

Facility Dynamics

ENGINEERING

Controlling the Mixed Air Section

Assessing an Economizer (Supplemental)

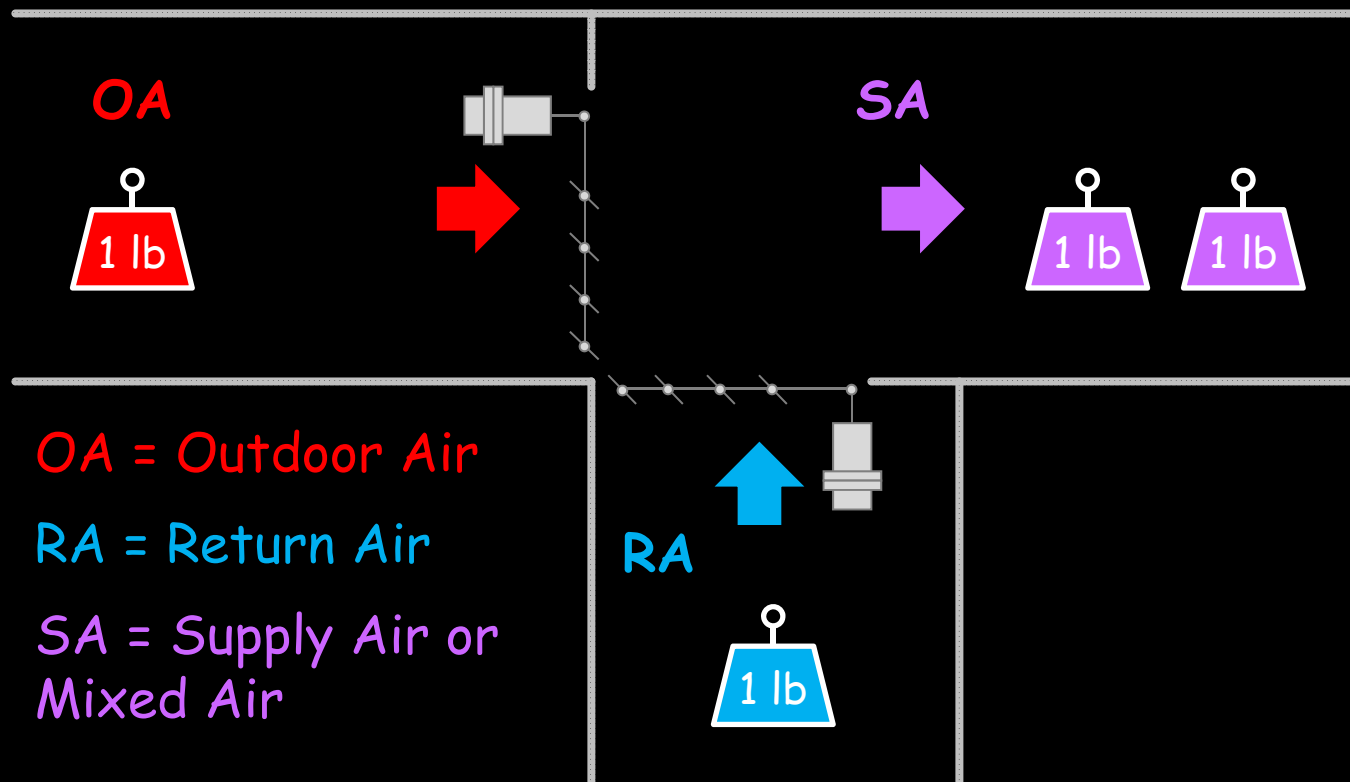
Presented By:

David Sellers; Facility Dynamics Engineering

Senior Engineer

NAVFAC, San Diego

Conservation of Mass in a Mixed Air Plenum



Conservation of Mass in a Mixed Air Plenum

$$\dot{m}_{\text{OutdoorAir}} + \dot{m}_{\text{ReturnAir}} = \dot{m}_{\text{MixedAir}}$$

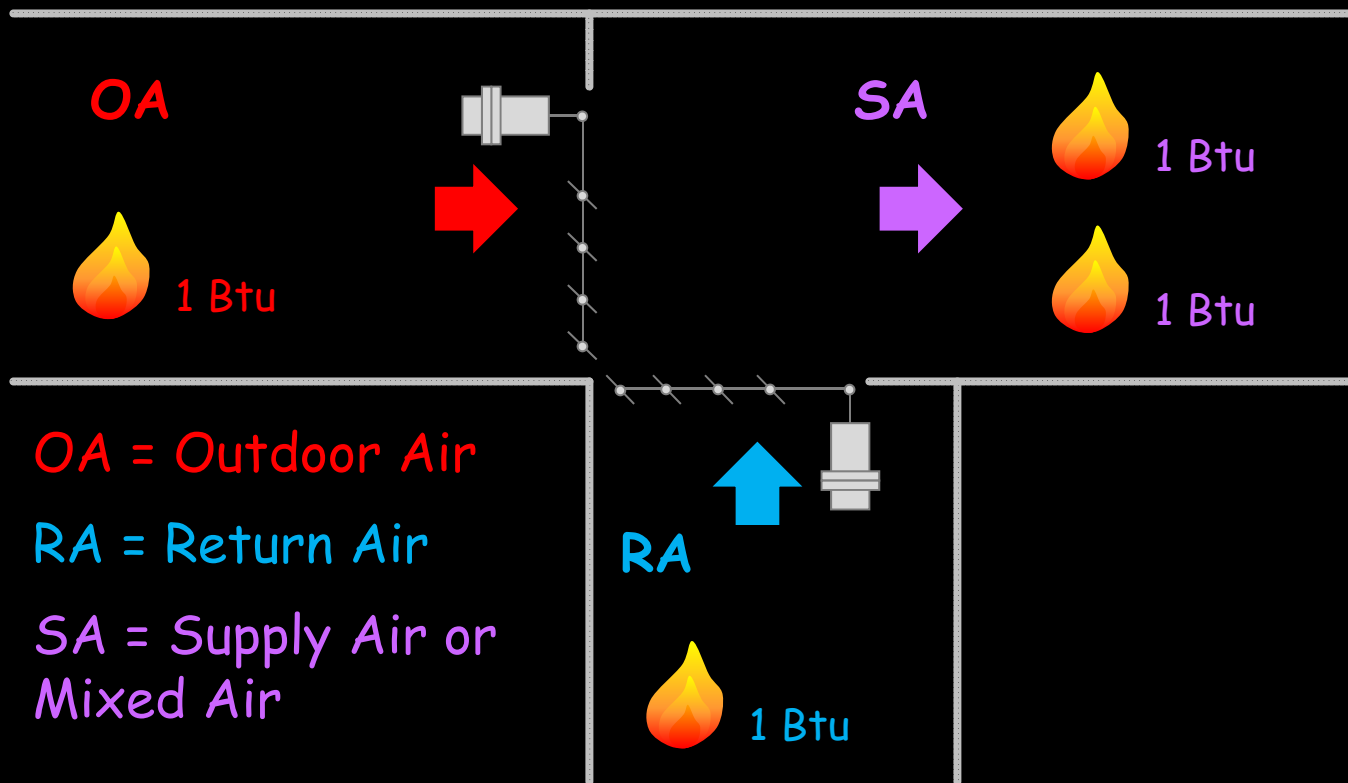
Where:

$\dot{m}_{\text{OutdoorAir}}$ = Mass flow rate for outdoor air in consistent units

$\dot{m}_{\text{ReturnAir}}$ = Mass flow rate for return air in consistent units

$\dot{m}_{\text{MixedAir}}$ = Mass flow rate for mixed air in consistent units

Conservation of Energy in a Mixed Air Plenum



This is the first law of thermodynamics

Conservation of Energy in a Mixed Air Plenum

If any system undergoes a process in which energy is added or removed from it (in the form of work or heat), none of the energy added is destroyed with-in the system and none of the energy removed is created with-in the system

*Herman Stoever,
Engineering Thermodynamics*

This is the first law of thermodynamics

Conservation of Energy in a Mixed Air Plenum

$$Q + u_1 + \frac{p_1 v_1}{J} + \frac{z_1}{J} + \frac{V_1^2}{2gJ} = \frac{W}{J} + u_2 + \frac{p_2 v_2}{J} + \frac{z_2}{J} + \frac{V_2^2}{2gJ}$$

Where:

Q = Heat in Btu/lb

W = Shaft work, ft-lb/lb

u = Internal energy, Btu/lb

pv = Flow work; pressure in lb/ft² x specific volume in ft³/lb, ft-lb/lb

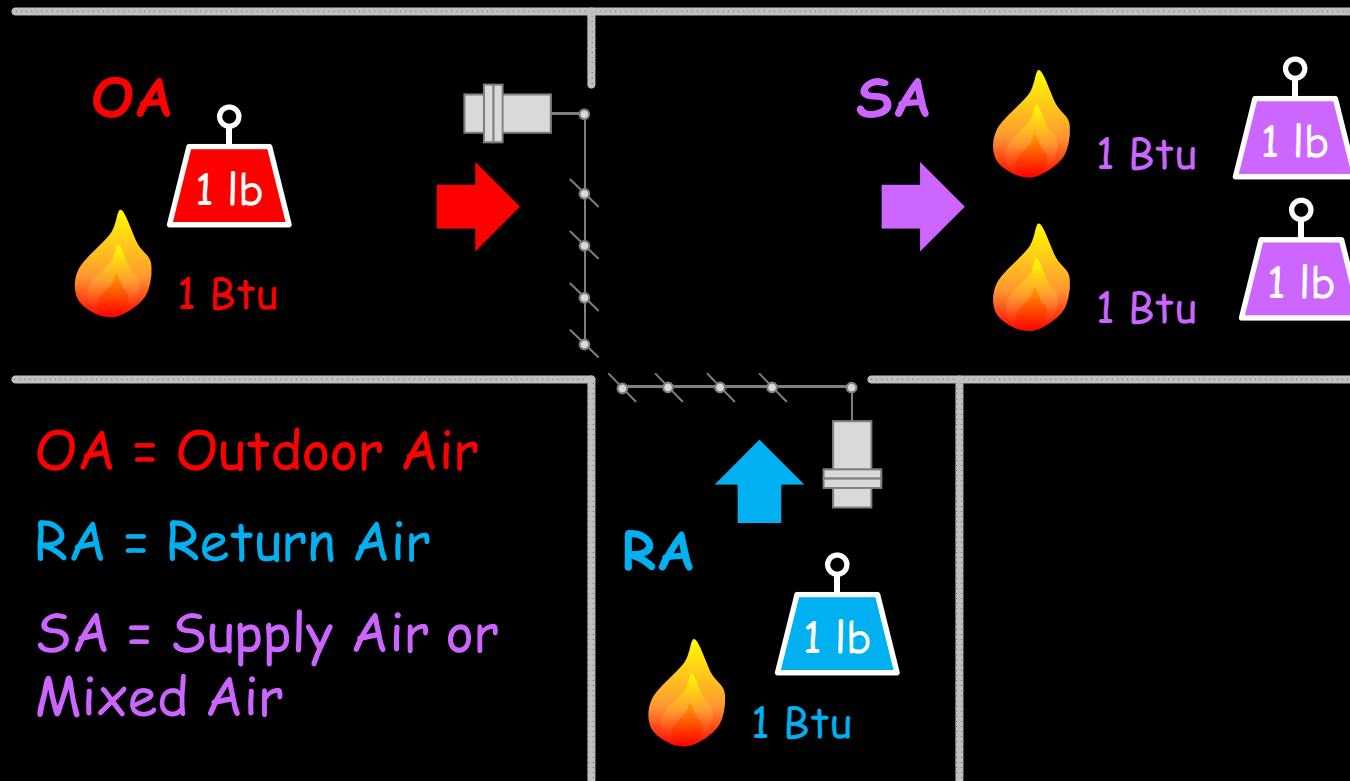
J = Mechanical equivalent of heat; 778 ft-lb/Btu

