1,500	0.14	0.05	0.01	33%
12	12	12	3	1,500	1,500	0.14	0.01	No measurable loss	



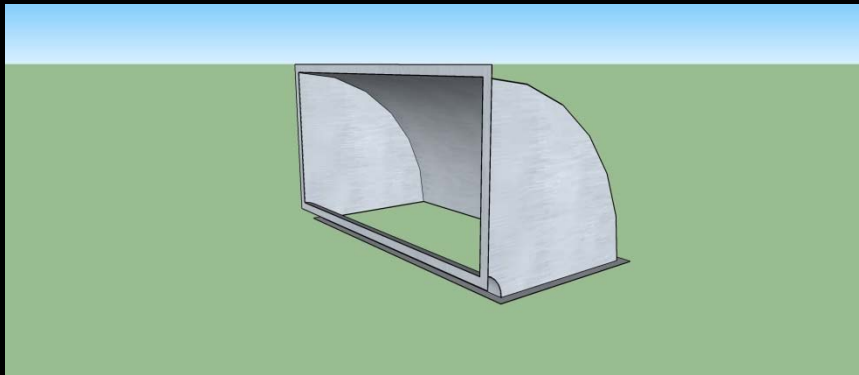
Base Case with Three Vanes



# Different Geometry = Different Loss

Losses Through A Radius 90 Degree Elbow with Different Flows, Numbers of Vanes, Turning Radiuses, and Aspect Ratios

Height (inches)	Width (inches)	Centerline Radius (inches)	Number of Vanes	Flow (cfm)	Velocity (fpm)	Velocity Pressure (inches w.c.)	Loss Coefficient	Loss	
								inches w.c.	% of base case
12	12	12	0	1,500	1,500	0.14	0.21	0.03	Base Case
12	12	12	1	1,500	1,500	0.14	0.05	0.01	33%
12	12	12	3	1,500	1,500	0.14	0.01	No measurable loss	
12	12	12	0	3,000	3,000	0.56	0.21	0.12	400%



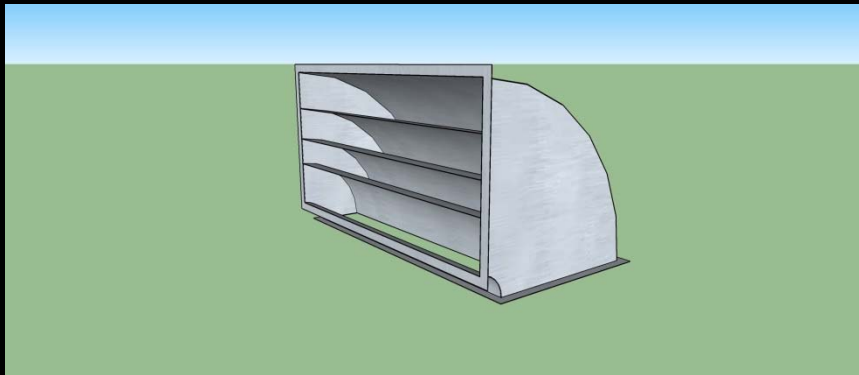
Base Case with Twice as Much  
Air Flow (Twice the Velocity)



# Different Geometry = Different Loss

Losses Through A Radius 90 Degree Elbow with Different Flows, Numbers of Vanes, Turning Radiuses, and Aspect Ratios

Height (inches)	Width (inches)	Centerline Radius (inches)	Number of Vanes	Flow (cfm)	Velocity (fpm)	Velocity Pressure (inches w.c.)	Loss Coefficient	Loss	
								inches w.c.	% of base case
12	12	12	0	1,500	1,500	0.14	0.21	0.03	Base Case
12	12	12	1	1,500	1,500	0.14	0.05	0.01	33%
12	12	12	3	1,500	1,500	0.14	0.01	No measurable loss	
12	12	12	0	3,000	3,000	0.56	0.21	0.12	400%
12	12	12	3	3,000	3,000	0.56	0.01	0.01	33%



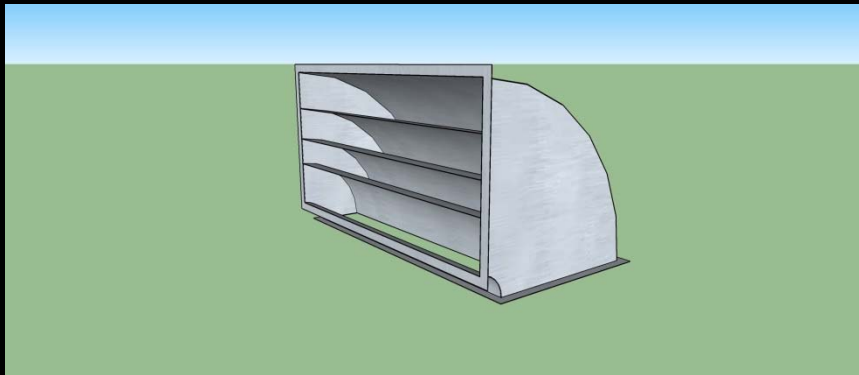
Base Case with Three Vanes  
and Twice as Much Air Flow  
(Twice the Velocity)



# Different Geometry = Different Loss

Losses Through A Radius 90 Degree Elbow with Different Flows, Numbers of Vanes, Turning Radiuses, and Aspect Ratios

Height (inches)	Width (inches)	Centerline Radius (inches)	Number of Vanes	Flow (cfm)	Velocity (fpm)	Velocity Pressure (inches w.c.)	Loss Coefficient	Loss	
								inches w.c.	% of base case
12	12	12	0	1,500	1,500	0.14	0.21	0.03	Base Case
12	12	12	1	1,500	1,500	0.14	0.05	0.01	33%
12	12	12	3	1,500	1,500	0.14	0.01	No measurable loss	
12	12	12	0	3,000	3,000	0.56	0.21	0.12	400%
12	12	12	3	3,000	3,000	0.56	0.01	0.01	33%
12	12	8	3	3,000	3,000	0.56	0.04	0.02	67%



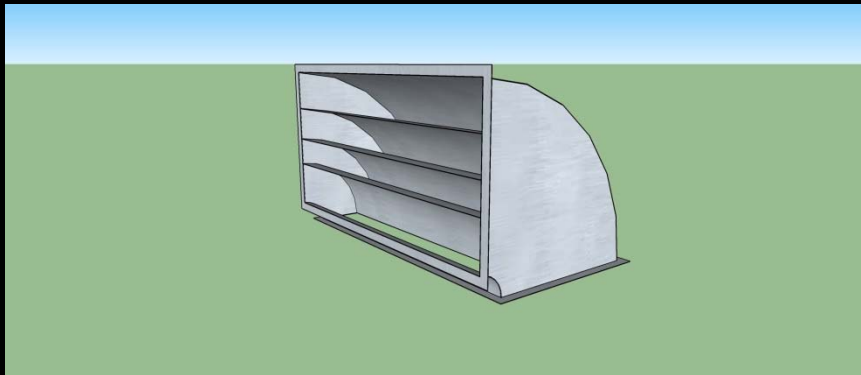
Base Case with Three Vanes  
and a Smaller Centerline  
Radius and Twice as Much Air  
Flow (Twice the Velocity)



# Different Geometry = Different Loss

Losses Through A Radius 90 Degree Elbow with Different Flows, Numbers of Vanes, Turning Radiuses, and Aspect Ratios

Height (inches)	Width (inches)	Centerline Radius (inches)	Number of Vanes	Flow (cfm)	Velocity (fpm)	Velocity Pressure (inches w.c.)	Loss Coefficient	Loss	
								inches w.c.	% of base case
12	12	12	0	1,500	1,500	0.14	0.21	0.03	Base Case
12	12	12	1	1,500	1,500	0.14	0.05	0.01	33%
12	12	12	3	1,500	1,500	0.14	0.01	No measurable loss	
12	12	12	0	3,000	3,000	0.56	0.21	0.12	400%
12	12	12	3	3,000	3,000	0.56	0.01	0.01	33%
12	12	8	3	3,000	3,000	0.56	0.04	0.02	67%
21	7	12	3	3,000	2,939	0.54	0.09	0.05	167%



Base Case with Three Vanes,  
and a High Aspect Ratio (Thin  
and Wide) and Twice as Much  
Air Flow (Twice the Velocity)



# A Tool that Makes the Analysis Easy

**ASHRAE Duct Fitting Database**

File Utilities Project Help

SR7-9

**SR7-9 Fan Outlet, Centrifugal, DW/DI, with Elbow (Position A)**  
(AMCA 1990, Fig. 8-5)

Input		Output	
Height (H, in.)	12.0	Velocity (V <sub>o</sub> , fpm)	2500
Width (W, in.)	12.0	Vel Pres at V <sub>o</sub> (P <sub>v</sub> , in. wg)	0.39
Length (L, in.)	24.0	Loss Coefficient (C <sub>o</sub> )	0.10
Blast Area Ratio (A <sub>b</sub> /A <sub>o</sub> )	0.80	Pressure Loss (in. wg)	0.04
Flow Rate (Q, cfm)	2500		

**Diagram:**

SR7-9 Fan Outlet, Centrifugal, DW/DI, with Elbow (Position A)  
(AMCA 1990, Fig. 8-5)

**DW/DI CENTRIFUGAL FAN**

$V_o > 2500 \text{ fpm: } L_e = V_o \sqrt{A_o} / 10.600$   
 $V_o \leq 2500 \text{ fpm: } L_e = \sqrt{A_o} / 4.3$   
 where  
 $V_o$  = duct velocity, fpm  
 $L_e$  = effective duct length, ft  
 $A_o$  = duct area, in<sup>2</sup>

$V_o > 13 \text{ m/s: } L_e = V_o \sqrt{A_o} / 4.500$   
 $V_o \leq 13 \text{ m/s: } L_e = \sqrt{A_o} / 350$   
 where  
 $V_o$  = duct velocity, m/s  
 $L_e$  = effective duct length, m  
 $A_o$  = duct area, mm<sup>2</sup>

01/07/2007 version: 2.02.05

Supply\Rectangular\Fan & System Interactions\Fan Outlet, Centrifugal\DW/DI, with Elbow, Position A



## A Recent Field Example







Shortridge Instruments, Inc.