V = Velocity in feet per second

g = gravitational constant, 32 ft/sec/sec

This is the first law of thermodynamics stated mathematically

Conservation of Mass and Energy in a Mixed Air Plenum



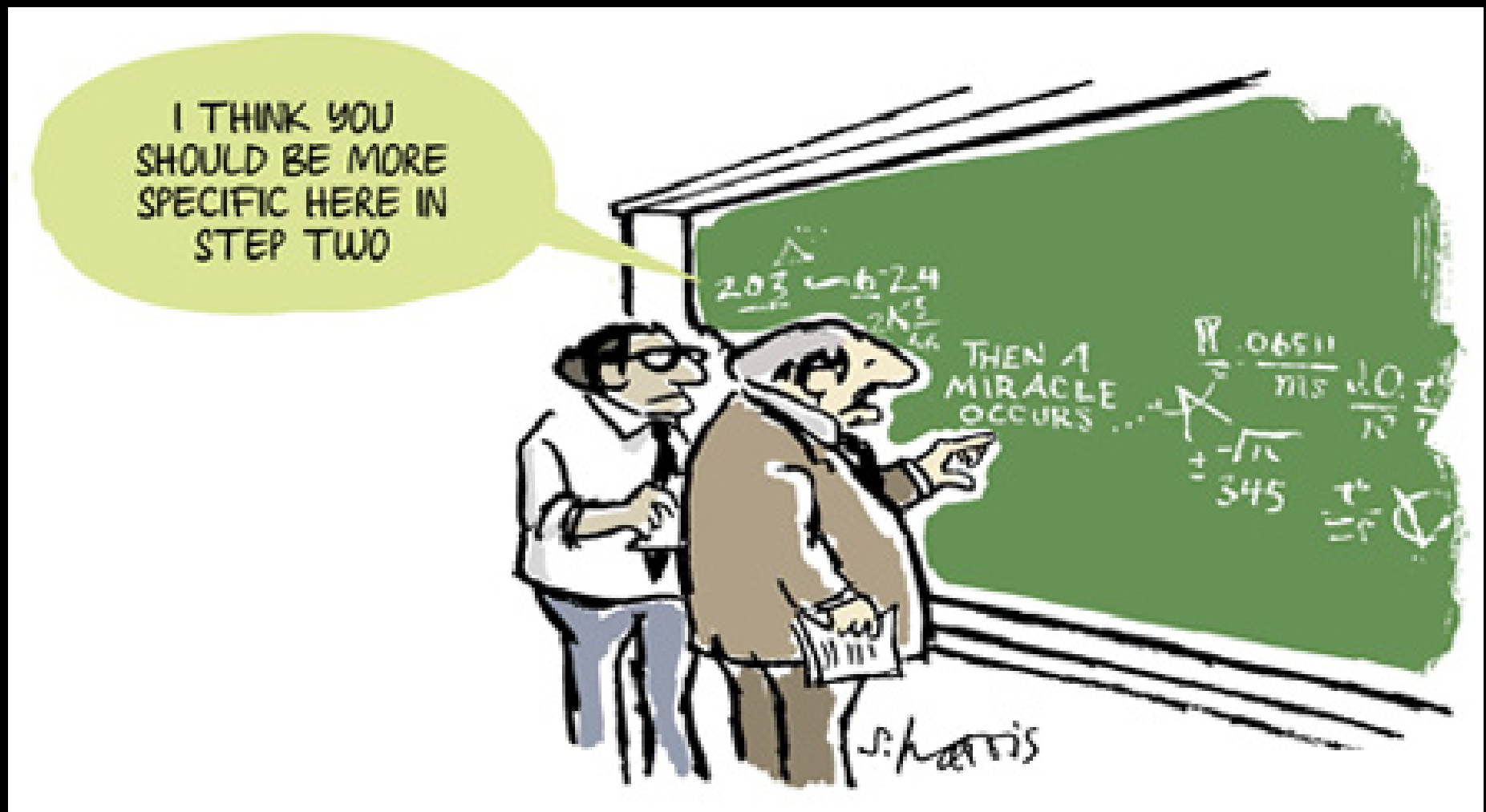
Conservation of Mass and Energy in a Mixed Air Plenum

$$\bar{Q} + \sum_1 \left[\dot{m} \times \left(u_1 + \frac{p_1 v_1}{J} + \frac{z_1}{J} + \frac{V_1^2}{2gJ} \right) \right] = \frac{\bar{W}}{J} + \sum_2 \left[\dot{m} \times \left(u_2 + \frac{p_2 v_2}{J} + \frac{z_2}{J} + \frac{V_2^2}{2gJ} \right) \right]$$

Where the bar over the Q and W terms (\bar{Q} and \bar{W}) means that the heat transfer and/or work are being done at some sort of rate, like Btu/hr or ft-lb/hr, and the dot over the m term (\dot{m}) means a mass flow rate, like pounds per hour.

The \sum symbol means that the parameters inside the parenthesis are totalled up for all of the fluid streams on each side of the equation.

Fast Forwarding ...



Ta-Da

$$\%_{OutdoorAir} = \frac{(t_{MixedAir} - t_{ReturnAir})}{(t_{OutdoorAir} - t_{ReturnAir})}$$

Assuming perfect mixing

See [Economizers – The Physics of a Mixed Air Plenum](http://www.Av8rDAS.Wordpress.com) at www.Av8rDAS.Wordpress.com for the in-between steps

A Few Other Useful Relationships

$$t_{OutdoorAir_{Mix32}} = \left[\frac{(32 - t_{ReturnAir})}{\%_{OutdoorAir}} \right] + t_{ReturnAir}$$

Where $t_{OutdoorAir_{Mix32}}$ is the outdoor temperature that will create a freezing condition in the mixed air plenum.

A Few Other Useful Relationships

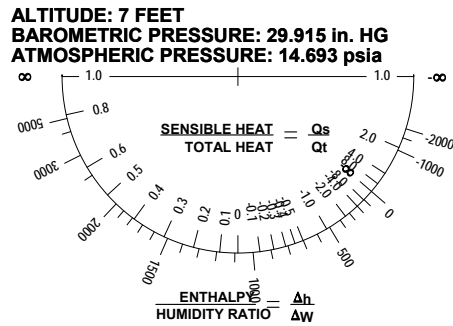
$$t_{OutdoorAir} = \left[\frac{(t_{MixedAir_{Design}} - t_{ReturnAir})}{\%_{OutdoorAir}} \right] + t_{ReturnAir}$$

Where $t_{MixedAir_{Design}}$ is the design mixed air temperature for the system and $t_{OutdoorAir}$ is the outdoor temperature that will create that condition.

A Few Other Useful Relationships

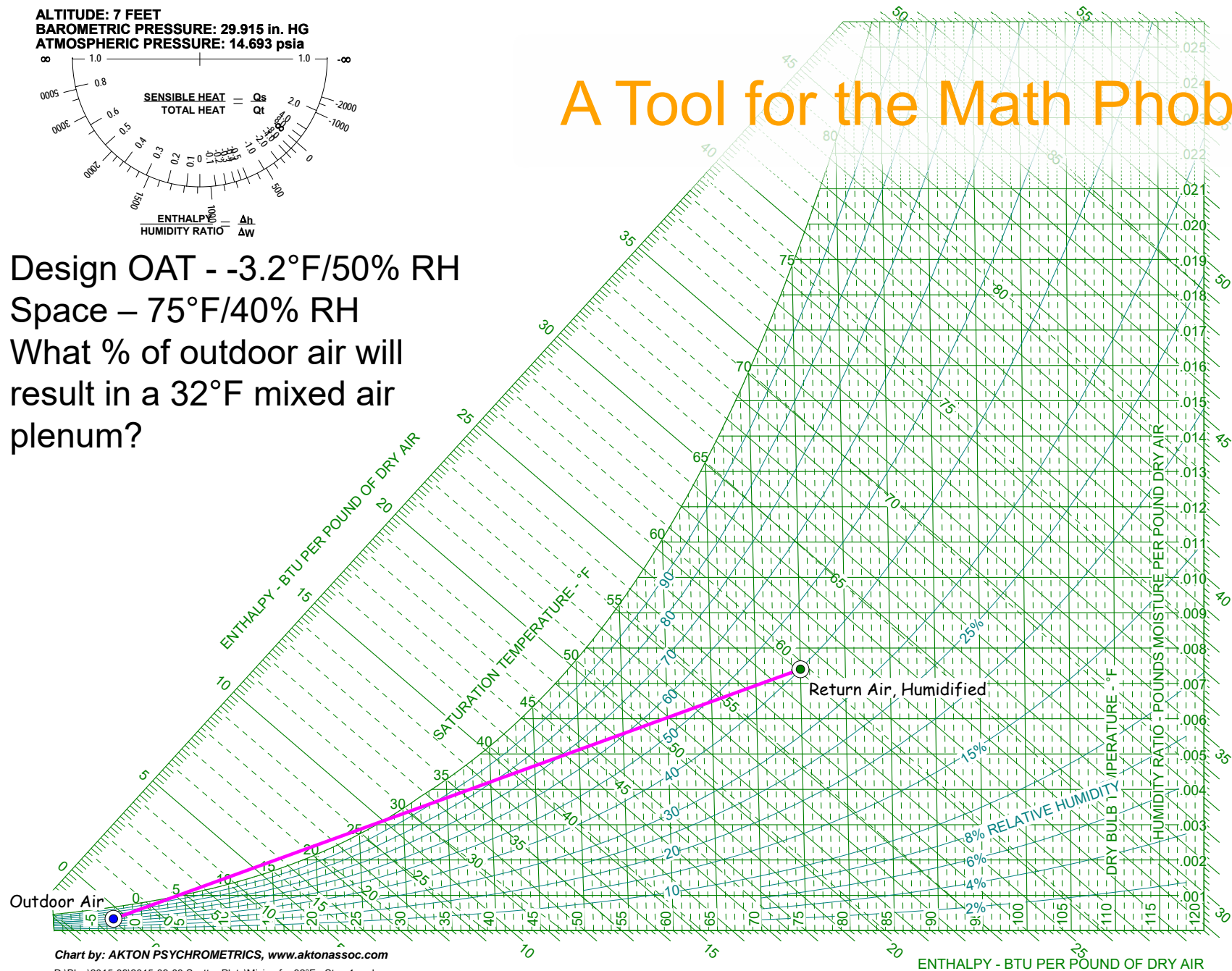
$$t_{MixedAir} = \left[\%_{OutdoorAir} \times (t_{OutdoorAir} - t_{ReturnAir}) \right] + t_{ReturnAir}$$

Where $t_{MixedAir}$ is the mixed air temperature created by the given outdoor air and return air temperatures and flow percentages *assuming perfect mixing*.



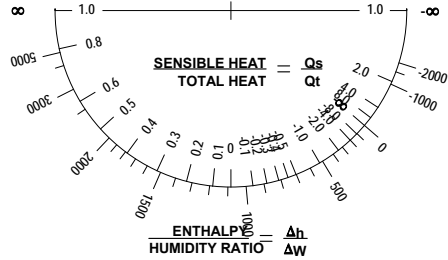
A Tool for the Math Phobic

Design OAT - -3.2°F/50% RH
 Space – 75°F/40% RH
 What % of outdoor air will
 result in a 32°F mixed air
 plenum?