1n: -2.652

AIR FLOW • VELOCITY • PRESSURE • TEMPERATURE

DUCTS

AIRDATA™ MULTIMETER ADM-870  
ELECTRONIC MICROMANOMETER  
MADE IN USA





DUCTS



Software in this meter is configured for use with the Airfoil Velocity Probe. Do not use with the VelProbe.

PEC

Shortridge Instruments, Inc.

1 in: - 2.430

• AIR FLOW • VELOCITY • PRESSURE • TEMPERATURE •

S  
I®

AIRDATA™ MULTIMETER ADM-870  
ELECTRONIC MICROMANOMETER  
MADE IN



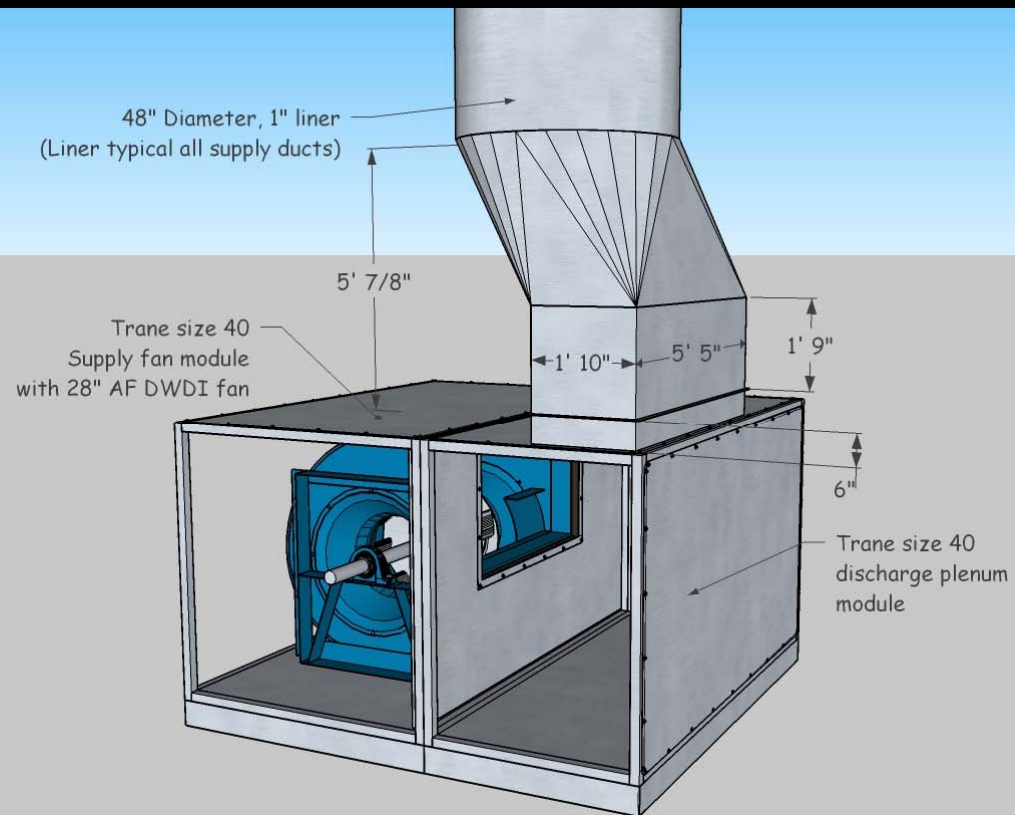
# Assessing the Operating Point



## Flow based on coil pressure drop - AHU2 Retested

Entering coil pressure at the time of my test -	0.8429 in.w.c.				
Leaving coil pressure at the time of my test -	0.7294 in.w.c.				
Coil pressure drop -	0.1135 in.w.c.				
Rated coil pressure drop at design flow -	0.384 in.w.c.				
Coil rated flow -	20,000 cfm				
Estimated flow rate based on coil pressure drop and the square law -	10,871 cfm				







# Interesting Relationships

*Looking at Different Options for Moving 10,000 cfm at a Nominal .2 in.w.c./100 ft.,  
2 inch Pressure Class Duct*

Duct Size - inches			Aspect Ratio	Cross Sectional Area - sq.ft.	Perimeter - ft.	Ratio of Cross Sectional Area to Perimeter	Gauge	Pounds of Sheetmetal per lineal foot of duct	Velocity - fpm
Height	Width	Diameter							
N/A	N/A	29.0	N/A	4.59	7.59	0.60	24	9.10	2,180
26.5	26.5	N/A	1.0	4.88	8.83	0.55	26	8.00	2,051
18.0	41.0	N/A	2.3	5.13	9.83	0.52	24	11.37	1,951
14.0	56.0	N/A	4.0	5.44	11.67	0.47	24	13.49	1,837
12.0	70.0	N/A	5.8	5.83	13.67	0.43	24	15.80	1,714

Round duct weight information based on spiral construction.



# Interesting Relationships

*Looking at Different Options for Moving 10,000 cfm at a Nominal .2 in.w.c./100 ft.,*

2 Higher velocities for ducts with less sheet metal implies higher operating cost all things being equal and more susceptibility problems due to poor fitting design

Duct Size - inches			Aspect Ratio				Perimeter	Pounds of Sheet metal per foot of duct	Velocity - fpm
Height	Width	Diameter							
N/A	N/A	29.0	N/A	4.59	7.59	0.60	24	9.10	2,180
26.5	26.5	N/A					24	8.00	2,051
18.0	41.0	N/A					24	11.37	1,951
14.0	56.0	N/A					24	13.42	1,837
12.0	70.0	N/A					24	15.80	1,714

Round duct weight information

Less sheet metal for a round or low aspect ratio duct implies a more sustainable solution (fewer resources used) assuming building height is not affected



# Interesting Relationships

## *Velocities and Velocity Pressures in Small vs. Large Ducts at Equal Friction Rates*

Duct Size - inches			Aspect Ratio	Cross Sectional Area - sq.ft.	Perimeter - ft.	Ratio of Cross Sectional Area to Perimeter	CFM Capacity at a Friction Rate of .15 in.w.c. per 100 ft.	Velocity - fpm	Velocity Pressure - in.w.c.
Height	Width	Diameter							
N/A	N/A	6.0	N/A	0.20	1.57	0.13	130	662	0.03
N/A	N/A	48.0	N/A	12.57	12.57	1.00	32,000	2,546	0.40
6.0	12.0	N/A	2.0	0.50	3.00	0.17	420	840	0.04
24.0	48.0	N/A	2.0	8.00	12.00	0.67	16,500	2,063	0.27



# Interesting Relationships

*Velocities and Velocity Pressures in Small vs. Large Ducts at Equal Friction Rates*

Duct Size - inches	Aspect Ratio	Cross Sectional Area - sq. ft.	Perimeter - ft.	Ratio of Cross Sectional Area to Perimeter	CFM Capacity at a Friction Rate of .15 in.w.c. per 100 ft.	Velocity - fpm	Velocity Pressure - in.w.c.
Height							
N/A	N/A	6.0	N/A	0.20	130	662	0.03
N/A	N/A	18.0	N/A	1.00	32,000	2,546	0.40
6.0					420	440	0.04
24.0				0.67	6,500	663	0.27

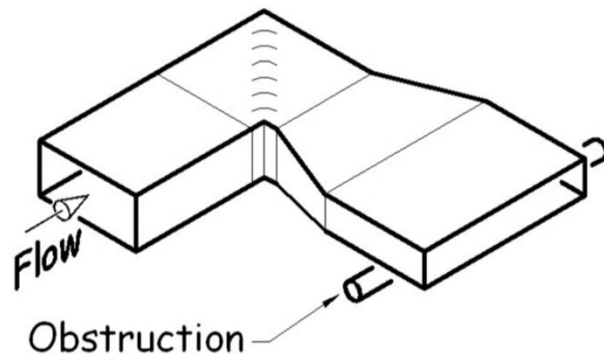
Small ducts don't handle much air relative to large ducts at the same friction rate because a relatively small volume of air is contained by a relatively large sheet metal perimeter.

Thus, small duct velocities and velocity pressures are low relative to large ducts and poor fittings are not as much of an issue.

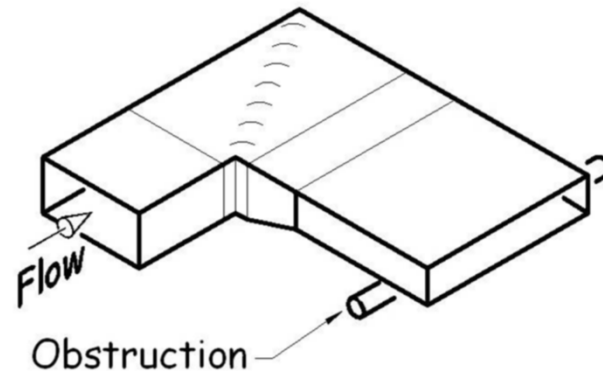


# I Specify Construction to SMACNA Standards so I'll Get Low Loss Fittings

Maybe ...