TAB 14-4 - ASSESSING AN ECONOMIZER

ALTITUDE: 7 FEET
 BAROMETRIC PRESSURE: 29.915 in. HG
 ATMOSPHERIC PRESSURE: 14.693 psia



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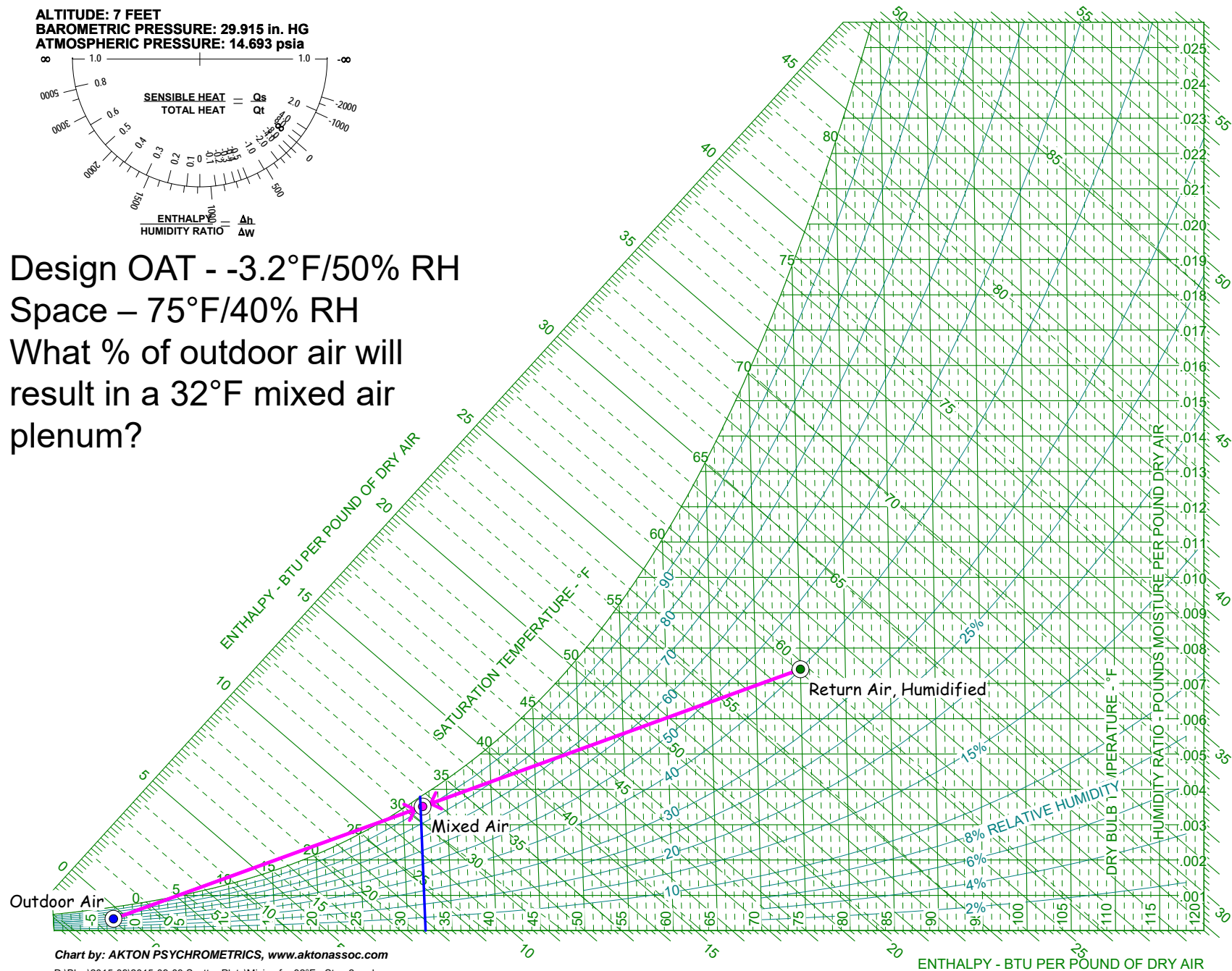
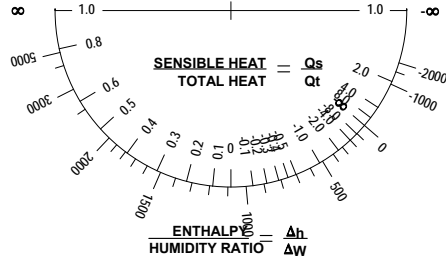


Chart by: AKTON PSYCHROMETRICS, www.aktonassoc.com
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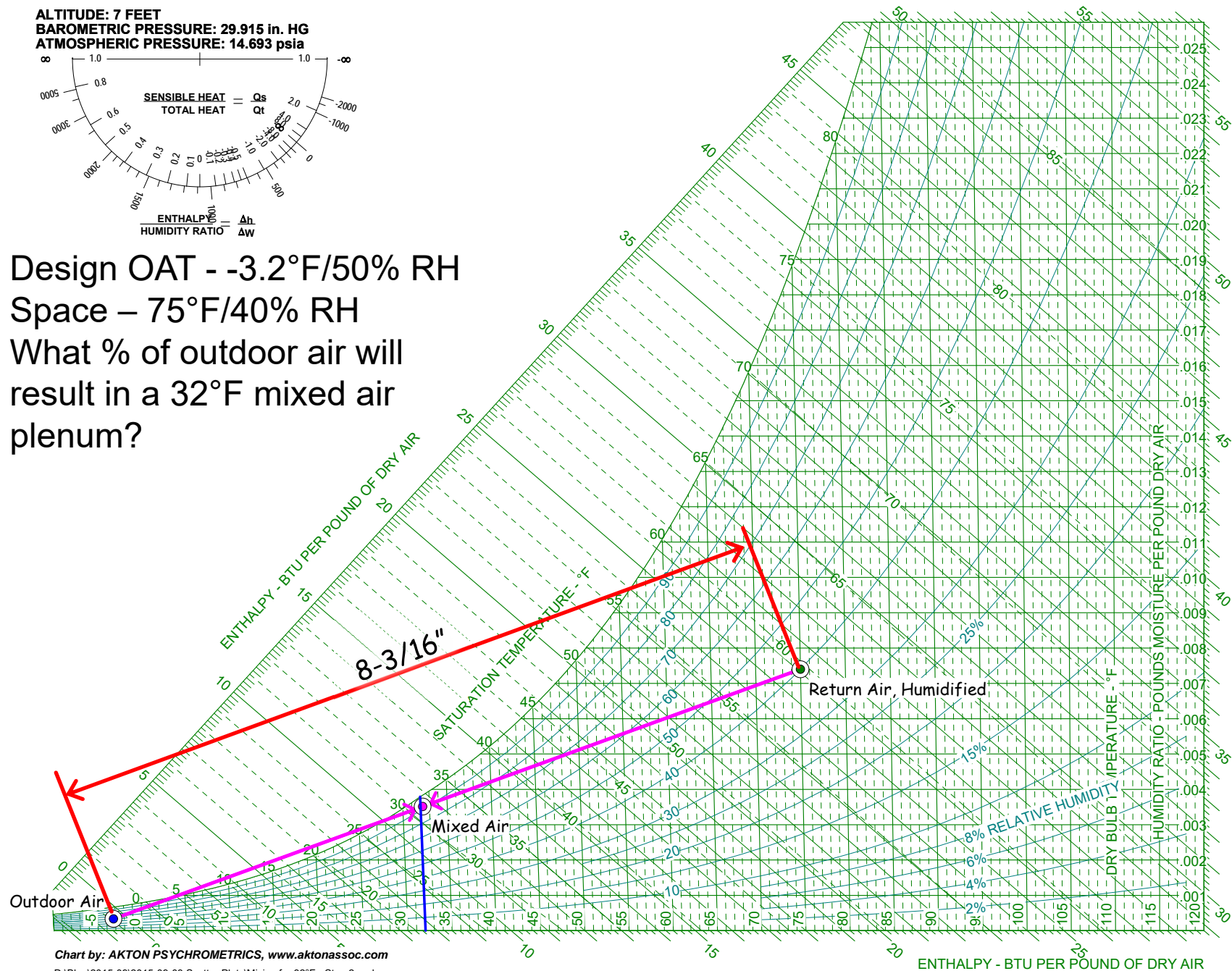
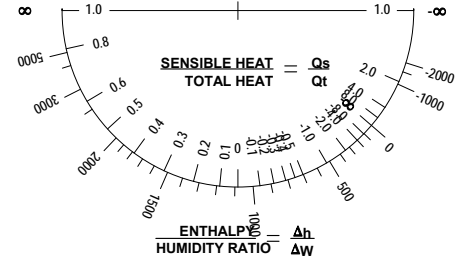


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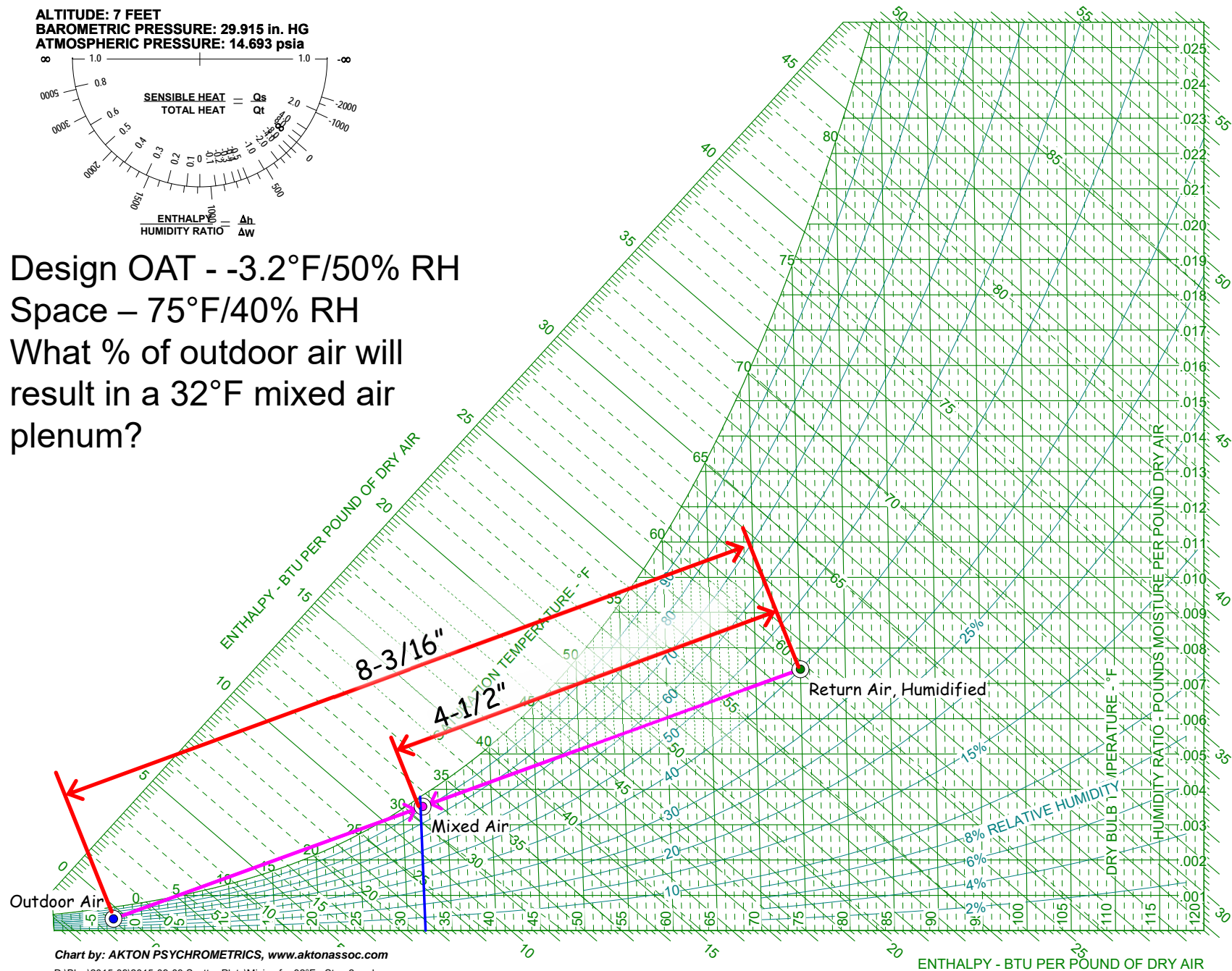
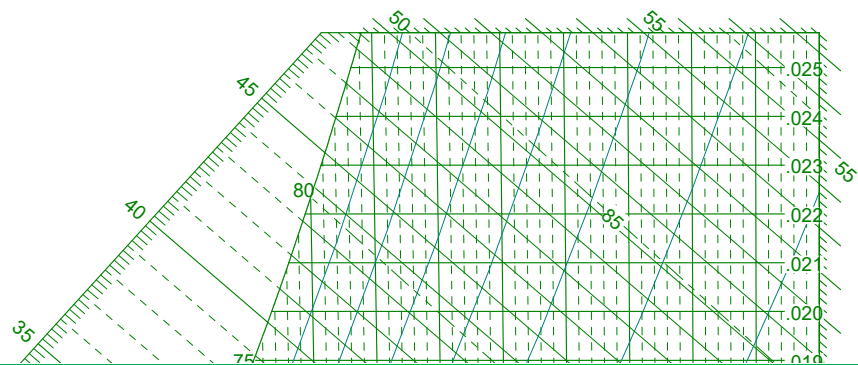
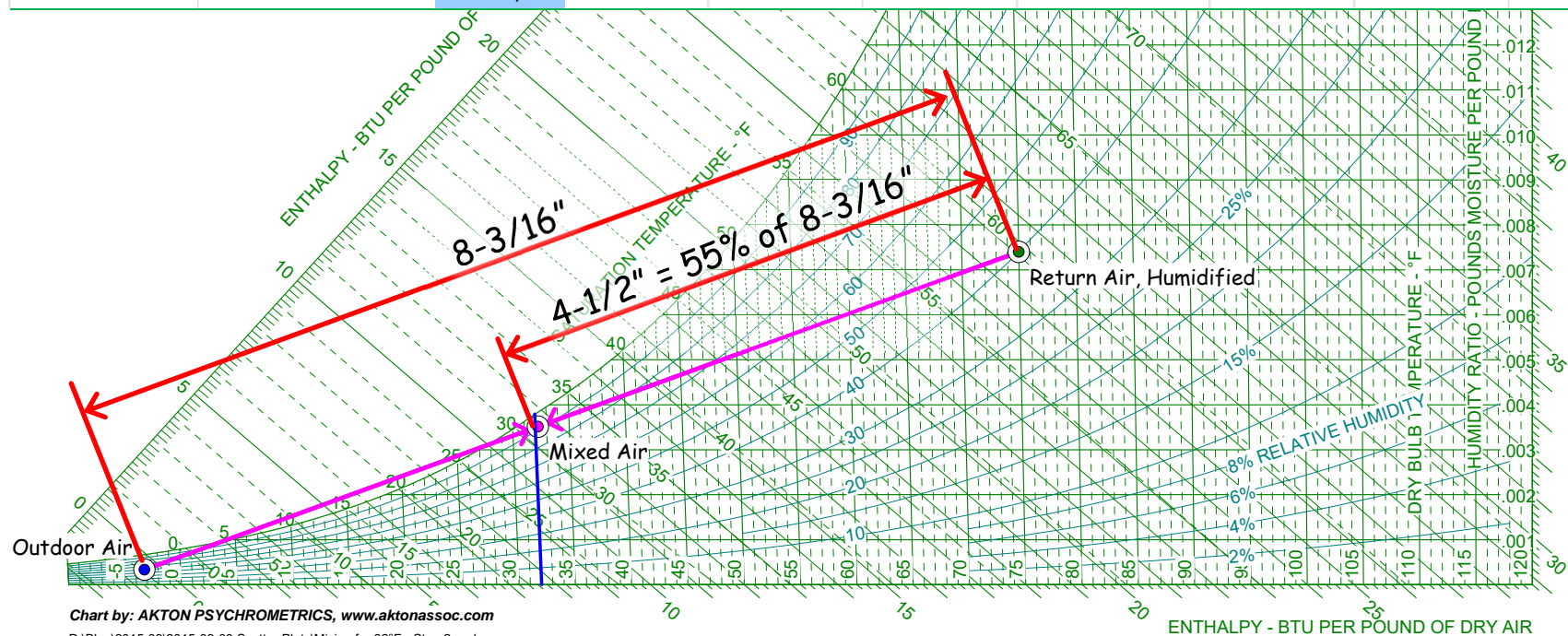