... or Maybe Not



*SMACNA is a design and construction standard, not an efficiency standard*



# For Any Given SMACNA Duct or Fitting:

3 in. w.c. Positive or Negative Duct Construction (SMACNA HVAC Duct Construction Standards Metal and Flexible, 3rd Edition)

Duct Dimension - in.	No.				Reinforcement Spacing Options - feet				
					5	4	3	2.5	2
11-13					B-26	B-26	B-26	B-26	B-26
13-15					C-24	C-26	C-26	B-26	B-26
15-17					C-26	C-26	C-26	C-26	
17-19			D-24	D-24	C-24	C-26	C-26	C-26	C-26
19-20	18		D-22	D-22	D-24	D-24	C-26	C-26	C-26
21-22	18		E-22	E-22	D-24	D-24	D-26	C-26	C-26
23-24	18		E-20	E-22	E-24	E-24	D-26	D-26	C-26
25-26	18		F-20	E-22	E-24	E-24	D-26	D-26	C-26
27-28	18		F-20	F-20	F-22	E-24	E-26	D-26	D-26
29-30	18		G-20	F-20	F-22	E-24	E-26	E-26	D-26
31-36	16	H-18G	H-18G	H-18G	G-20	F-22	F-24	E-26	E-26
37-42			I-16G	H-18G	H-20G	G-22	F-24	F-24	E-26
43-48			J-16H	I-18G	I-18G	H-20	G-22	G-24	F-24
49-54				J-16H	I-18G	I-18G	H-22G	G-24	G-24
55-60				J-16H	I-18G	I-18G	H-20G	H-22G	G-24
61-72					J-16I	J-18H	I-20G	I-22G	I-24G
73-84					L-16I	K-16H	J-18H	I-20H	I-22G
85-96						L-16I	K-18I	J-18I	I-20H
97-108							L-16I	L-18I	K-18I
109-120							L-16I	L-18I	K-18I

There are multiple combinations of metal thickness (gauge) and reinforcement

Not Designed

Note 1 The number in the table cell is the minimum gauge.

Note 2 The letter in the box to the left of the gauge is the minimum reinforcement grade for joints and intermediate stiffeners occurring at a maximum spacing interval in the column heading.

Note 3 A letter to the right of the gauge gives a tie-rodged reinforcement alternative.

Note 4 A "t" compels the use of tie rods for the reinforcement listing.

Note 5 Beading and cross bracing may also be required



# Internal Reinforcement







# External Reinforcement and a Flow Division Fitting

11/14/2002





Inside the Fitting

11/14/2002





## Spiral Duct and a “Boot” Type Duct Tap



# Inside Spiral Duct



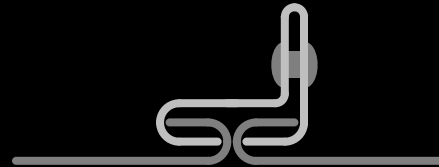
# For Any Given SMACNA Duct or Fitting:

There are multiple combinations of metal thickness (gauge) and reinforcement

There are multiple joint and seam specifications



Drive slip



Standing  
drive slip



Hemmed  
S slip



Flange with  
gasket; bolted or  
riveted

SMACNA shows about 27 transverse joint options and about 7 longitudinal joint options



# For Any Given SMACNA Duct or Fitting:

There are multiple combinations of metal thickness (gauge) and reinforcement

There are multiple joint and seam specifications

There are multiple geometries; SMACNA details:

- 15 different elbow designs
- 21 different branch connections
- 9 different ways to offset around an obstruction

ASHRAE documents 11 different turning vane designs



*Three different ways to split of flow;  
three different pressure drops; three  
different costs to fabricate*



# Typical Turning Vanes

Double Thickness Turning Vanes Slip Over Tabs on the Mounting Rail



Mounting Rail  
Screwed to Duct wall





# Leakage; Another SMACNA Standard

Multiple leakage classes in terms of cfm per hundred square feet of duct area for a given test pressure

General procedure:

- Calculate anticipated leakage
- Select test section based on test machine capacity
- Temporarily seal open ends of duct
- Gradually pressurize duct
- Read leakage from flow meter



DUCTS





Duct Sealant







Duct Sealant as a Clue to a Different Problem



# Flex Duct

Accommodates field tolerances  
for final alignment of exposed  
devices

Provides some vibration isolation

Proper installation is critical

- Use minimum lengths
- Support is critical
  - Frequency
  - Methodology
- Bend radius is critical

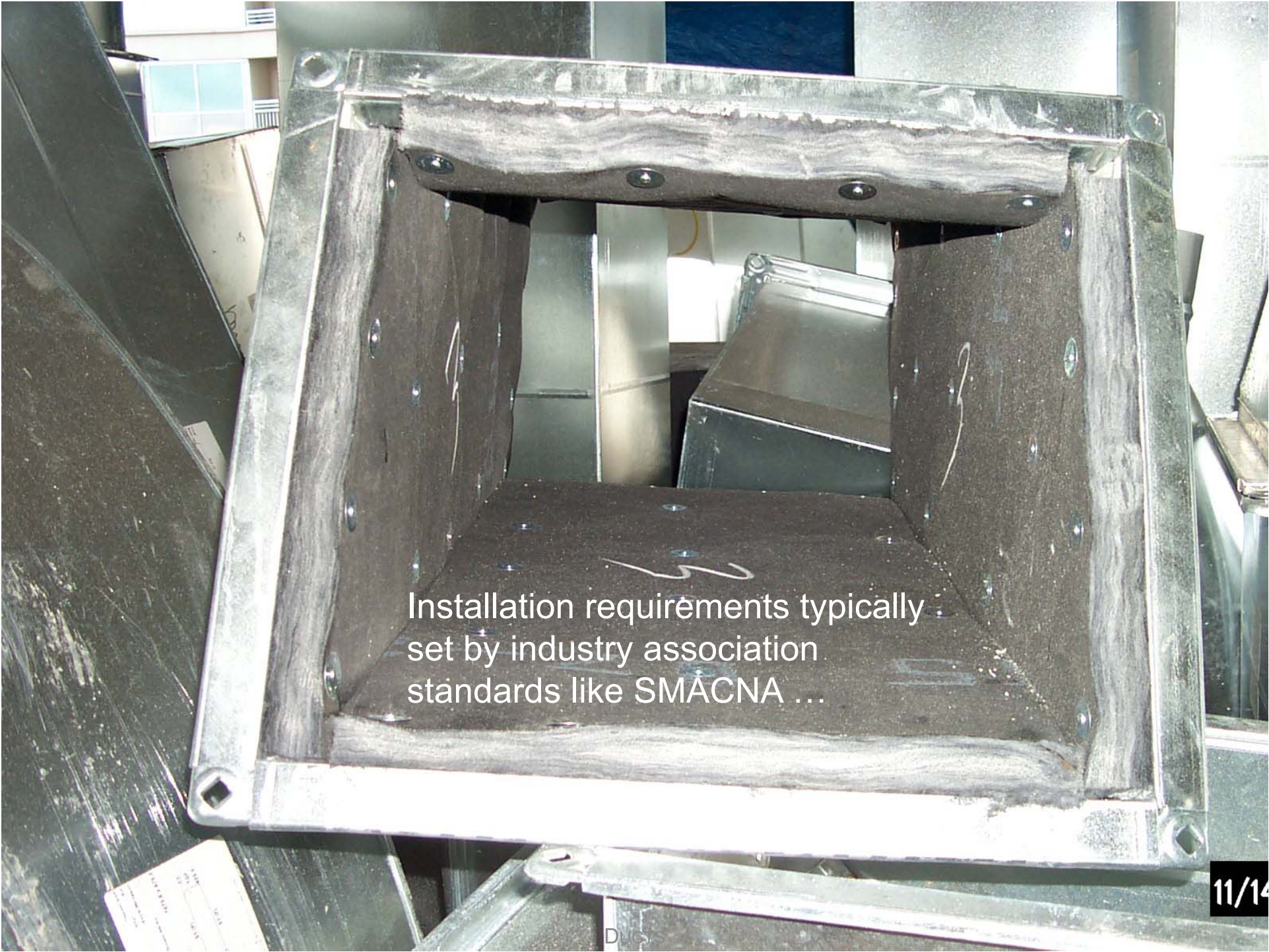


# Insulation and Duct Liner

Thickness typically set  
by energy and efficiency  
codes and standards ...


DUCTS





Installation requirements typically  
set by industry association  
standards like SMACNA ...





Protection during construction  
usually covered by LEED® or other  
project contractual requirements

DUCTS





Protection during construction  
usually covered by LEED® or other  
project contractual requirements ... or not



# Flex Duct Resources

JPLFlex website ([www.jplflex.com](http://www.jplflex.com))

- Installation guide lines
- Friction loss calculator

*Predicting the Performance of Flexible Duct Systems*

- William Allen
- December 2010 Heating, Piping and Air Conditioning Magazine, page 28
- [www.HPAC.com](http://www.HPAC.com)



# Fans, Ductwork, & Air Handling Components:

Design, Performance, & Commissioning Issues

**Supplement - Loss Coefficient Exercise**



Instructor:

David Sellers

Senior Engineer

Facility Dynamics Engineering

November 10, 2015



# Loss Coefficient Exercise

## Given

**The ASHRAE loss coefficient table that follows**

**A 12" x 12" duct dimension**

**A 12" centerline radius**

**A flow rate of 1,500 cfm**

## Determine

- The loss through an elbow with no vanes
- The loss through the elbow with 1 vane
- The loss through the elbow with no vanes if the flow rate is 3,000 cfm

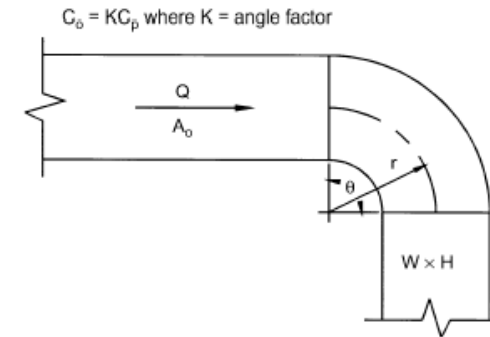


### CR3-1 Elbow, Smooth Radius, Without Vanes

$C_p$ Values											
$r/W$	$H/W$										
	0.25	0.50	0.75	1.00	1.50	2.00	3.00	4.00	5.00	6.00	8.00
0.50	1.53	1.38	1.29	1.18	1.06	1.00	1.00	1.06	1.12	1.16	1.18
0.75	0.57	0.52	0.48	0.44	0.40	0.39	0.39	0.40	0.42	0.43	0.44
1.00	0.27	0.25	0.23	0.21	0.19	0.18	0.18	0.19	0.20	0.21	0.21
1.50	0.22	0.20	0.19	0.17	0.15	0.14	0.14	0.15	0.16	0.17	0.17
2.00	0.20	0.18	0.16	0.15	0.14	0.13	0.13	0.14	0.14	0.15	0.15

Angle Factor $K$											
$\theta$	0	20	30	45	60	75	90	110	130	150	180
$K$	0.00	0.31	0.45	0.60	0.78	0.90	1.00	1.13	1.20	1.28	1.40



### CR3-3 Elbow, Smooth Radius, One Splitter Vane

$C_p$ Values											
$r/W$	$H/W$										
	0.25	0.50	1.00	1.50	2.00	3.00	4.00	5.00	6.00	7.00	8.00
0.55	0.52	0.40	0.43	0.49	0.55	0.66	0.75	0.84	0.93	1.01	1.09
0.60	0.36	0.27	0.25	0.28	0.30	0.35	0.39	0.42	0.46	0.49	0.52
0.65	0.28	0.21	0.18	0.19	0.20	0.22	0.25	0.26	0.28	0.30	0.32
0.70	0.22	0.16	0.14	0.14	0.15	0.16	0.17	0.18	0.19	0.20	0.21
0.75	0.18	0.13	0.11	0.11	0.11	0.12	0.13	0.14	0.14	0.15	0.15
0.80	0.15	0.11	0.09	0.09	0.09	0.09	0.10	0.10	0.11	0.11	0.12
0.85	0.13	0.09	0.08	0.07	0.07	0.08	0.08	0.08	0.08	0.09	0.09
0.90	0.11	0.08	0.07	0.06	0.06	0.06	0.06	0.07	0.07	0.07	0.07
0.95	0.10	0.07	0.06	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06
1.00	0.09	0.06	0.05	0.05	0.04	0.04	0.04	0.05	0.05	0.05	0.05

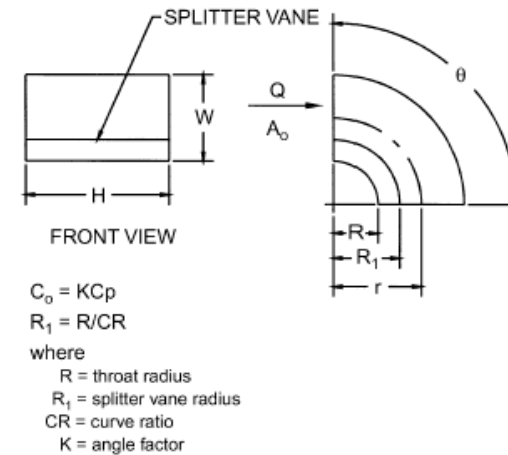
Angle Factor $K$					
$\theta$	0	30	45	60	90
$K$	0.00	0.45	0.60	0.78	1.00

Curve Ratio CR										
$r/W$	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
CR	0.218	0.302	0.361	0.408	0.447	0.480	0.509	0.535	0.557	0.577

Throat Radius/Width Ratio ( $R/W$ )										
$r/W$	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
$R/W$	0.05	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50





# Calculating Velocity Pressure

$$V = 4,005 \sqrt{p_{velocity}}$$

Therefore :

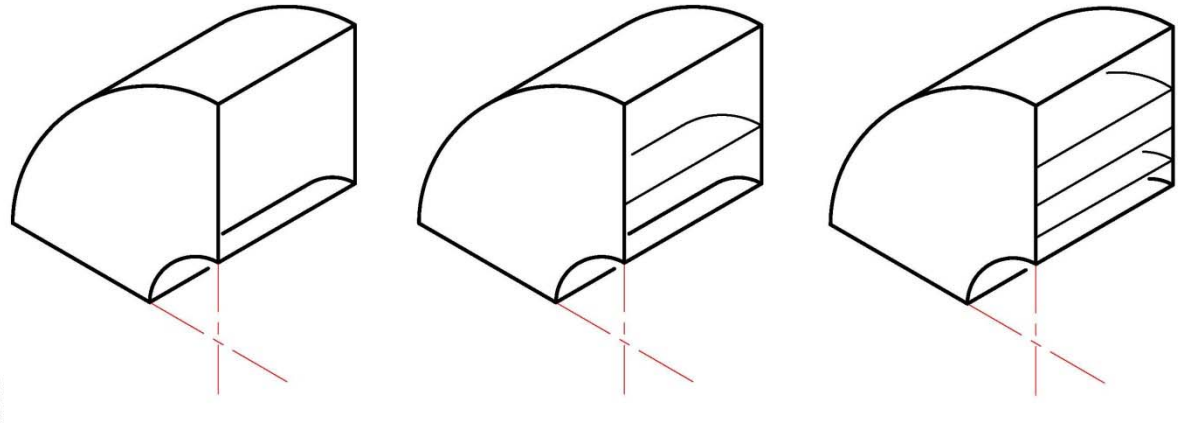
$$p_{velocity} = \left( \frac{V}{4,005} \right)^2$$

Where :

$p_{velocity}$  = Velocity pressure in inches water column

$V$  = Velocity in feet per minute

4,005 = A units conversion constant





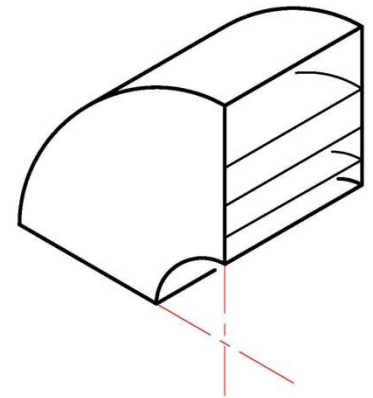
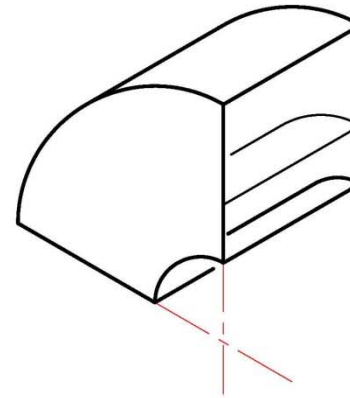
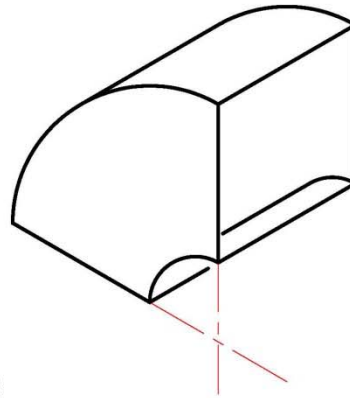
# Calculating Velocity Pressure

$$V = 4,005 \sqrt{p_{velocity}}$$

Therefore :

$$p_{velocity} = \left( \frac{1,500}{4,005} \right)^2$$

$$p_{velocity} = 0.14 \text{ in.w.c.}$$





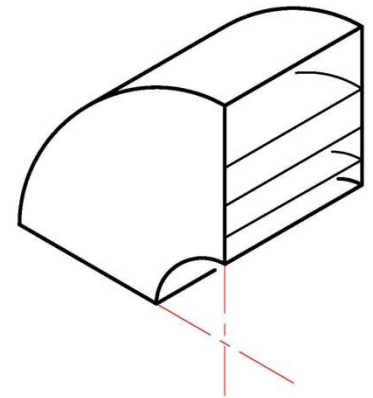
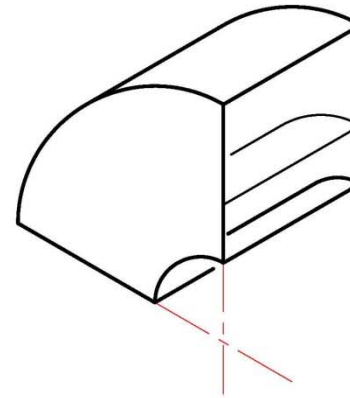
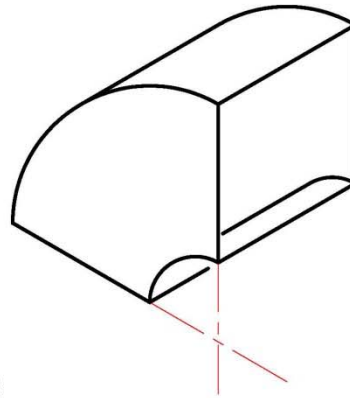
# Calculating Velocity Pressure