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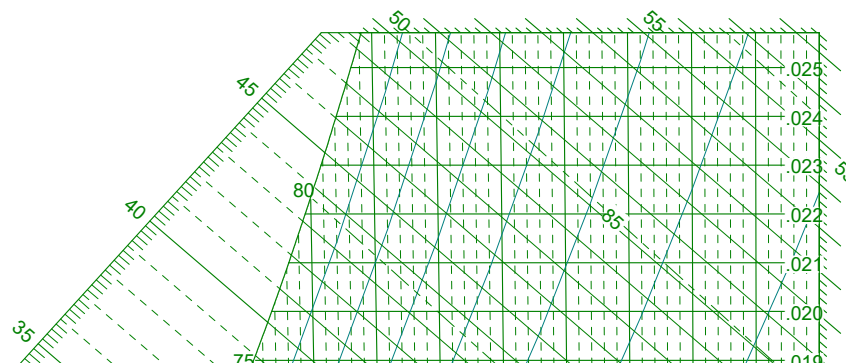
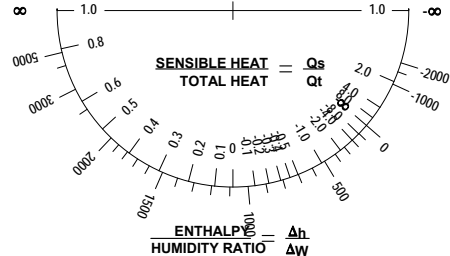
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Mixed air temperature (MAT) =	32.0 °F	$\%OutdoorAir = \frac{(t_{MixedAir} - t_{ReturnAir})}{(t_{OutdoorAir} - t_{ReturnAir})}$				
Return air temperature (RAT) =	75.0 °F					
Outdoor air temperature (OAT)=	-3.2 °F					
Supply flow (SAF) =	20,000 cfm					
Outdoor air flow (OA Flow) =	10,997 cfm					
Outdoor air percentage =	55%					
RA Flow =	9,003 cfm					

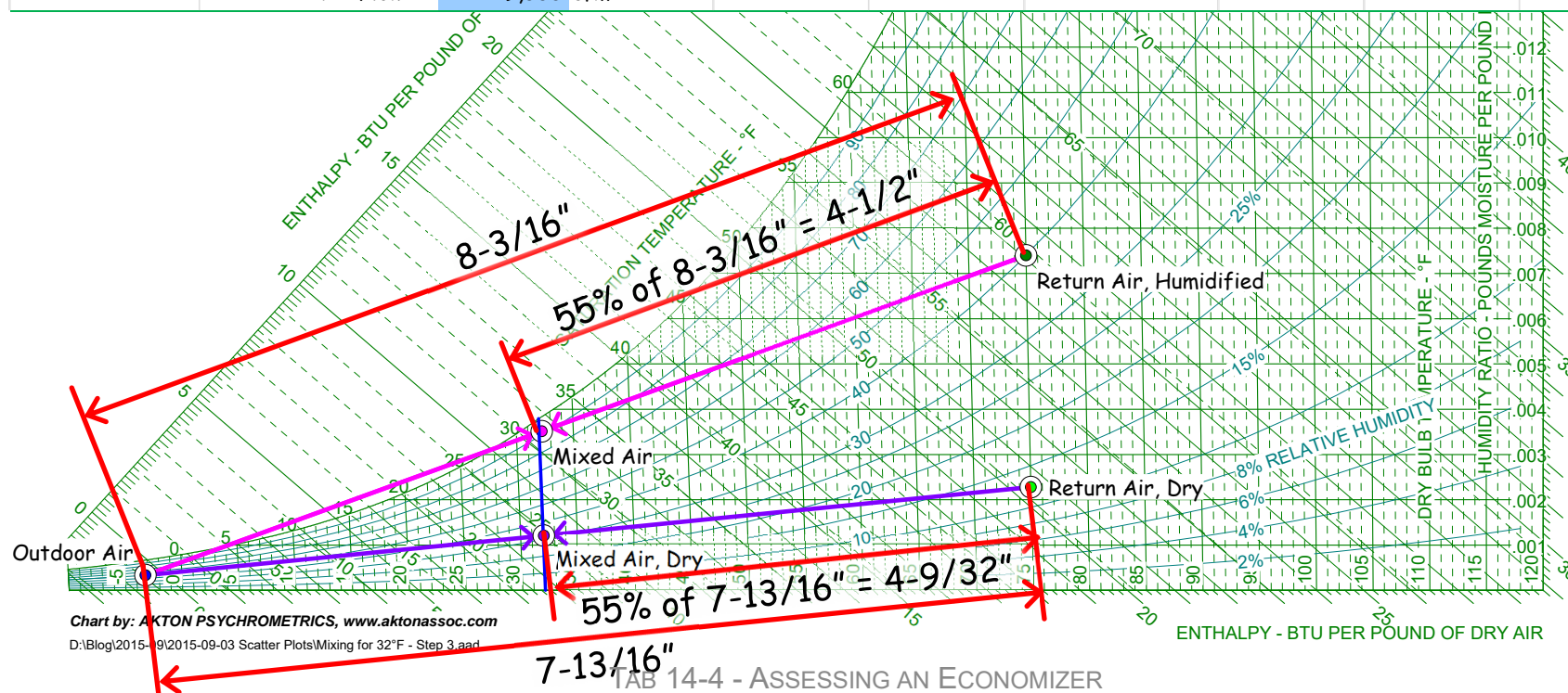


ALTITUDE: 7 FEET
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Outdoor percentage based on outdoor air, return air, and supply air temperature

Mixed air temperature (MAT) =	32.0 °F	$\%_{OutdoorAir} = \frac{(t_{MixedAir} - t_{ReturnAir})}{(t_{OutdoorAir} - t_{ReturnAir})}$			
Return air temperature (RAT) =	75.0 °F				
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Assessing the Perfect Economizer Using These Relationships

What is a Perfect Economizer?

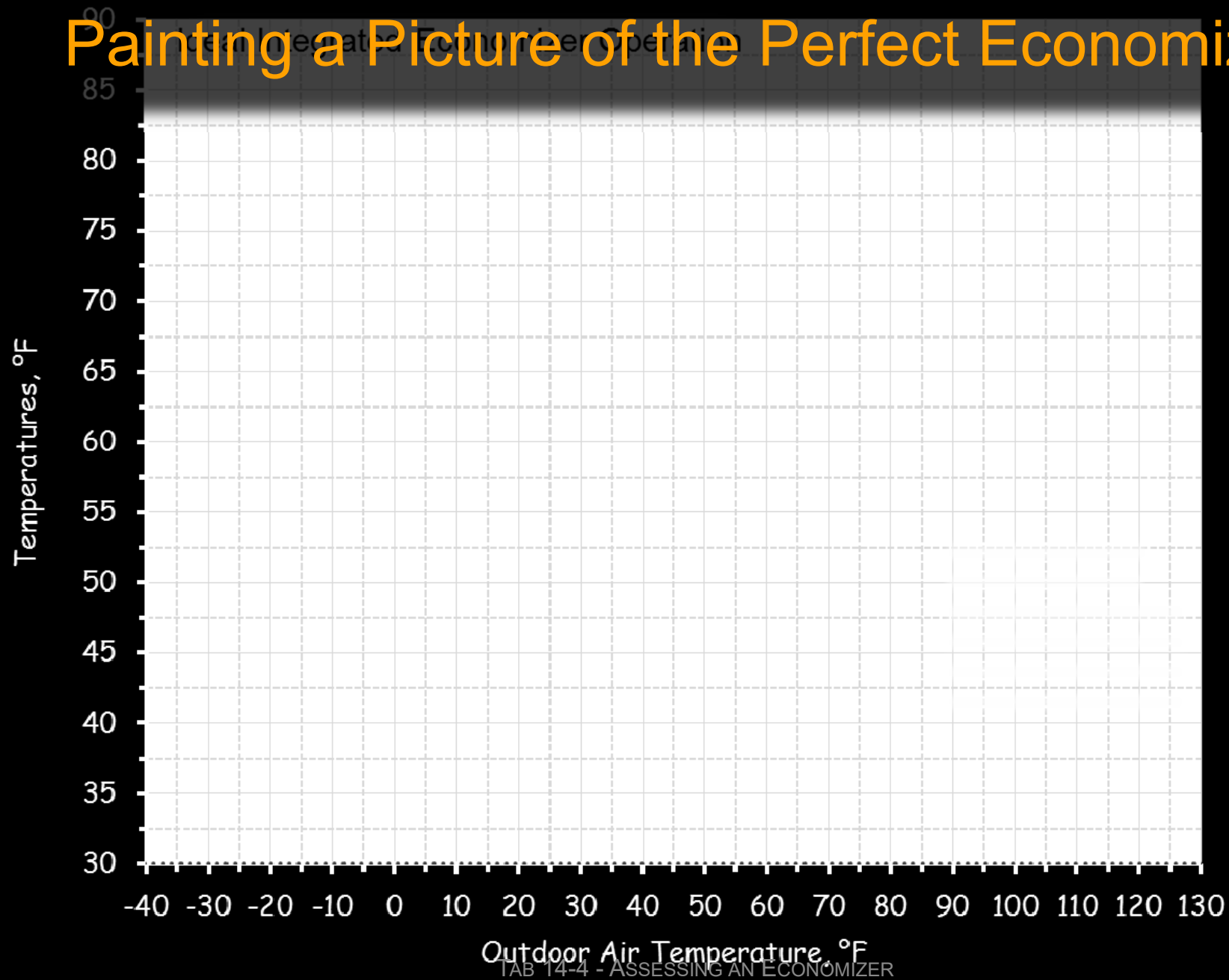
- Does not provide cooling if the preheat process is active
- Promotes good mixing
- Based on the true mixed air temperature
- Set point is properly coordinated with other HVAC processes occurring in the system
- Integrated with mechanical cooling to minimize energy consumption
 - Mechanical cooling not used until outdoor air can not meet set point
 - Outdoor air setting returned to the minimum requirement when outdoor air conditions make it no longer suitable for cooling
- Disabled when the system is not in operation