$$V = 4,005 \sqrt{p_{velocity}}$$

Therefore :

$$p_{velocity} = \left( \frac{3,000}{4,005} \right)^2$$

$$p_{velocity} = 0.56 \text{ in.w.c.}$$





# Selecting and Applying the Loss Coefficient

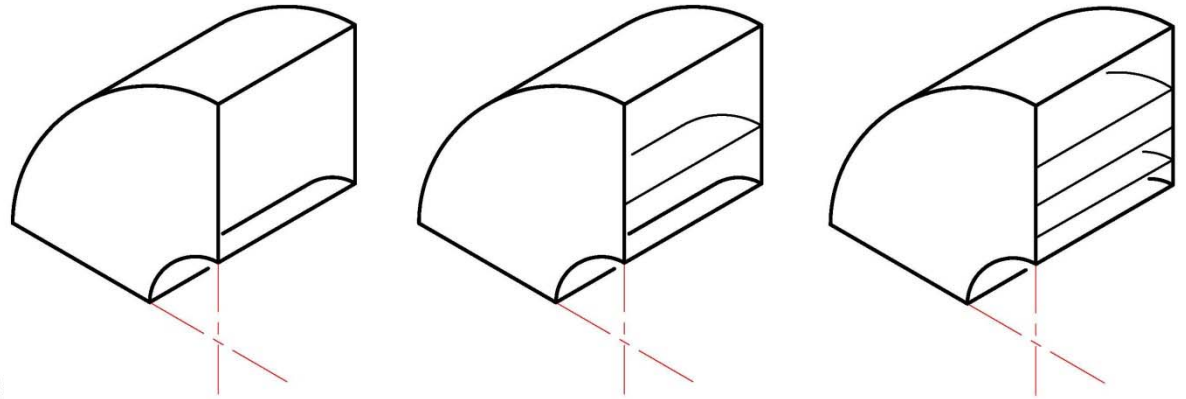
$$\Delta p_{\text{fitting}} = C_o p_{\text{velocity}}$$

Where :

$\Delta p_{\text{fitting}}$  = Fitting pressure loss

$C_o$  = Local loss coefficient from ASHRAE tables or equivalent

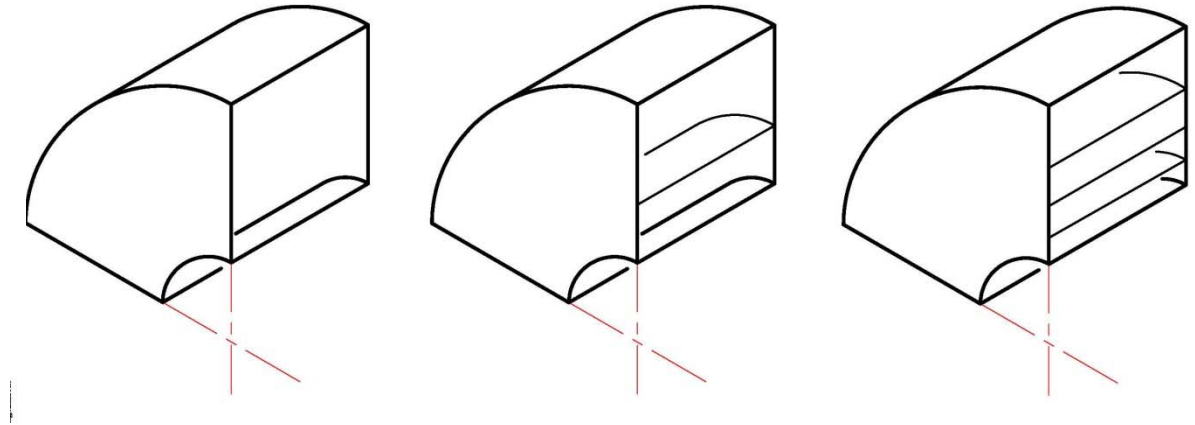
$p_{\text{velocity}}$  = Velocity pressure





# Selecting and Applying the Loss Coefficient

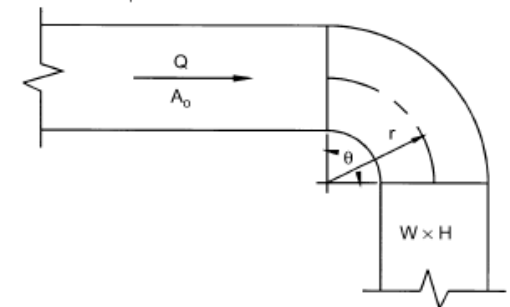
$$\Delta p_{fitting} = C_o p_{velocity}$$



CR3-1 Elbow, Smooth Radius, Without Vanes

$C_p$ Values												
$r/W$	0.25	0.50	0.75	1.00	$H/W$							
	0.25	0.50	0.75	1.00	1.50	2.00	3.00	4.00	5.00	6.00	8.00	
0.50	1.53	1.38	1.29	1.18	1.06	1.00	1.00	1.06	1.12	1.16	1.18	
0.75	0.57	0.52	0.48	0.44	0.40	0.39	0.39	0.40	0.42	0.43	0.44	
1.00	0.27	0.25	0.23	0.21	0.19	0.18	0.18	0.19	0.20	0.21	0.21	
1.50	0.22	0.20	0.19	0.17	0.15	0.14	0.14	0.15	0.16	0.17	0.17	
2.00	0.20	0.18	0.16	0.15	0.14	0.13	0.13	0.14	0.14	0.15	0.15	
Angle Factor $K$												
$\theta$	0	20	30	45	60	75	90	110	130	150	180	
$K$	0.00	0.31	0.45	0.60	0.78	0.90	1.00	1.13	1.20	1.28	1.40	

$C_o = KC_p$  where  $K$  = angle factor



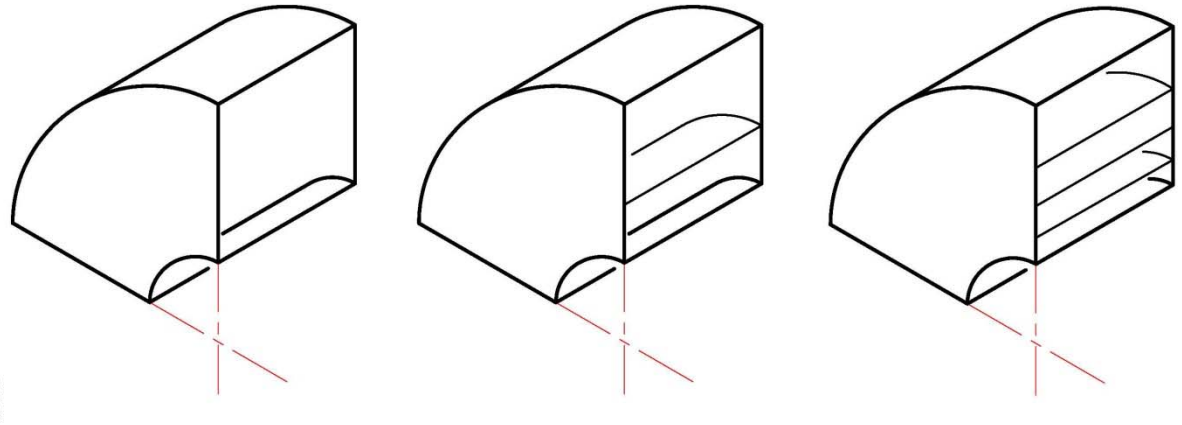


# Selecting and Applying the Loss Coefficient

$$\Delta p_{fitting} = C_o p_{velocity}$$

$$\Delta p_{fitting} = .21 \times .14$$

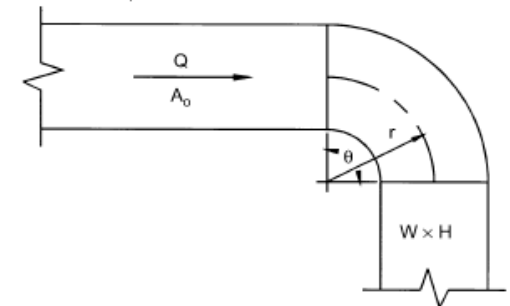
$$\Delta p_{fitting} = .03 \text{ in.w.c.}$$



CR3-1 Elbow, Smooth Radius, Without Vanes

$C_p$ Values												
$r/W$	0.25	0.50	0.75	1.00	1.50	2.00	3.00	4.00	5.00	6.00	8.00	
0.50	1.53	1.38	1.29	1.18	1.06	1.00	1.00	1.06	1.12	1.16	1.18	
0.75	0.57	0.52	0.48	0.44	0.40	0.39	0.39	0.40	0.42	0.43	0.44	
1.00	0.27	0.25	0.23	0.21	0.19	0.18	0.18	0.19	0.20	0.21	0.21	
1.50	0.22	0.20	0.19	0.17	0.15	0.14	0.14	0.15	0.16	0.17	0.17	
2.00	0.20	0.18	0.16	0.15	0.14	0.13	0.13	0.14	0.14	0.15	0.15	
Angle Factor $K$												
$\theta$	0	20	30	45	60	75	90	110	130	150	180	
$K$	0.00	0.31	0.45	0.60	0.78	0.90	1.00	1.13	1.20	1.28	1.40	

$C_o = KC_p$  where  $K$  = angle factor

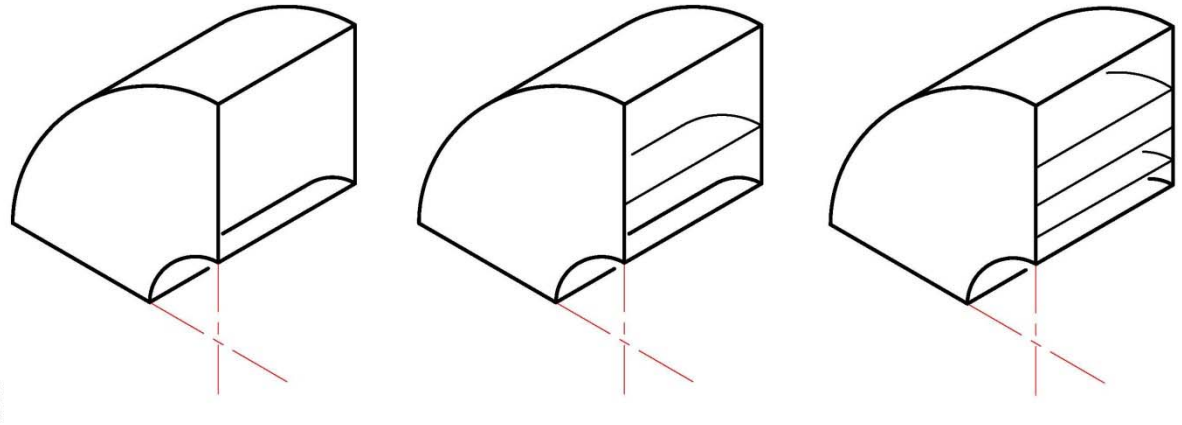




# Selecting and Applying the Loss Coefficient

$$\Delta p_{fitting} = C_o p_{velocity}$$

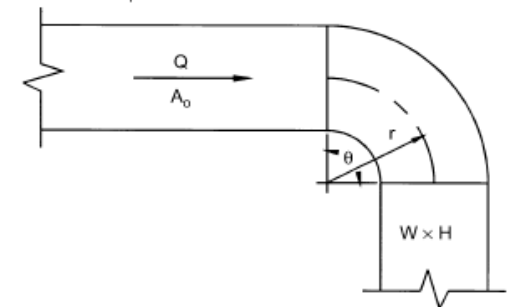
$$\Delta p_{fitting} = .21 \times .56$$



CR3-1 Elbow, Smooth Radius, Without Vanes

$C_p$ Values												
$r/W$	0.25	0.50	0.75	1.00	1.50	2.00	3.00	4.00	5.00	6.00	8.00	
0.50	1.53	1.38	1.29	1.18	1.06	1.00	1.00	1.06	1.12	1.16	1.18	
0.75	0.57	0.52	0.48	0.44	0.40	0.39	0.39	0.40	0.42	0.43	0.44	
1.00	0.27	0.25	0.23	0.21	0.19	0.18	0.18	0.19	0.20	0.21	0.21	
1.50	0.22	0.20	0.19	0.17	0.15	0.14	0.14	0.15	0.16	0.17	0.17	
2.00	0.20	0.18	0.16	0.15	0.14	0.13	0.13	0.14	0.14	0.15	0.15	
Angle Factor $K$												
$\theta$	0	20	30	45	60	75	90	110	130	150	180	
$K$	0.00	0.31	0.45	0.60	0.78	0.90	1.00	1.13	1.20	1.28	1.40	

$C_o = KC_p$  where  $K$  = angle factor



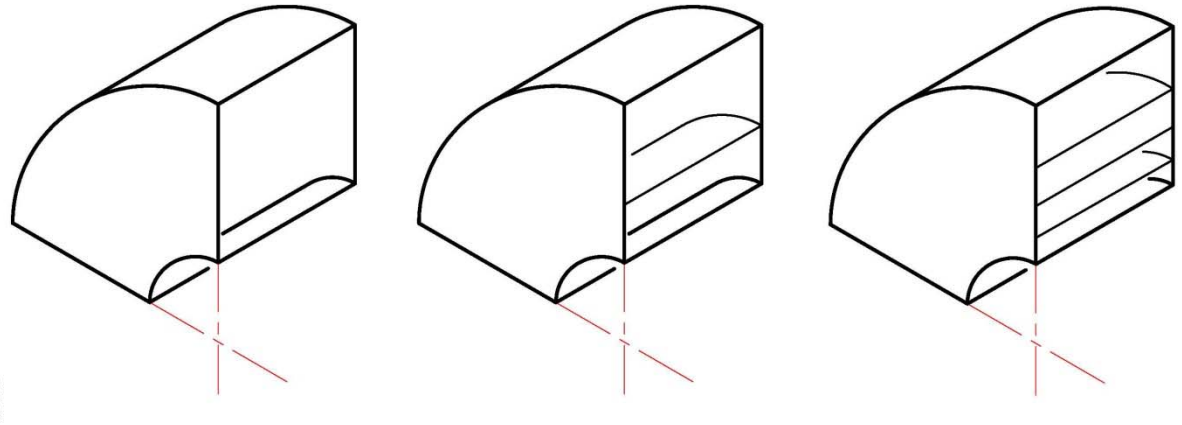


# Selecting and Applying the Loss Coefficient

$$\Delta p_{fitting} = C_o p_{velocity}$$

$$\Delta p_{fitting} = .21 \times .56$$

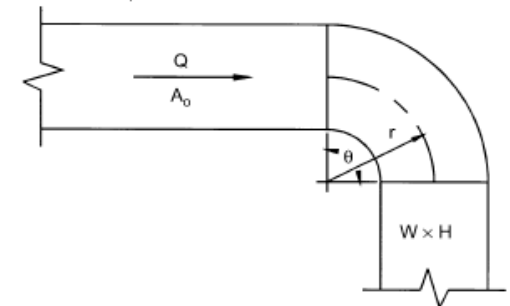
$$\Delta p_{fitting} = .12 \text{ in.w.c.}$$



CR3-1 Elbow, Smooth Radius, Without Vanes

$C_p$ Values												
$r/W$	0.25	0.50	0.75	1.00	1.50	2.00	3.00	4.00	5.00	6.00	8.00	
0.50	1.53	1.38	1.29	1.18	1.06	1.00	1.00	1.06	1.12	1.16	1.18	
0.75	0.57	0.52	0.48	0.44	0.40	0.39	0.39	0.40	0.42	0.43	0.44	
1.00	0.27	0.25	0.23	0.21	0.19	0.18	0.18	0.19	0.20	0.21	0.21	
1.50	0.22	0.20	0.19	0.17	0.15	0.14	0.14	0.15	0.16	0.17	0.17	
2.00	0.20	0.18	0.16	0.15	0.14	0.13	0.13	0.14	0.14	0.15	0.15	
Angle Factor $K$												
$\theta$	0	20	30	45	60	75	90	110	130	150	180	
$K$	0.00	0.31	0.45	0.60	0.78	0.90	1.00	1.13	1.20	1.28	1.40	

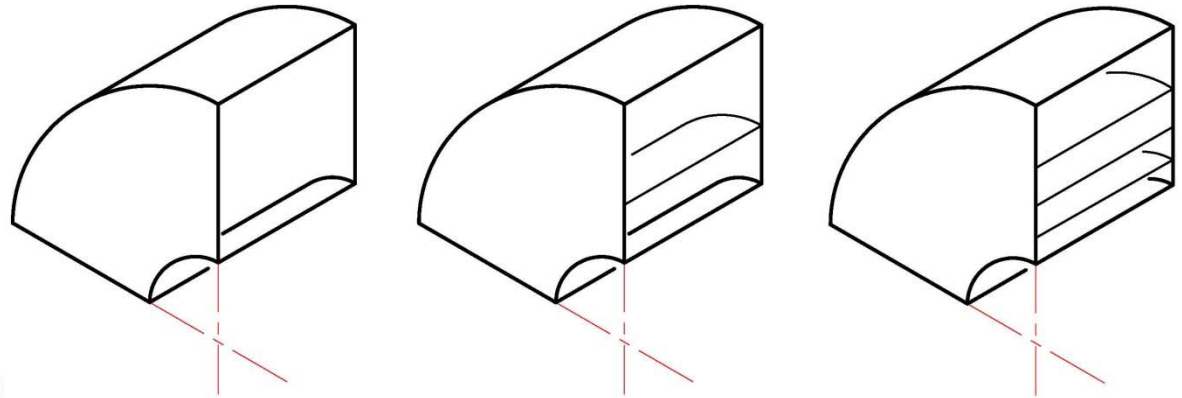
$C_o = KC_p$  where  $K$  = angle factor