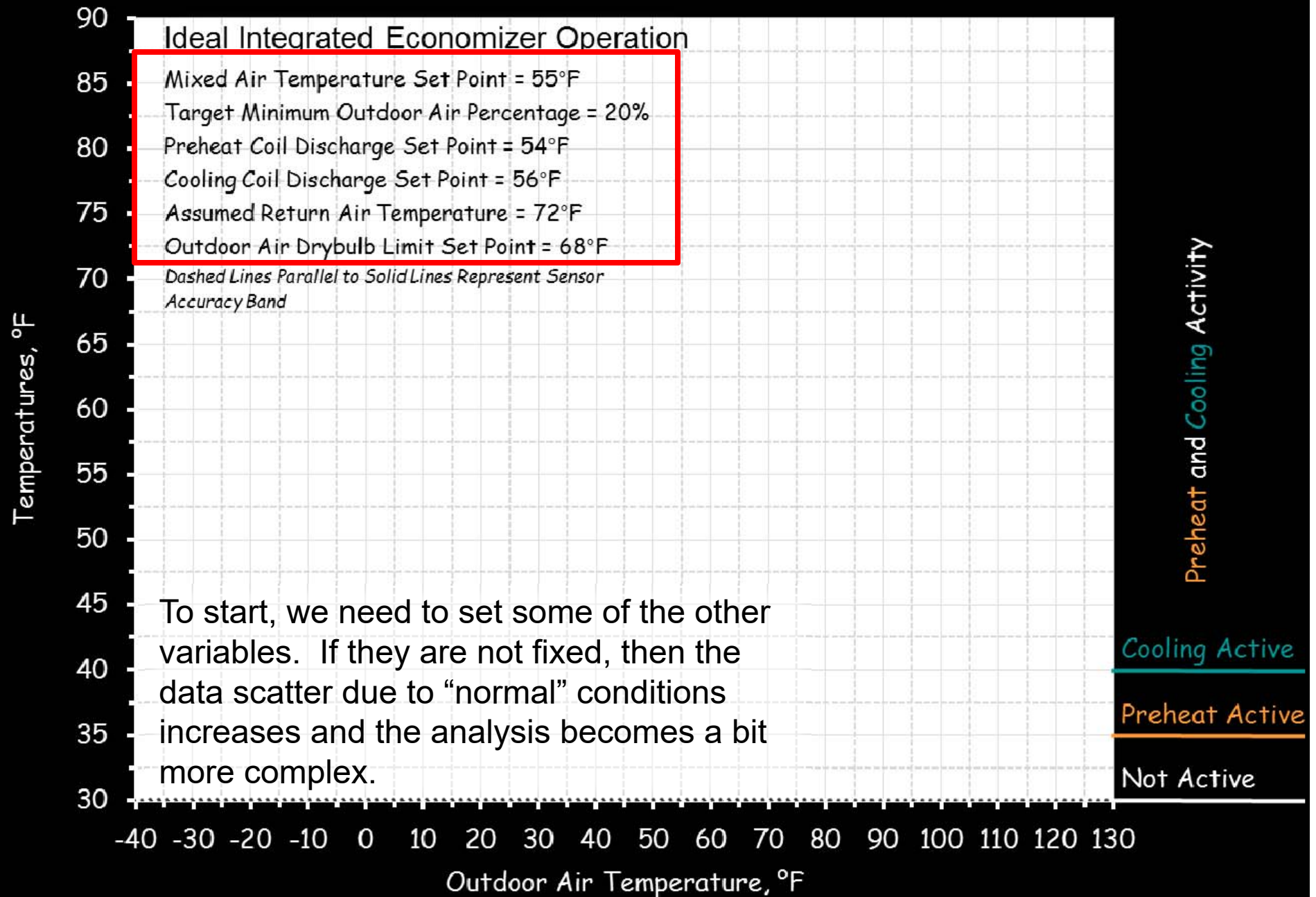
Painting a Picture of the Perfect Economizer

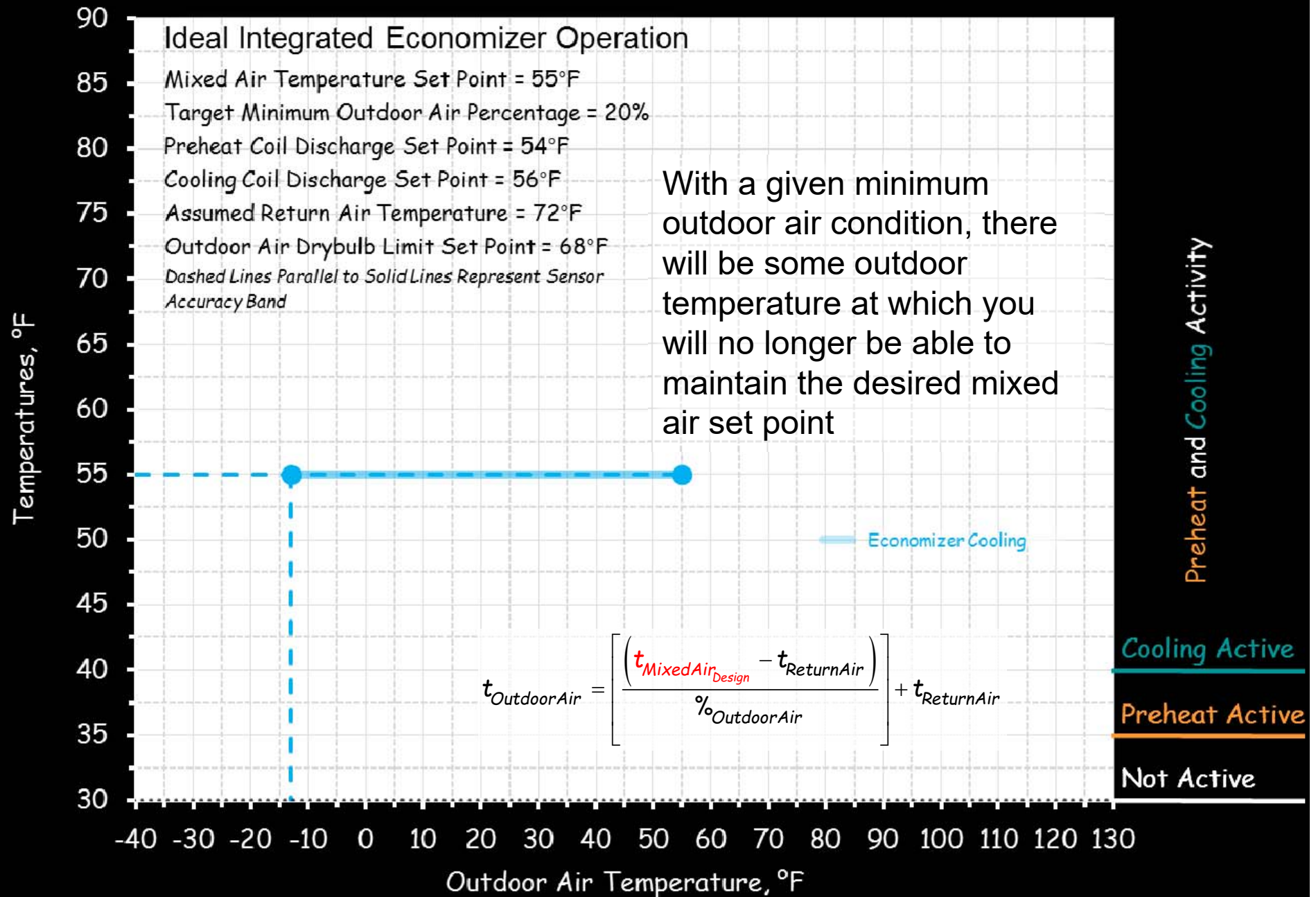
Plot mixed air temperature (the dependent variable) as a function of some other economizer related parameter like outdoor temperature (the independent variable)

- There should be a predictable mixed air temperature for every value of the dependent variable
- The predicted data points for a perfect economizer will draw a line on the graph
- The data points for a real economizer will create a cloud when you plot them
 - Cloud follows the perfect economizer line – Good
 - Cloud doesn't follow the perfect economizer line – Bad (and a clue about What is Wrong)