# Selecting and Applying the Loss Coefficient

$$\Delta p_{\text{fitting}} = C_o p_{\text{velocity}}$$

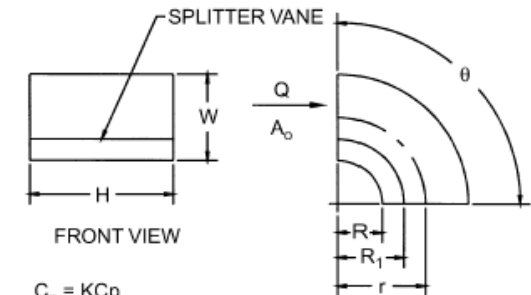


CR3-3 Elbow, Smooth Radius, One Splitter Vane

$C_p$ Values											
		H/W									
$r/W$	0.25	0.50	1.00	1.50	2.00	3.00	4.00	5.00	6.00	7.00	8.00
0.55	0.52	0.40	0.43	0.49	0.55	0.66	0.75	0.84	0.93	1.01	1.09
0.60	0.36	0.27	0.25	0.28	0.30	0.35	0.39	0.42	0.46	0.49	0.52
0.65	0.28	0.21	0.18	0.19	0.20	0.22	0.25	0.26	0.28	0.30	0.32
0.70	0.22	0.16	0.14	0.14	0.15	0.16	0.17	0.18	0.19	0.20	0.21
0.75	0.18	0.13	0.11	0.11	0.11	0.12	0.13	0.14	0.14	0.15	0.15
0.80	0.15	0.11	0.09	0.09	0.09	0.09	0.10	0.10	0.11	0.11	0.12
0.85	0.13	0.09	0.08	0.07	0.07	0.08	0.08	0.08	0.08	0.09	0.09
0.90	0.11	0.08	0.07	0.06	0.06	0.06	0.06	0.07	0.07	0.07	0.07
0.95	0.10	0.07	0.06	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06
1.00	0.09	0.06	0.05	0.05	0.04	0.04	0.04	0.05	0.05	0.05	0.05

Angle Factor $K$					
$\theta$	0	30	45	60	90
$K$	0.00	0.45	0.60	0.78	1.00



$C_o = KC_p$

$R_1 = R/CR$

where

$R$  = throat radius

$R_1$  = splitter vane radius

$CR$  = curve ratio

$K$  = angle factor

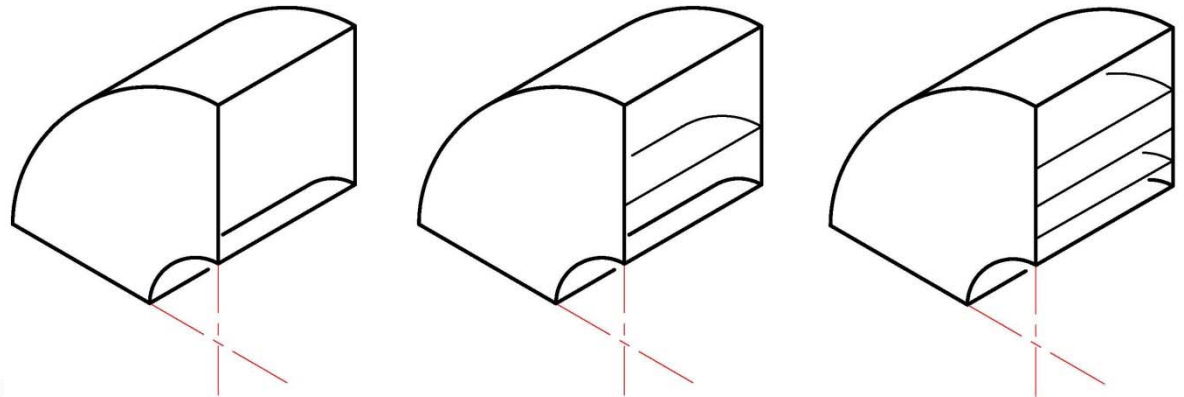


# Selecting and Applying the Loss Coefficient

$$\Delta p_{fitting} = C_o p_{velocity}$$

$$\Delta p_{fitting} = .05 \times .14$$

$$\Delta p_{fitting} = .01 \text{ in.w.c.}$$

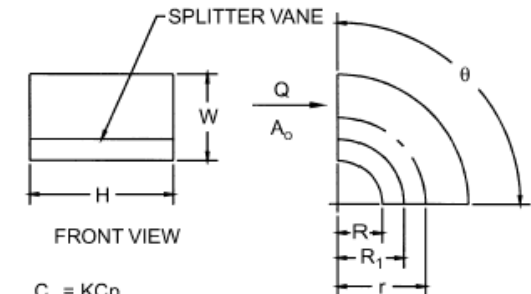


CR3-3 Elbow, Smooth Radius, One Splitter Vane

C <sub>p</sub> Values											
		H/W									
r/W	0.25	0.50	1.00	1.50	2.00	3.00	4.00	5.00	6.00	7.00	8.00
0.55	0.52	0.40	0.43	0.49	0.55	0.66	0.75	0.84	0.93	1.01	1.09
0.60	0.36	0.27	0.25	0.28	0.30	0.35	0.39	0.42	0.46	0.49	0.52
0.65	0.28	0.21	0.18	0.19	0.20	0.22	0.25	0.26	0.28	0.30	0.32
0.70	0.22	0.16	0.14	0.14	0.15	0.16	0.17	0.18	0.19	0.20	0.21
0.75	0.18	0.13	0.11	0.11	0.11	0.12	0.13	0.14	0.14	0.15	0.15
0.80	0.15	0.11	0.09	0.09	0.09	0.09	0.10	0.10	0.11	0.11	0.12
0.85	0.13	0.09	0.08	0.07	0.07	0.08	0.08	0.08	0.08	0.09	0.09
0.90	0.11	0.08	0.07	0.06	0.06	0.06	0.06	0.07	0.07	0.07	0.07
0.95	0.10	0.07	0.06	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06
1.00	0.09	0.06	0.05	0.05	0.04	0.04	0.04	0.05	0.05	0.05	0.05

Angle Factor K					
θ	0	30	45	60	90
K	0.00	0.45	0.60	0.78	1.00



$$C_o = KC_p$$

$$R_1 = R/CR$$

where

R = throat radius

R<sub>1</sub> = splitter vane radius

CR = curve ratio

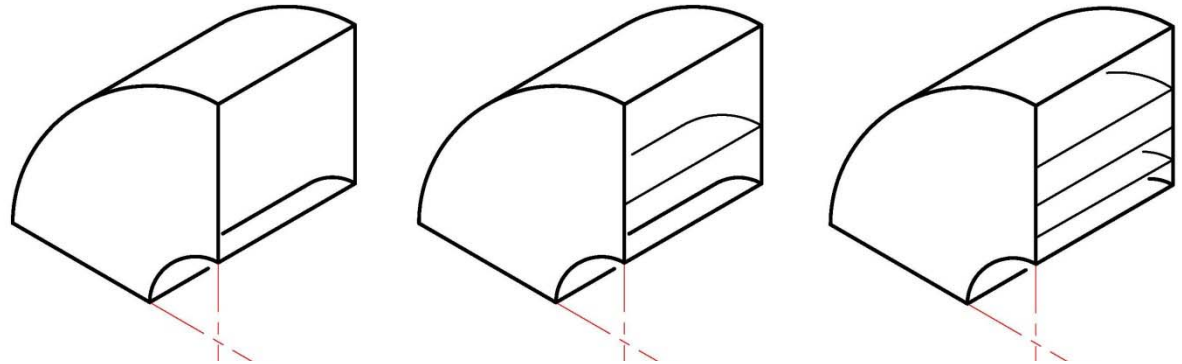
K = angle factor



# Selecting and Applying the Loss Coefficient

$$\Delta p_{fitting} = C_o p_{velocity}$$

$$\Delta p_{fitting} = .05 \times .56$$

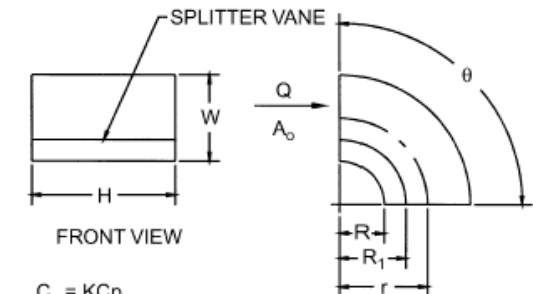


CR3-3 Elbow, Smooth Radius, One Splitter Vane

$r/W$	$C_p$ Values										
	H/W										
	0.25	0.50	1.00	1.50	2.00	3.00	4.00	5.00	6.00	7.00	8.00
0.55	0.52	0.40	0.43	0.49	0.55	0.66	0.75	0.84	0.93	1.01	1.09
0.60	0.36	0.27	0.25	0.28	0.30	0.35	0.39	0.42	0.46	0.49	0.52
0.65	0.28	0.21	0.18	0.19	0.20	0.22	0.25	0.26	0.28	0.30	0.32
0.70	0.22	0.16	0.14	0.14	0.15	0.16	0.17	0.18	0.19	0.20	0.21
0.75	0.18	0.13	0.11	0.11	0.11	0.12	0.13	0.14	0.14	0.15	0.15
0.80	0.15	0.11	0.09	0.09	0.09	0.09	0.10	0.10	0.11	0.11	0.12
0.85	0.13	0.09	0.08	0.07	0.07	0.08	0.08	0.08	0.08	0.09	0.09
0.90	0.11	0.08	0.07	0.06	0.06	0.06	0.06	0.07	0.07	0.07	0.07
0.95	0.10	0.07	0.06	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06
1.00	0.09	0.06	0.05	0.05	0.04	0.04	0.04	0.05	0.05	0.05	0.05