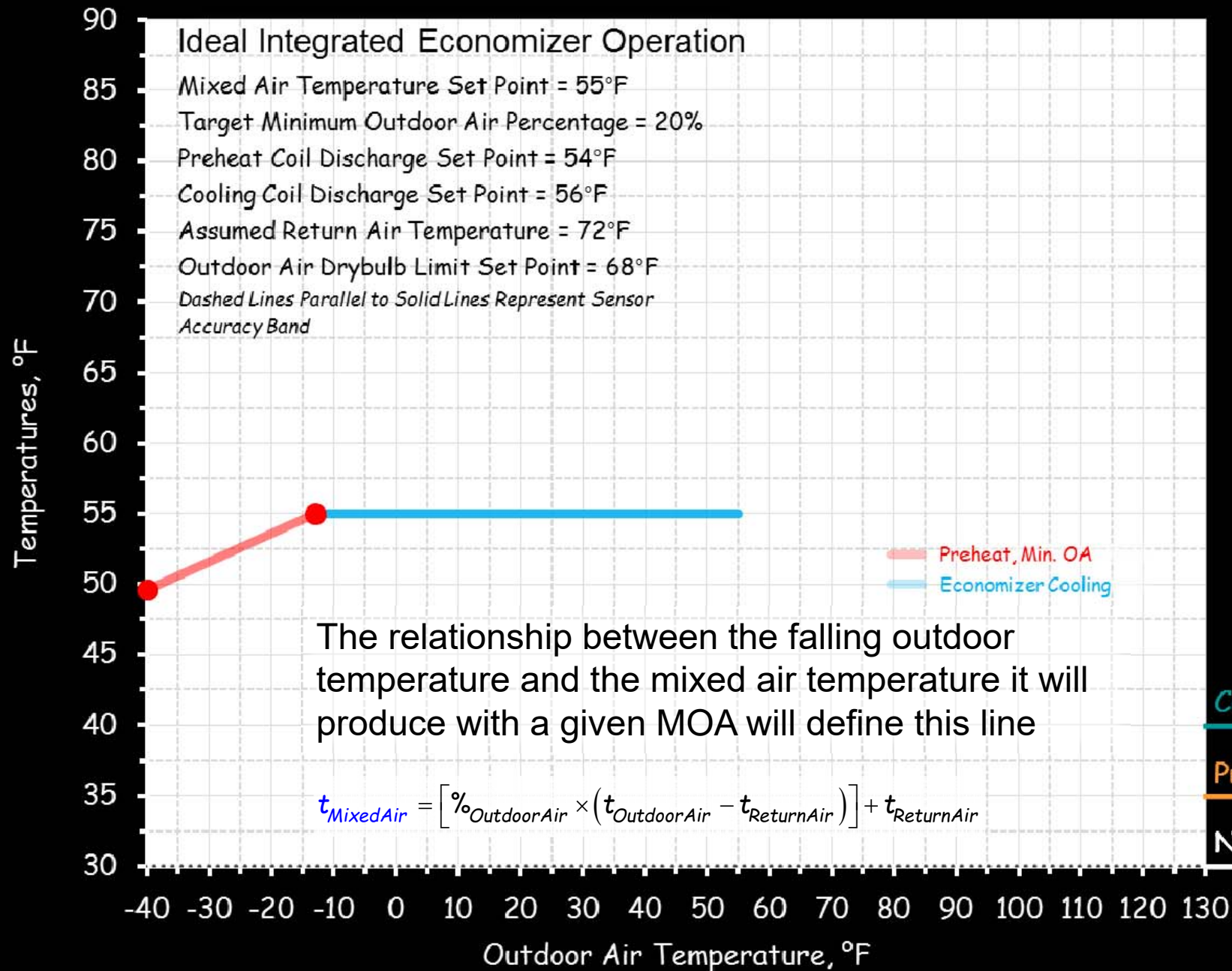
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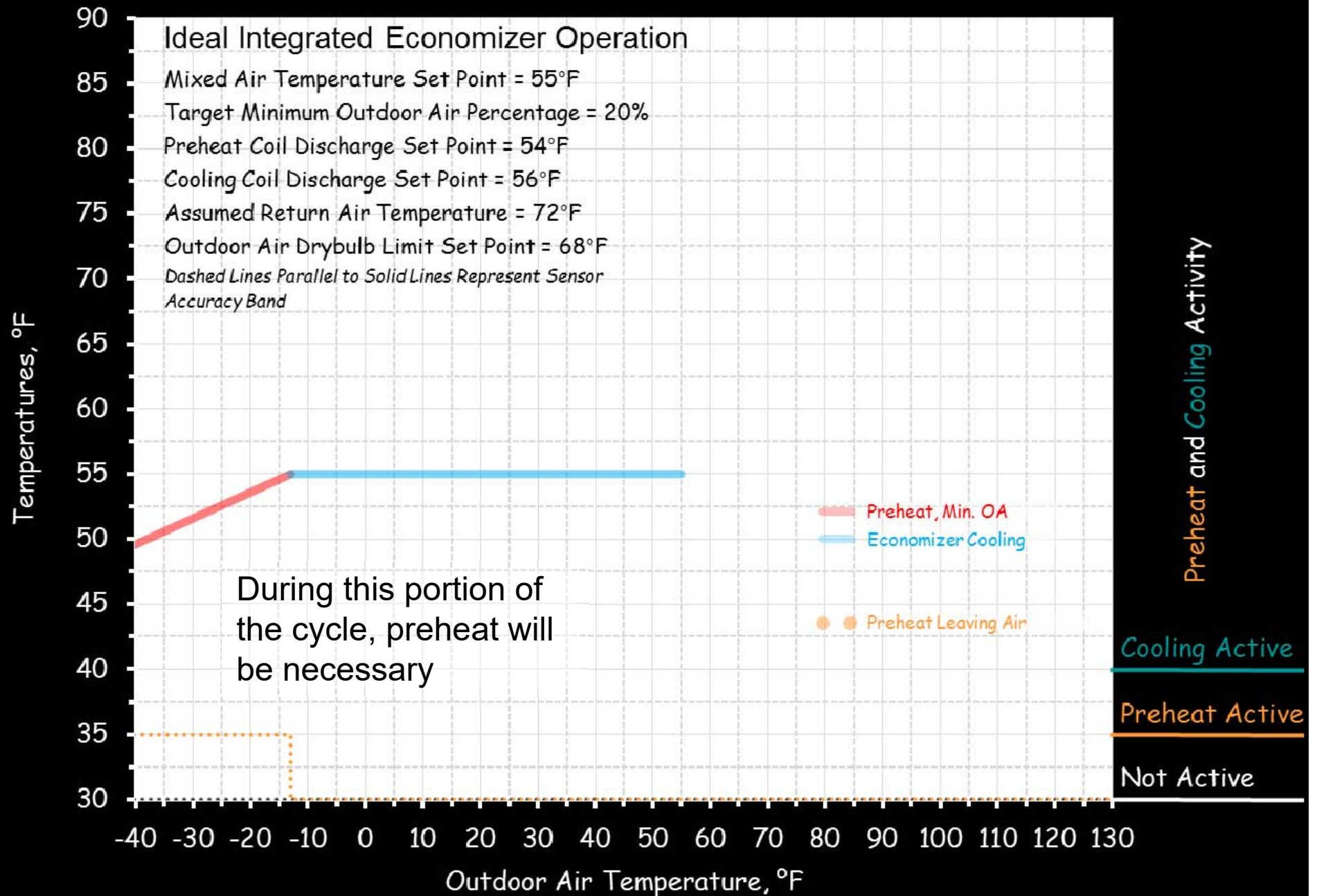