Angle Factor $K$					
$\theta$	0	30	45	60	90
$K$	0.00	0.45	0.60	0.78	1.00



$$C_o = KC_p$$

$$R_1 = R/CR$$

where

$R$  = throat radius

$R_1$  = splitter vane radius

$CR$  = curve ratio

$K$  = angle factor

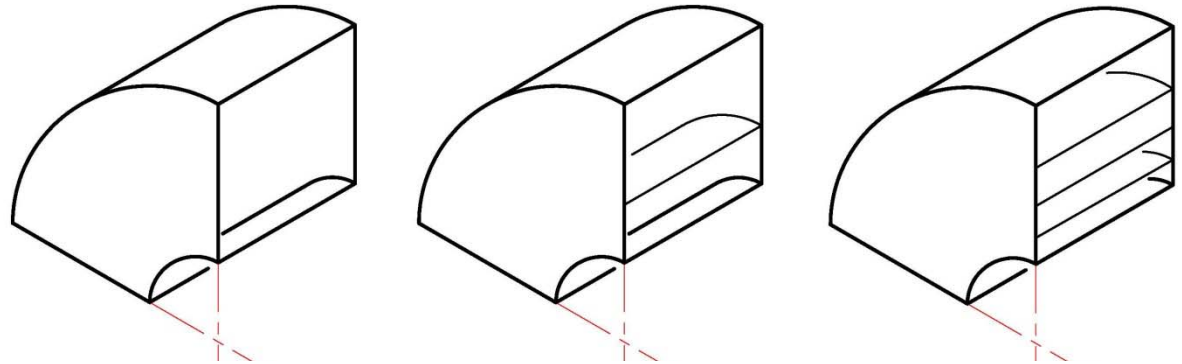


# Selecting and Applying the Loss Coefficient

$$\Delta p_{fitting} = C_o p_{velocity}$$

$$\Delta p_{fitting} = .05 \times .56$$

$$\Delta p_{fitting} = .03 \text{ in.w.c.}$$

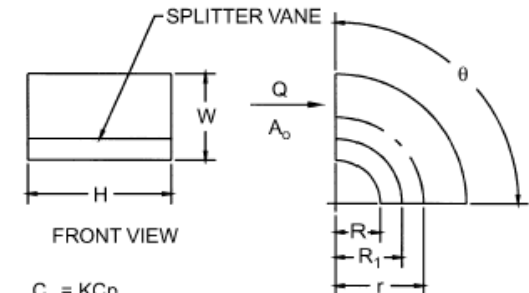


CR3-3 Elbow, Smooth Radius, One Splitter Vane

C <sub>p</sub> Values											
		H/W									
r/W	0.25	0.50	1.00	1.50	2.00	3.00	4.00	5.00	6.00	7.00	8.00
0.55	0.52	0.40	0.43	0.49	0.55	0.66	0.75	0.84	0.93	1.01	1.09
0.60	0.36	0.27	0.25	0.28	0.30	0.35	0.39	0.42	0.46	0.49	0.52
0.65	0.28	0.21	0.18	0.19	0.20	0.22	0.25	0.26	0.28	0.30	0.32
0.70	0.22	0.16	0.14	0.14	0.15	0.16	0.17	0.18	0.19	0.20	0.21
0.75	0.18	0.13	0.11	0.11	0.11	0.12	0.13	0.14	0.14	0.15	0.15
0.80	0.15	0.11	0.09	0.09	0.09	0.09	0.10	0.10	0.11	0.11	0.12
0.85	0.13	0.09	0.08	0.07	0.07	0.08	0.08	0.08	0.08	0.09	0.09
0.90	0.11	0.08	0.07	0.06	0.06	0.06	0.06	0.07	0.07	0.07	0.07
0.95	0.10	0.07	0.06	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06
1.00	0.09	0.06	0.05	0.05	0.04	0.04	0.04	0.05	0.05	0.05	0.05

Angle Factor K					
θ	0	30	45	60	90
K	0.00	0.45	0.60	0.78	1.00



$$C_o = KC_p$$

$$R_1 = R/CR$$

where

R = throat radius

R<sub>1</sub> = splitter vane radius

CR = curve ratio

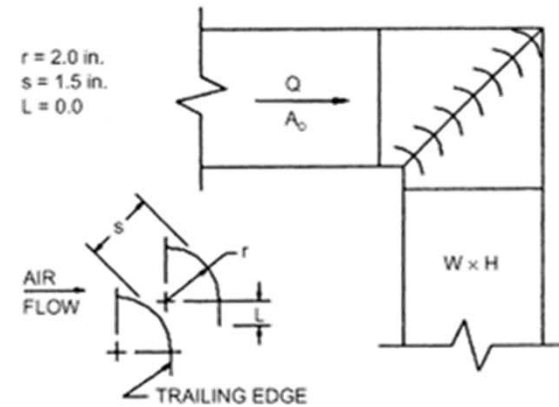
K = angle factor



# CR3-9 Elbow, Mitered, 90 Degree, Single-Thickness Vanes (Design 1)

## A Contrast

$$C_o = 0.11$$



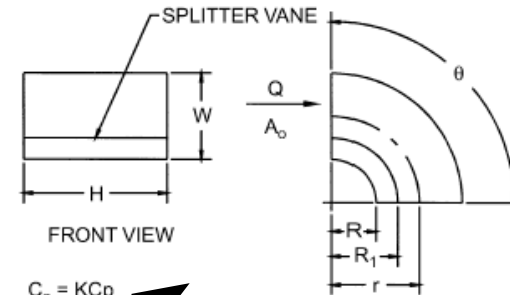
### CR3-3 Elbow, Smooth Radius, One Splitter Vane

$r/W$	$C_p$ Values										
	H/W										
	0.25	0.50	1.00	1.50	2.00	3.00	4.00	5.00	6.00	7.00	8.00
0.55	0.52	0.40	0.43	0.49	0.55	0.66	0.75	0.84	0.93	1.01	1.09
0.60	0.36	0.27	0.25	0.28	0.30	0.35	0.39	0.42	0.46	0.49	0.52
0.65	0.28	0.21	0.18	0.19	0.20	0.22	0.25	0.26	0.28	0.30	0.32
0.70	0.22	0.16	0.14	0.14	0.15	0.16	0.17	0.18	0.19	0.20	0.21
0.75	0.18	0.13	0.11	0.11	0.11	0.12	0.13	0.14	0.14	0.15	0.15
0.80	0.15	0.11	0.09	0.09	0.09	0.09	0.10	0.10	0.11	0.11	0.12
0.85	0.13	0.09	0.08	0.07	0.07	0.08	0.08	0.08	0.08	0.09	0.09
0.90	0.11	0.08	0.07	0.06	0.06	0.06	0.06	0.07	0.07	0.07	0.07
0.95	0.10	0.07	0.06	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06
1.00	0.09	0.06	0.05	0.05	0.04	0.04	0.04	0.05	0.05	0.05	0.05

Angle Factor $K$					
$\theta$	0	30	45	60	90
$K$	0.00	0.45	0.60	0.78	1.00

Curve Ratio CR										
$r/W$	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
CR	0.218	0.302	0.361	0.408	0.447	0.480	0.509	0.535	0.557	0.577

Throat Radius/Width Ratio ( $R/W$ )										
$r/W$	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
$R/W$	0.05	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50



$C_o = KC_p$   
 $R_1 = R/CR$   
 where  
 $R$  = throat radius  
 $R_1$  = splitter vane radius  
 $CR$  = curve ratio  
 $K$  = angle factor

$C_p = C_o$  for a 90° elbow



# CR3-9 Elbow, Mitered, 90 Degree, Single-Thickness Vanes (Design 1)

## A Contrast

$$C_{\phi} = 0.11$$

The loss coefficient for a mitered 90° elbow is about twice that of a radiused 90° elbow with one vane

### CR3-3 Elbow, Smooth Radius, One Splitter Vane

$r/W$	$C_p$ Values										
	H/W										
	0.25	0.50	1.00	1.50	2.00	3.00	4.00	5.00	6.00	7.00	8.00
0.55	0.52	0.40	0.43	0.49	0.55	0.66	0.75	0.84	0.93	1.01	1.09
0.60	0.36	0.27	0.25	0.28	0.30	0.35	0.39	0.42	0.46	0.49	0.52
0.65	0.28	0.21	0.18	0.19	0.20	0.22	0.25	0.26	0.28	0.30	0.32
0.70	0.22	0.16	0.14	0.14	0.15	0.16	0.17	0.18	0.19	0.20	0.21
0.75	0.18	0.13	0.11	0.11	0.11	0.12	0.13	0.14	0.14	0.15	0.15
0.80	0.15	0.11	0.09	0.09	0.09	0.09	0.10	0.10	0.11	0.11	0.12
0.85	0.13	0.09	0.08	0.07	0.07	0.08	0.08	0.08	0.08	0.09	0.09
0.90	0.11	0.08	0.07	0.06	0.06	0.06	0.06	0.07	0.07	0.07	0.07
0.95	0.10	0.07	0.06	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06
1.00	0.09	0.06	0.05	0.05	0.04	0.04	0.04	0.05	0.05	0.05	0.05

### Angle Factor $K$

$\theta$	0	30	45	60	90
$K$	0.00	0.45	0.60	0.78	1.00

### Curve Ratio CR

$r/W$	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
CR	0.218	0.302	0.361	0.408	0.447	0.480	0.509	0.535	0.557	0.577

### Throat Radius/Width Ratio ( $R/W$ )

$r/W$	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00
$R/W$	0.05	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50

$r = 2.0$  in.  
 $s = 1.5$  in.  
 $L = 0.0$

AIR FLOW

TRAILING EDGE

FRONT VIEW

$$C_L = KC_p$$

where

$R$  = throat radius

$R_1$  = splitter vane radius

CR = curve ratio

$K$  = angle factor