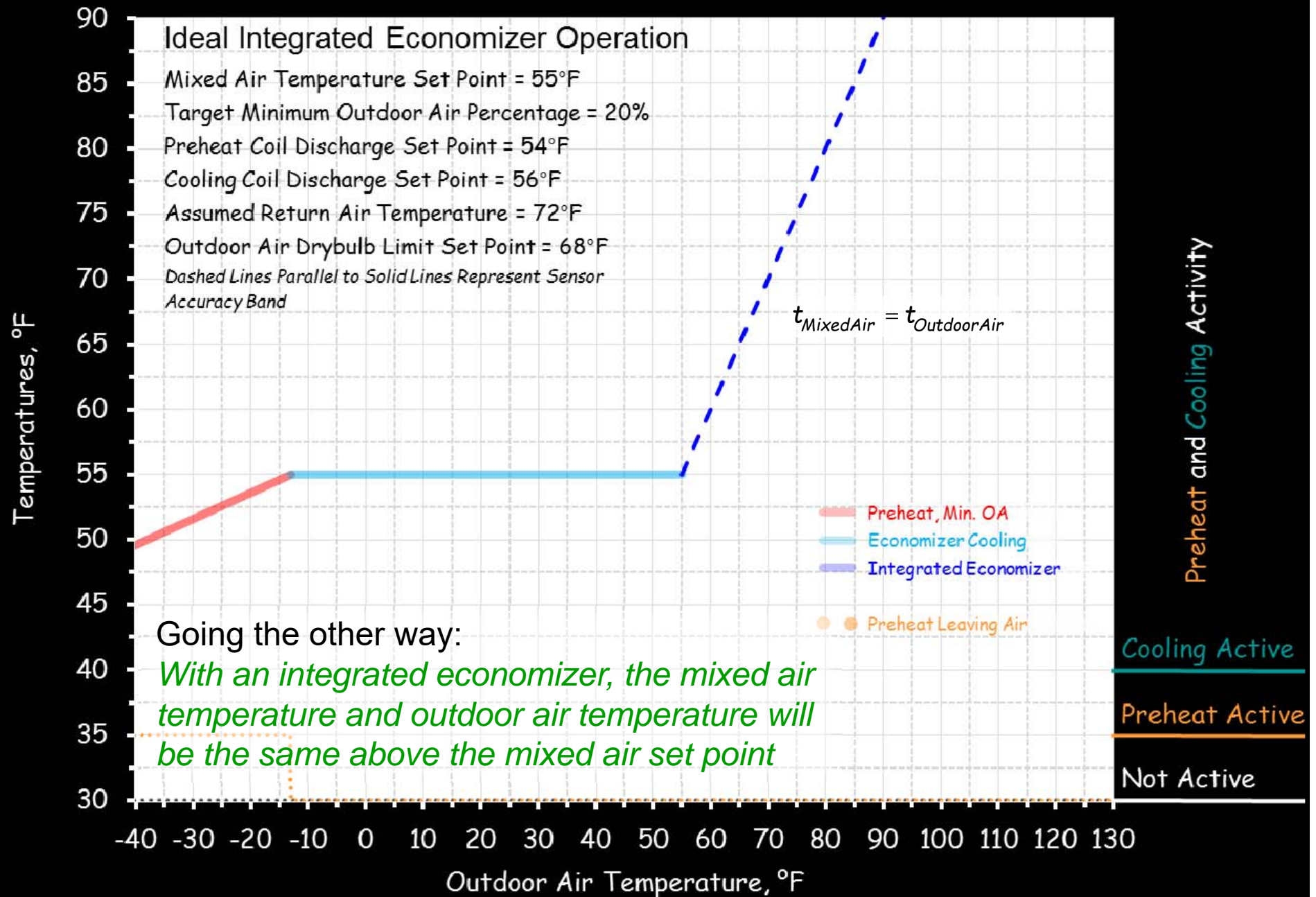


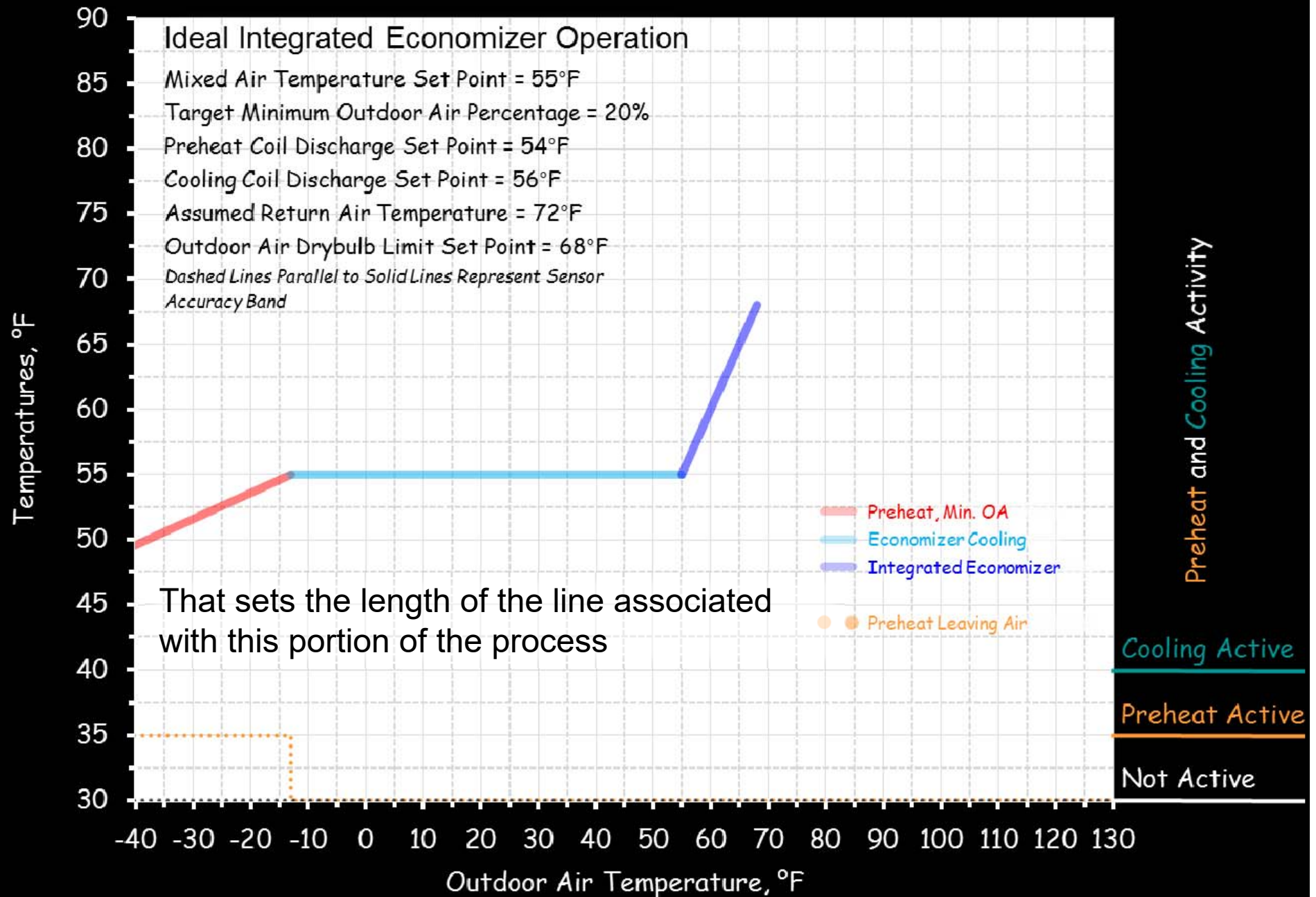
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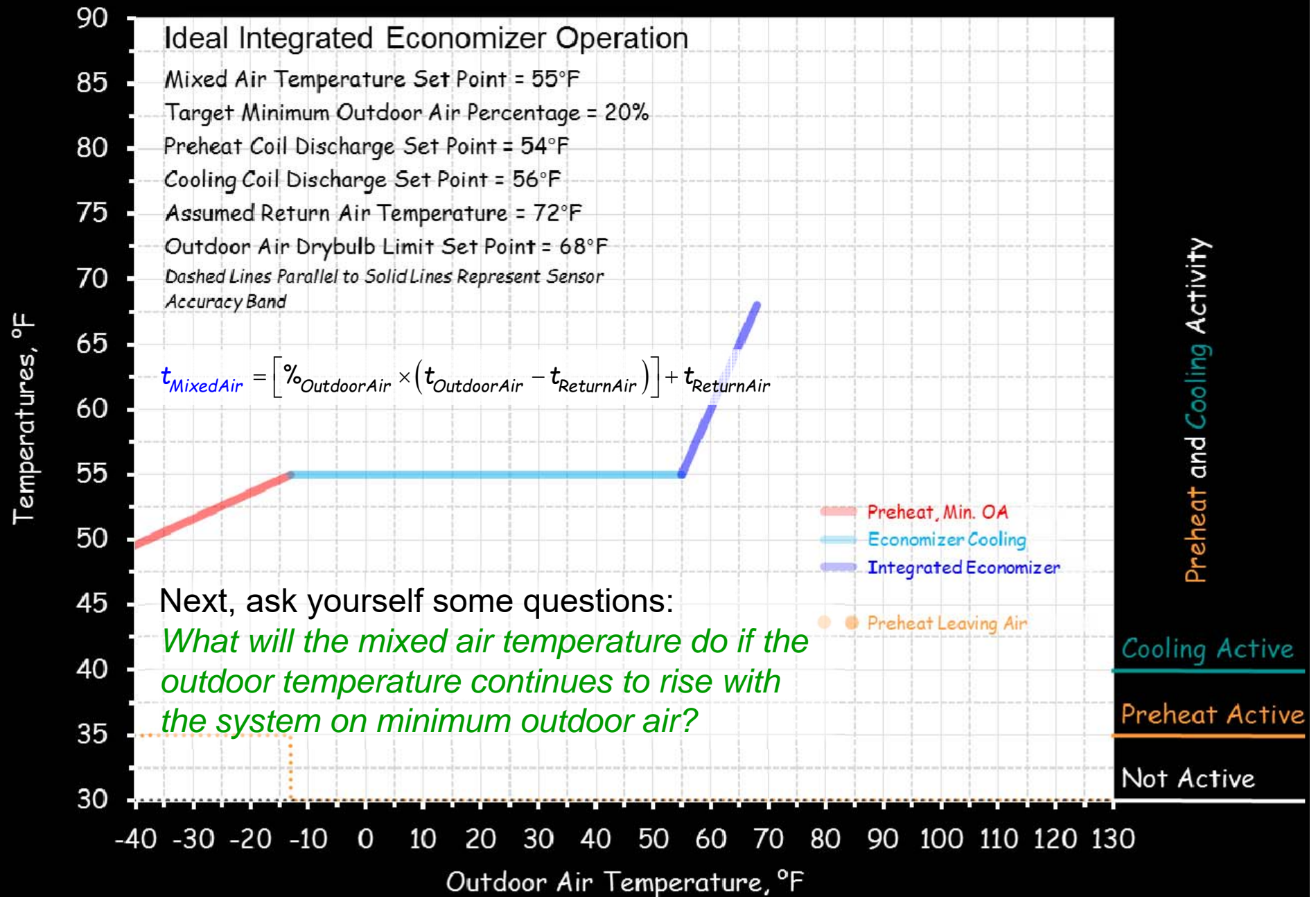


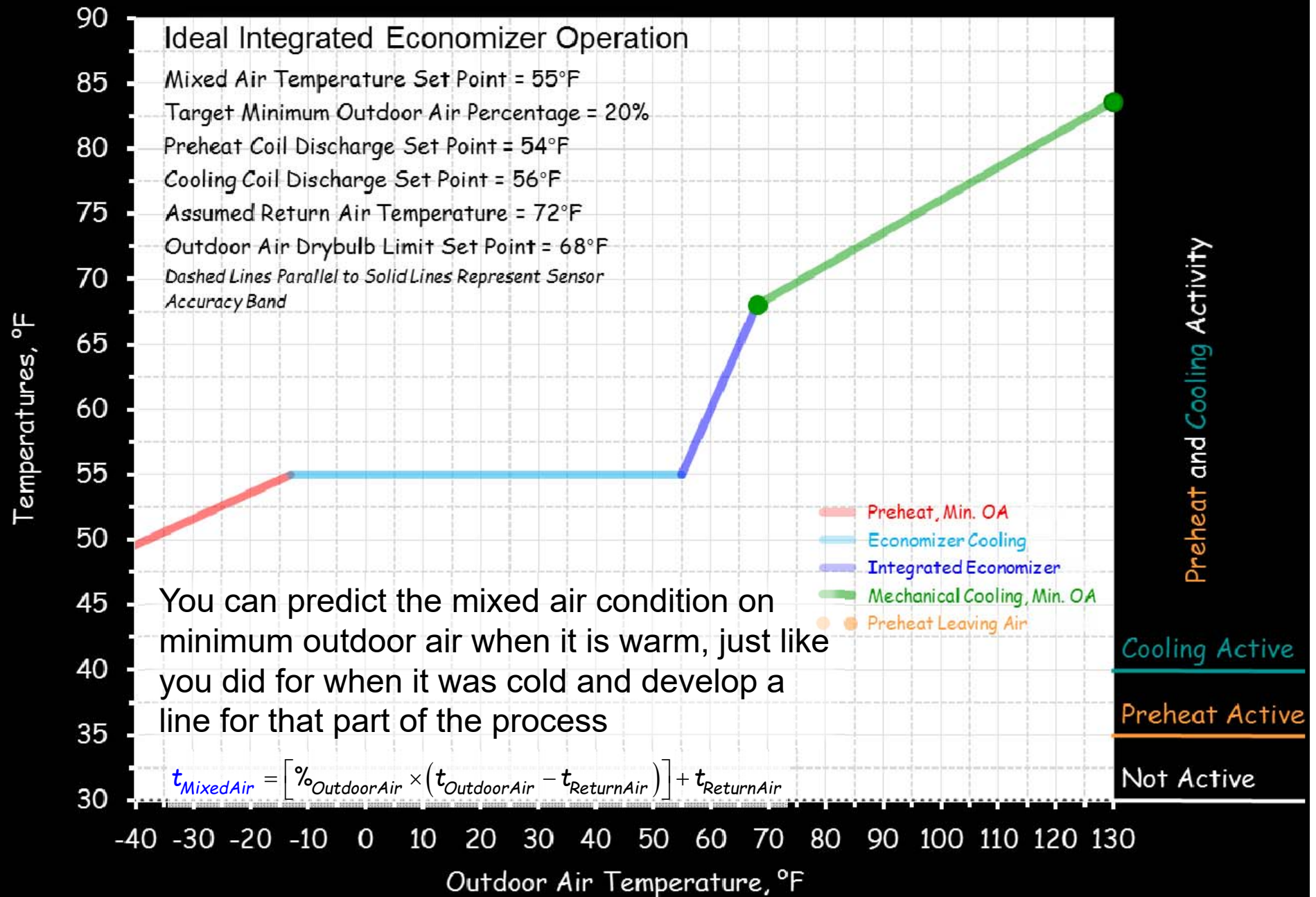
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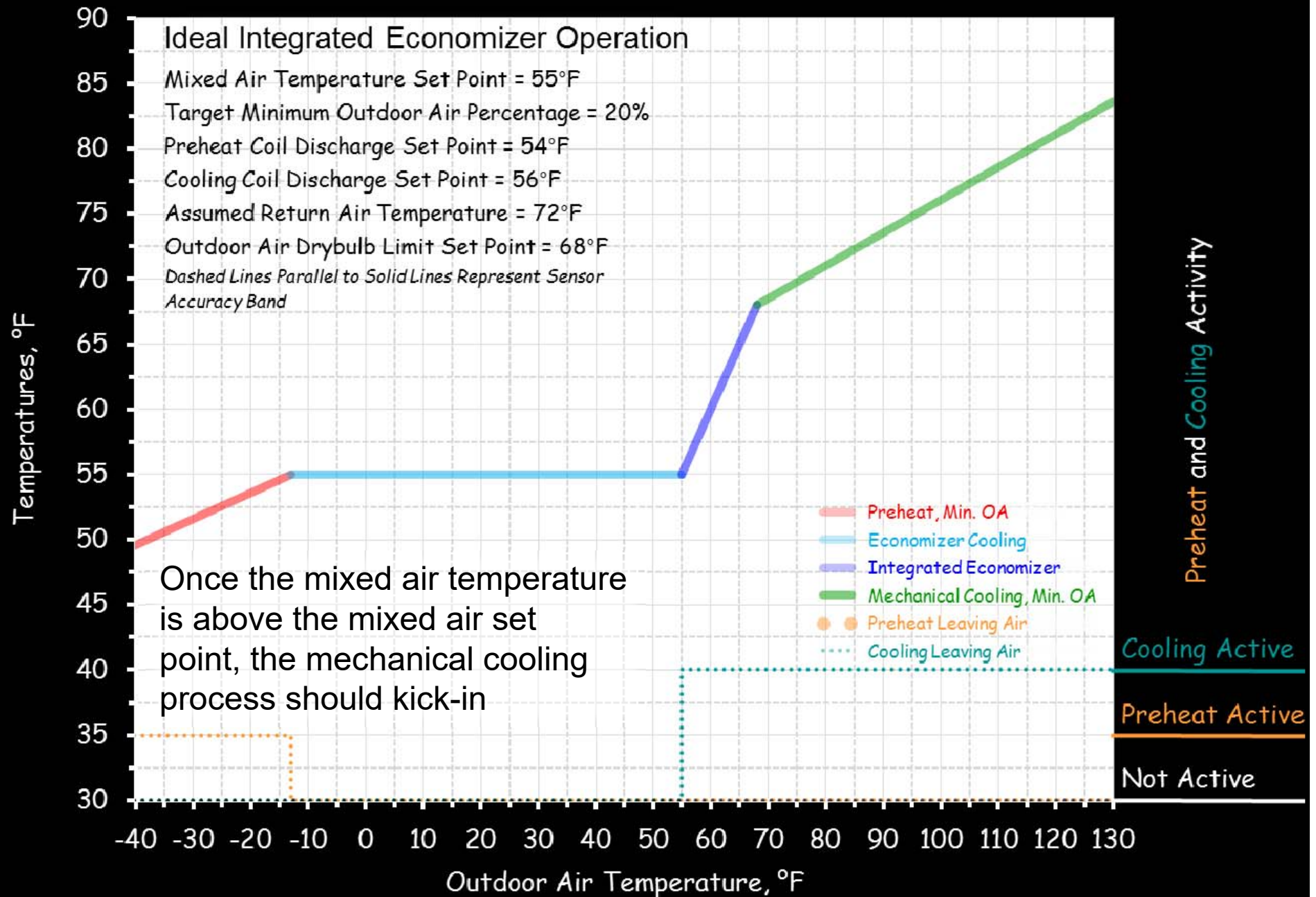




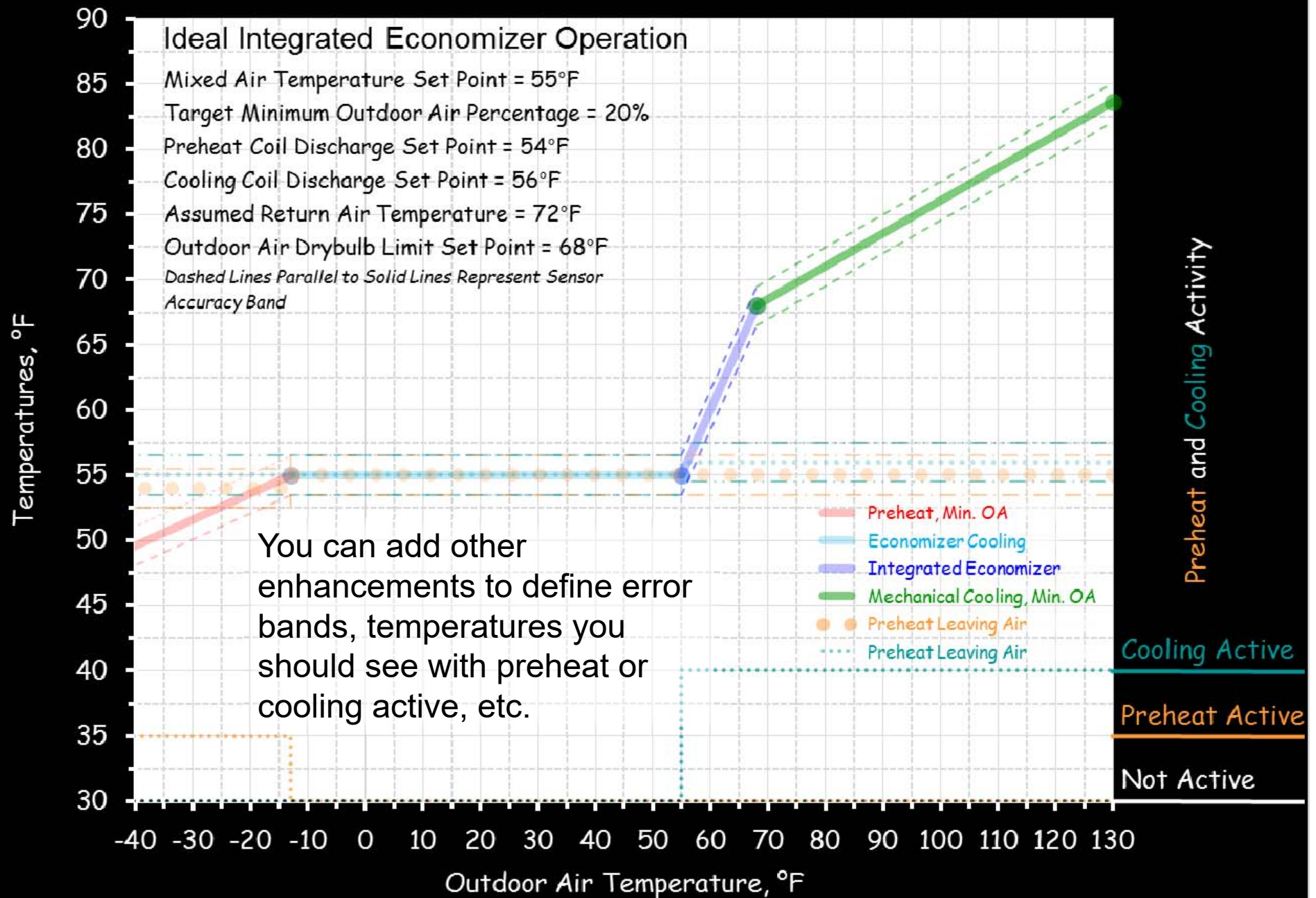




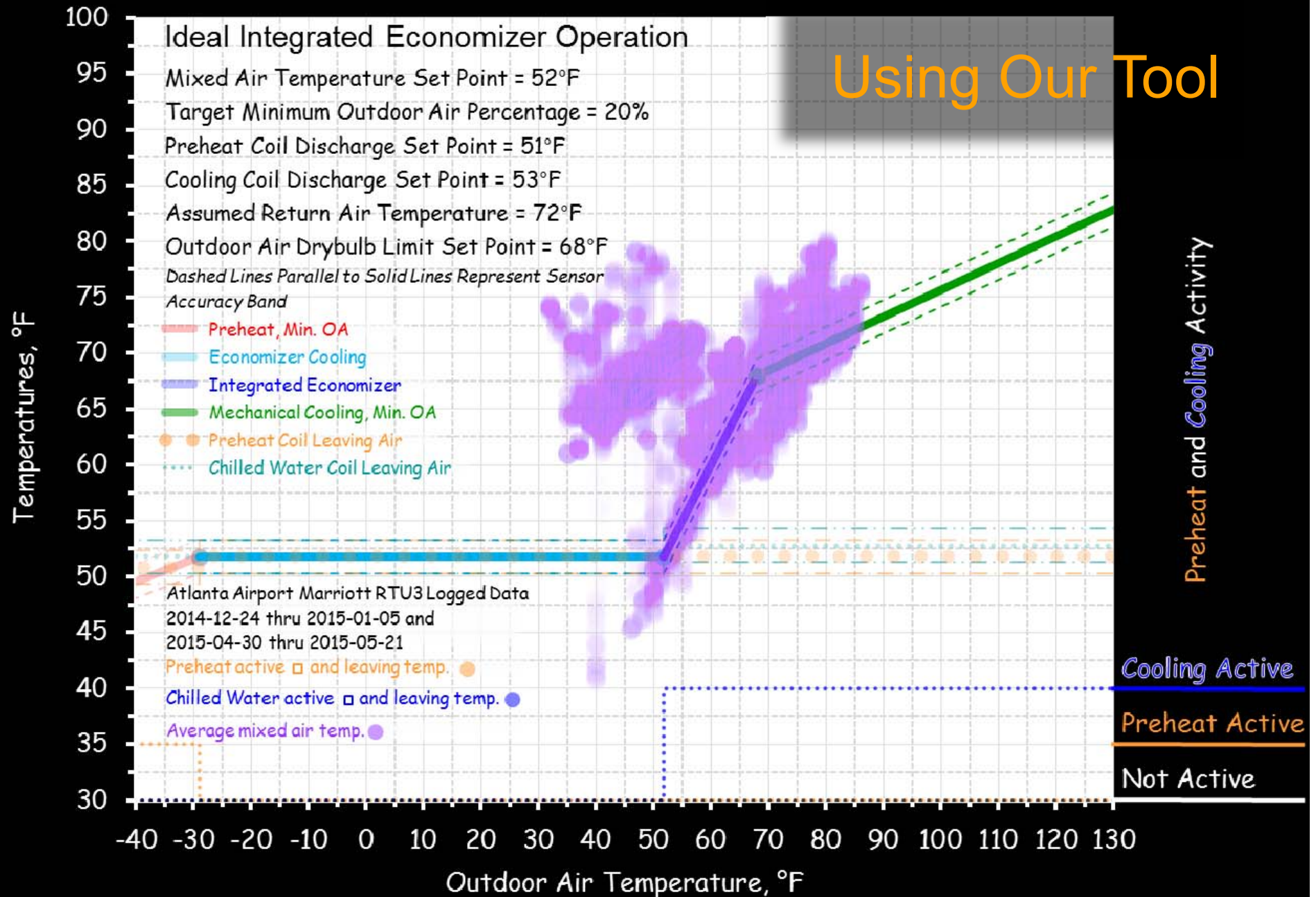
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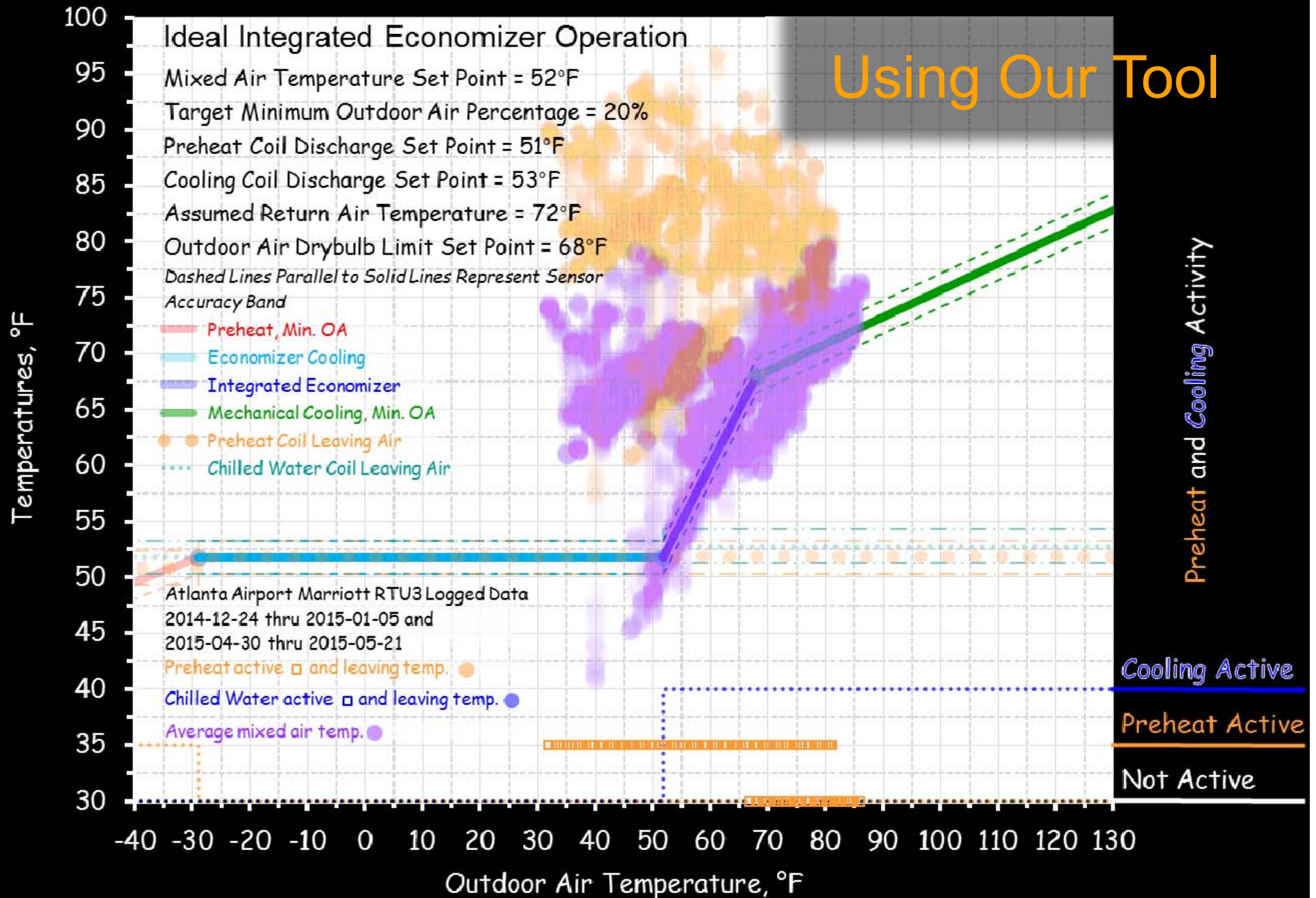


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Using Our Tool





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